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# galpy Documentation

*Release v0.1*

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galpy is a python package for galactic dynamics. It supports orbit integration in a variety of potentials, evaluating and sampling various distribution functions, and the calculation of action-angle coordinates for all static potentials.



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## Quick-start guide

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### 1.1 Installation

galpy can be installed using pip as:

```
> pip install galpy
```

or to upgrade without upgrading the dependencies:

```
> pip install -U --no-deps galpy
```

Some advanced features require the GNU Scientific Library (GSL; see below). If you want to use these, install the GSL first (or install it later and re-install using the upgrade command above).

galpy can also be installed from the source code downloaded from github using the standard python `setup.py` installation:

```
> python setup.py install
```

or:

```
> python setup.py install --prefix=~/local
```

for a local installation. A basic installation works with just the numpy/scipy/matplotlib stack. Some basic tests can be performed by executing:

```
> nosetests -v -w nose/
```

#### 1.1.1 Advanced installation

Certain advanced features require the GNU Scientific Library ([GSL](#)), with action calculations requiring version 1.14 or higher. On a Mac you can make sure that the correct architecture is installed using [Homebrew](#) as:

```
> brew install gsl --universal
```

You should be able to check your version using:

```
> gsl-config --version
```

Other advanced features, including calculating the normalization of certain distribution functions using Gauss-Legendre integration require numpy version 1.7.0 or higher.

## 1.2 Introduction

The most basic features of galpy are its ability to display rotation curves and perform orbit integration for arbitrary combinations of potentials. This section introduce the most basic features of `galpy.potential` and `galpy.orbit`.

### 1.2.1 Rotation curves

The following code example shows how to initialize a Miyamoto-Nagai disk potential and plot its rotation curve

```
>>> from galpy.potential import MiyamotoNagaiPotential
>>> mp= MiyamotoNagaiPotential(a=0.5,b=0.0375,normalize=1.)
>>> mp.plotRotcurve(Rrange=[0.01,10.],grid=1001)
```

The `normalize=1.` option normalizes the potential such that the radial force is a fraction `normalize=1.` of the radial force necessary to make the circular velocity 1 at R=1.

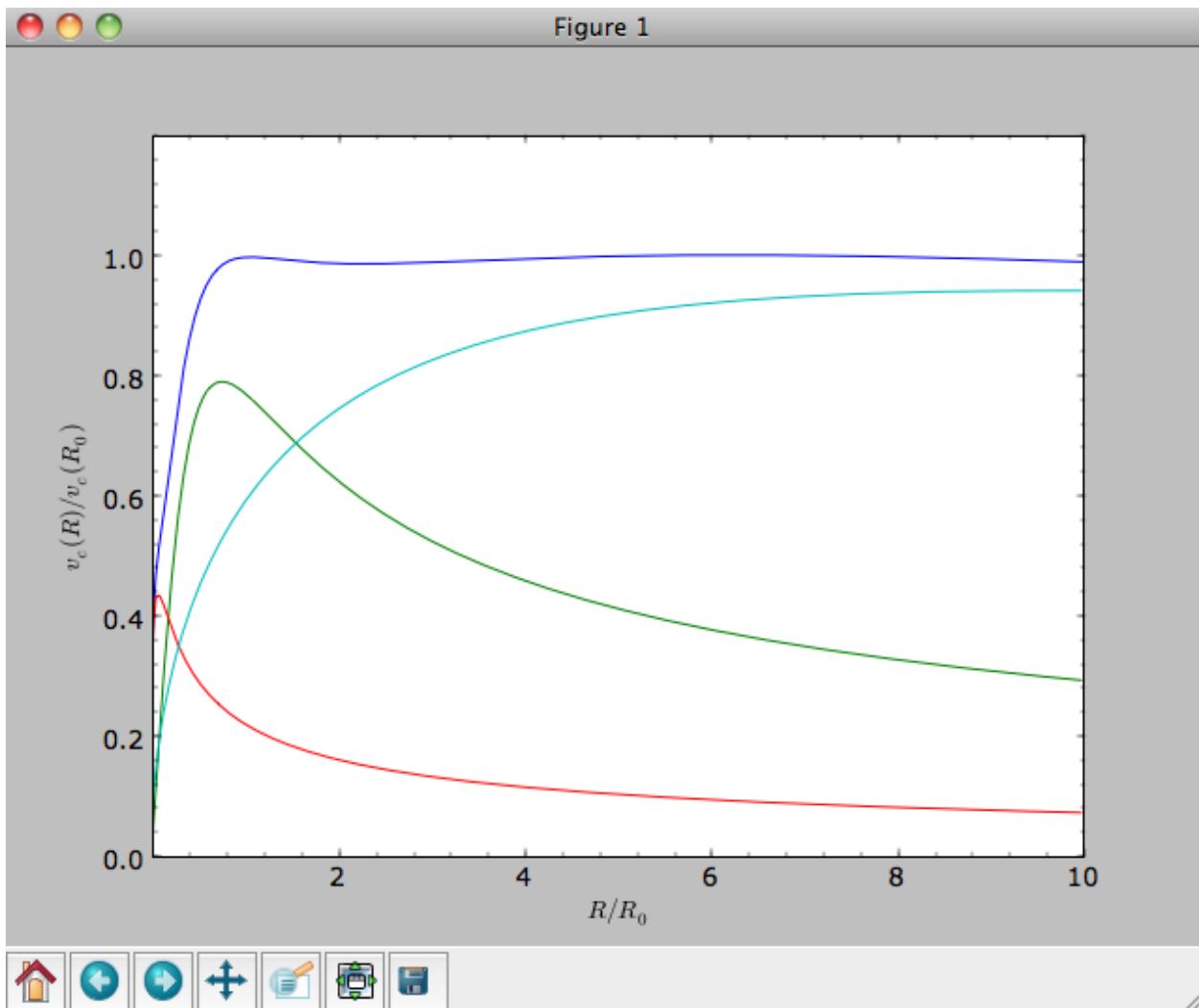
Similarly we can initialize other potentials and plot the combined rotation curve

```
>>> from galpy.potential import NFWPotential, HernquistPotential
>>> mp= MiyamotoNagaiPotential(a=0.5,b=0.0375,normalize=.6)
>>> np= NFWPotential(a=4.5,normalize=.35)
>>> hp= HernquistPotential(a=0.6/8,normalize=0.05)
>>> from galpy.potential import plotRotcurve
>>> plotRotcurve([hp,mp,np],Rrange=[0.01,10.],grid=1001,yrange=[0.,1.2])
```

Note that the `normalize` values add up to 1. such that the circular velocity will be 1 at R=1. The resulting rotation curve is approximately flat. To show the rotation curves of the three components do

```
>>> mp.plotRotcurve(Rrange=[0.01,10.],grid=1001,overplot=True)
>>> hp.plotRotcurve(Rrange=[0.01,10.],grid=1001,overplot=True)
>>> np.plotRotcurve(Rrange=[0.01,10.],grid=1001,overplot=True)
```

You'll see the following



As a shortcut the [hp, mp, np] Milky-Way-like potential is defined as

```
>>> from galpy.potential import MWPotential
```

## 1.2.2 Units in galpy

Above we normalized the potentials such that they give a circular velocity of 1 at  $R=1$ . These are the standard galpy units (sometimes referred to as *natural units* in the documentation). galpy will work most robustly when using these natural units. When using galpy to model a real galaxy with, say, a circular velocity of 220 km/s at  $R=8$  kpc, all of the velocities should be scaled as  $v = V/[220 \text{ km/s}]$  and all of the positions should be scaled as  $x = X/[8 \text{ kpc}]$  when using galpy's natural units.

For convenience, a utility module `bovy_conversion` is included in galpy that helps in converting between physical units and natural units for various quantities. For example, in natural units the orbital time of a circular orbit at  $R=1$  is  $2\pi$ ; in physical units this corresponds to

```
>>> from galpy.util import bovy_conversion
>>> print 2.*numpy.pi*bovy_conversion.time_in_Gyr(220.,8.)
0.223405444283
```

or about 223 Myr. We can also express forces in various physical units. For example, for the Milky-Way-like potential defined in galpy, we have that the vertical force at 1.1 kpc is

```
>>> from galpy.potential import MWPotential, evaluatezforces
>>> -evaluatezforces(1., 1.1/8., MWPotential) *bovy_conversion.force_in_pcMyr2(220., 8.)
2.3941221528330314
```

which we can also express as an equivalent surface-density by dividing by  $2\pi G$

```
>>> -evaluatezforces(1., 1.1/8., MWPotential) *bovy_conversion.force_in_2piGmsolpc2(220., 8.)
84.681625645335686
```

Because the vertical force at the solar circle in the Milky Way at 1.1 kpc above the plane is approximately  $70 (2\pi G M_\odot \text{ pc}^{-2})$  (e.g., 2013arXiv1309.0809B), this shows that our Milky-Way-like potential has a bit too heavy of a disk.

bovy\_conversion further has functions to convert densities, masses, surface densities, and frequencies to physical units (actions are considered to be too obvious to be included); see [here](#) for a full list. As a final example, the local dark matter density in the Milky-Way-like potential is given by

```
>>> MWPotential[1].dens(1., 0.) *bovy_conversion.dens_in_msolpc3(220., 8.)
0.0085853601686596628
```

or about  $0.0085 M_\odot \text{ pc}^{-3}$ , in line with current measurements (e.g., 2012ApJ...756...89B).

### 1.2.3 Orbit integration

We can also integrate orbits in all galpy potentials. Going back to a simple Miyamoto-Nagai potential, we initialize an orbit as follows

```
>>> from galpy.orbit import Orbit
>>> mp= MiyamotoNagaiPotential(a=0.5,b=0.0375,amp=1.,normalize=1.)
>>> o= Orbit(vxvv=[1.,0.1,1.1,0.,0.1])
```

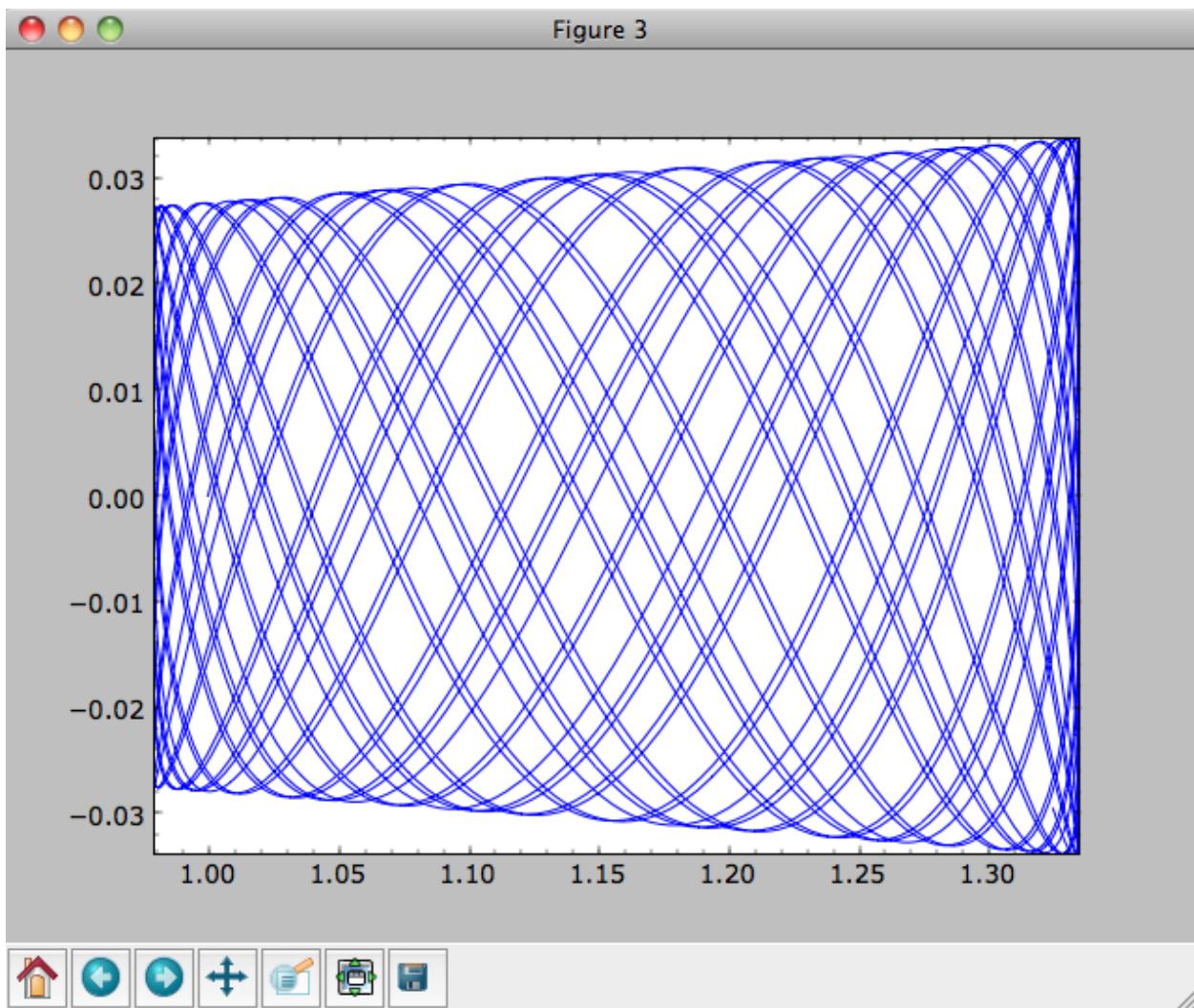
Since we gave Orbit() a five-dimensional initial condition [R, vR, vT, z, vz], we assume we are dealing with a three-dimensional axisymmetric potential in which we do not wish to track the azimuth. We then integrate the orbit for a set of times ts

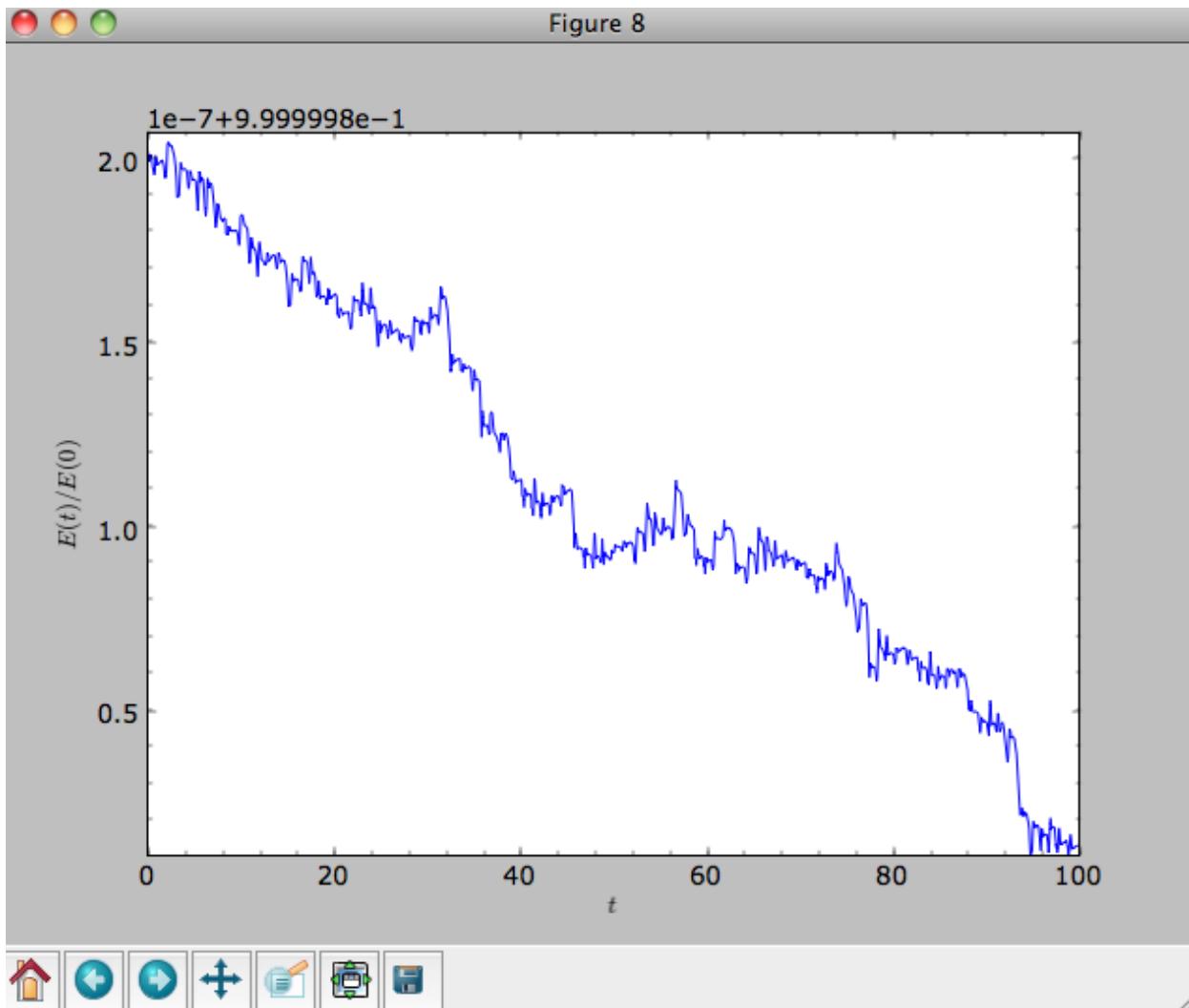
```
>>> import numpy
>>> ts= numpy.linspace(0,100,10000)
>>> o.integrate(ts,mp)
```

Now we plot the resulting orbit as

```
>>> o.plot()
```

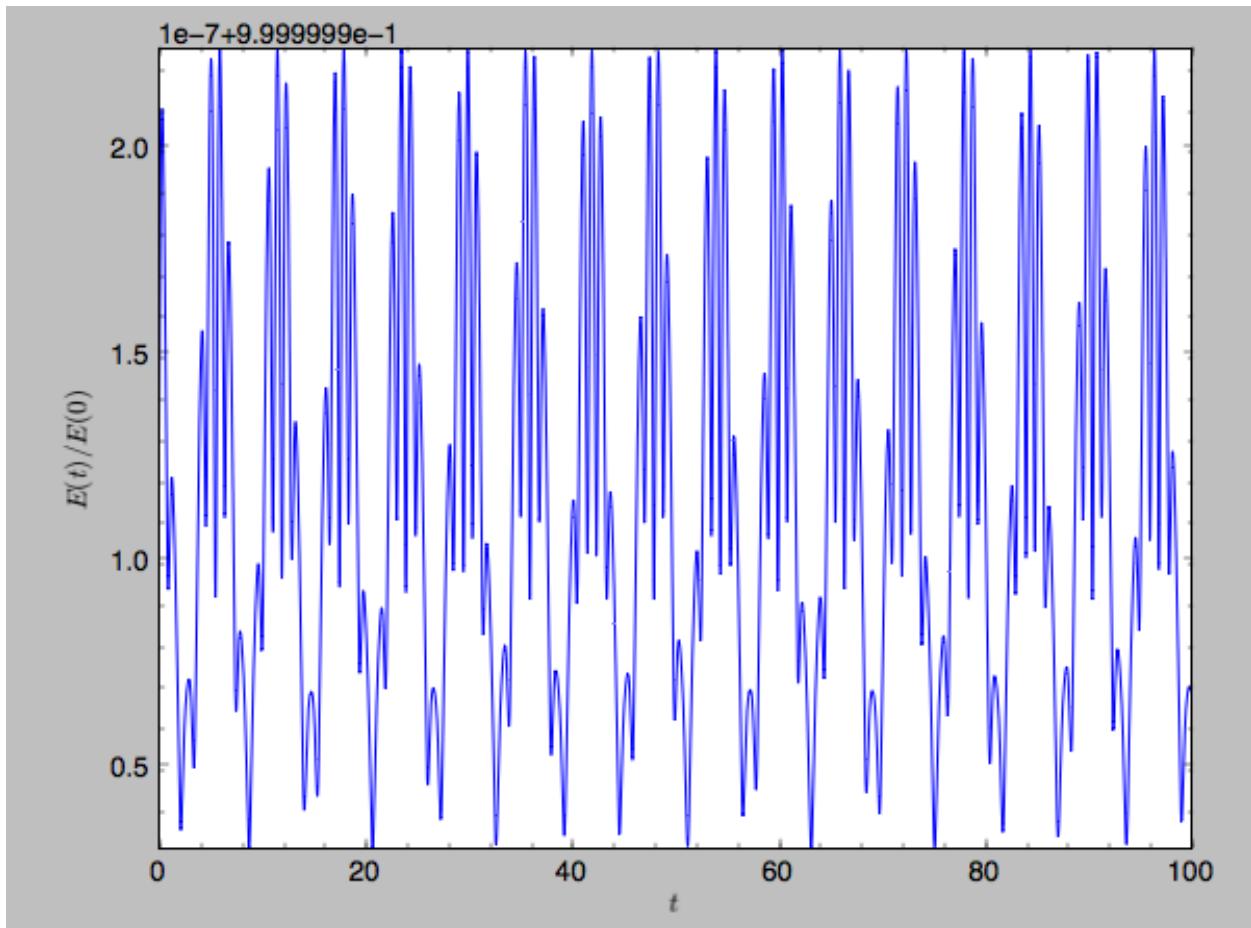
Which gives





When we use a symplectic leapfrog integrator, we see that the energy error remains constant

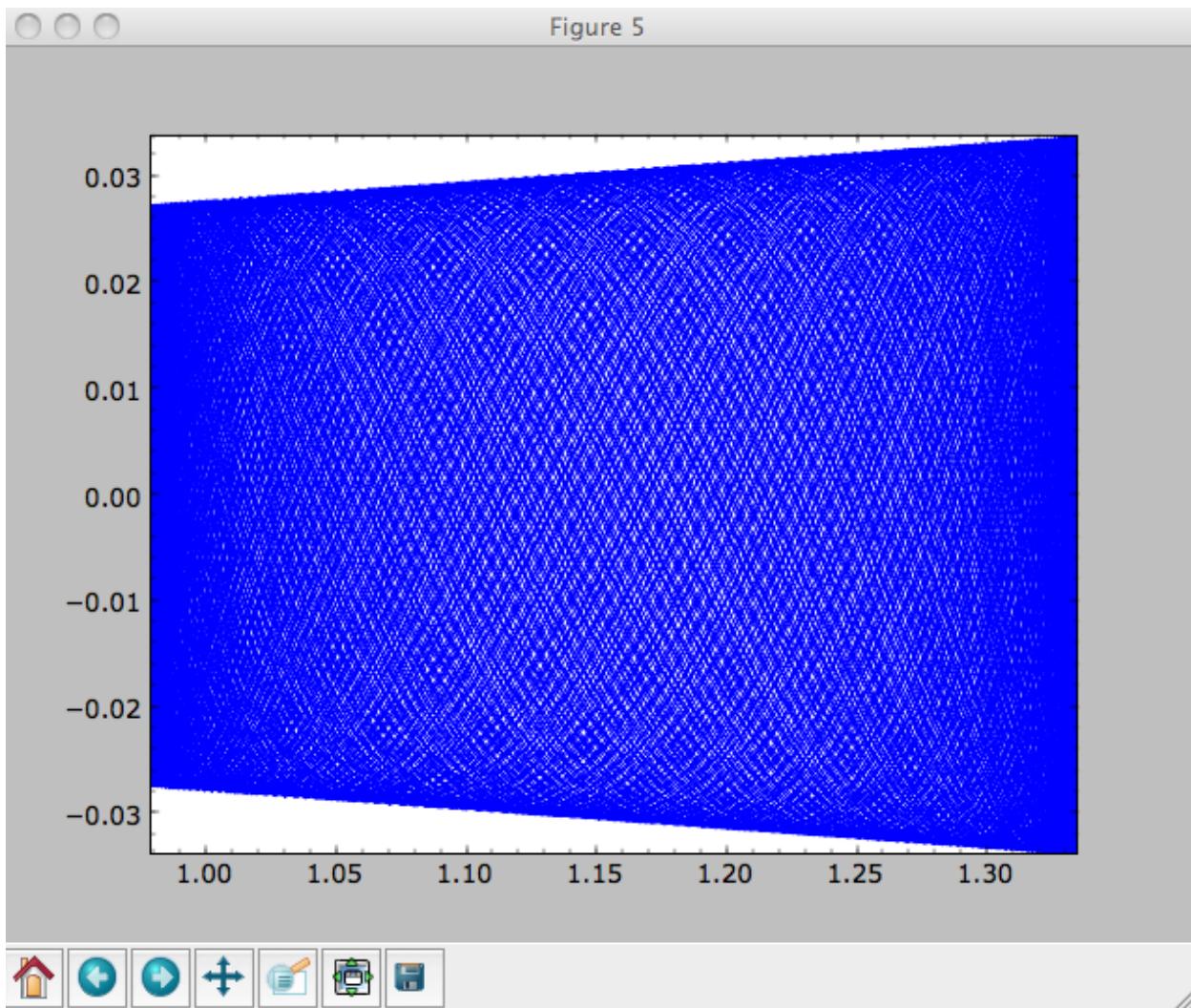
```
>>> o.integrate(ts,mp,method='leapfrog')
>>> o.plotE(xlabel=r'$t$',ylabel=r'$E(t)/E(0)$')
```



Because stars have typically only orbited the center of their galaxy tens of times, using symplectic integrators is mostly unnecessary (compared to planetary systems which orbits millions or billions of times). galpy contains fast integrators written in C, which can be accessed through the `method=` keyword (e.g., `integrate(...,method='dopr54_c')` is a fast high-order Dormand-Prince method).

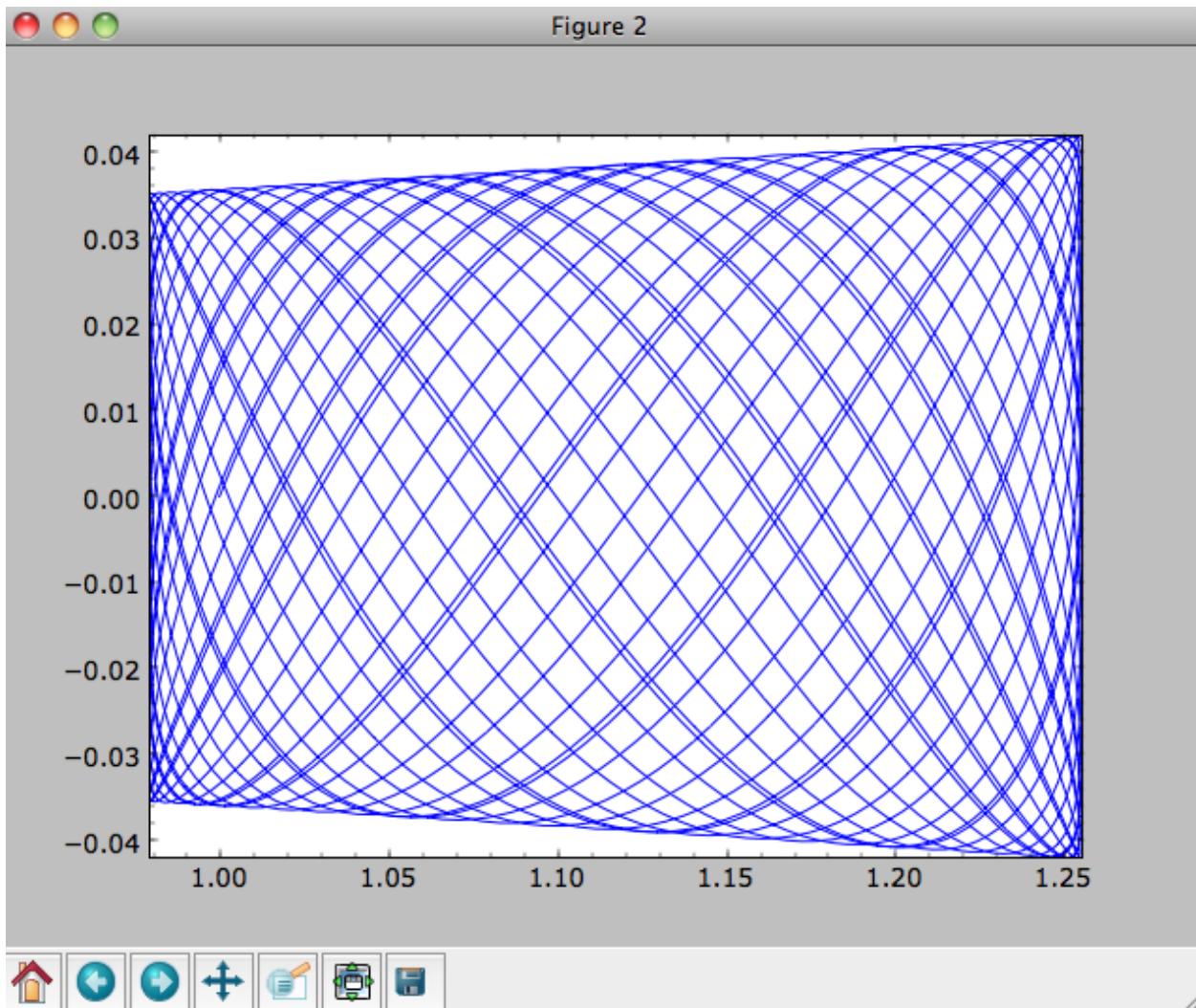
When we integrate for much longer we see how the orbit fills up a torus (this could take a minute)

```
>>> ts= numpy.linspace(0,1000,10000)
>>> o.integrate(ts,mp)
>>> o.plot()
```



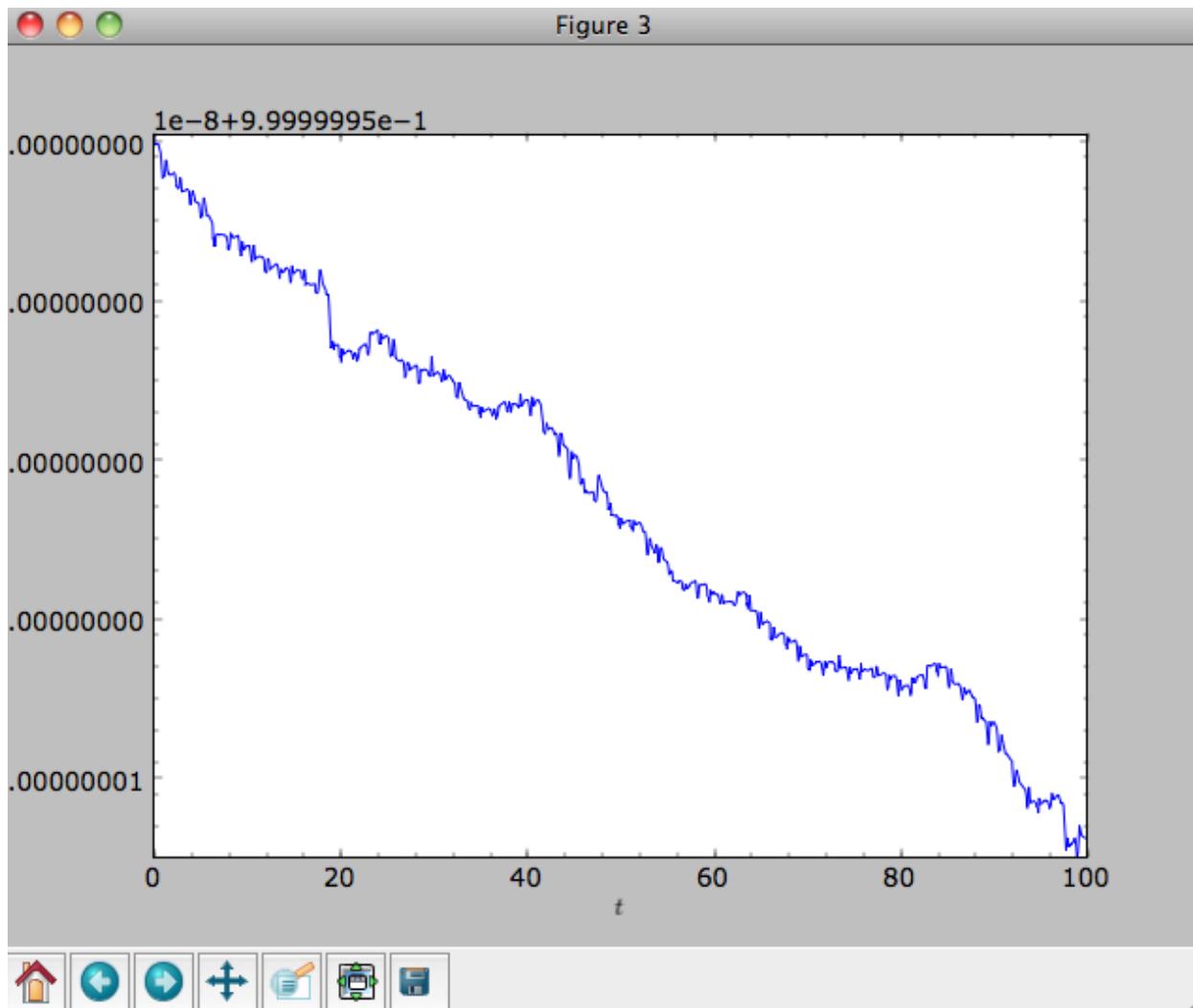
As before, we can also integrate orbits in combinations of potentials. Assuming `mp`, `np`, and `hp` were defined as above, we can

```
>>> ts= numpy.linspace(0,100,10000)
>>> o.integrate(ts,[mp,hp,np])
>>> o.plot()
```



Energy is again approximately conserved

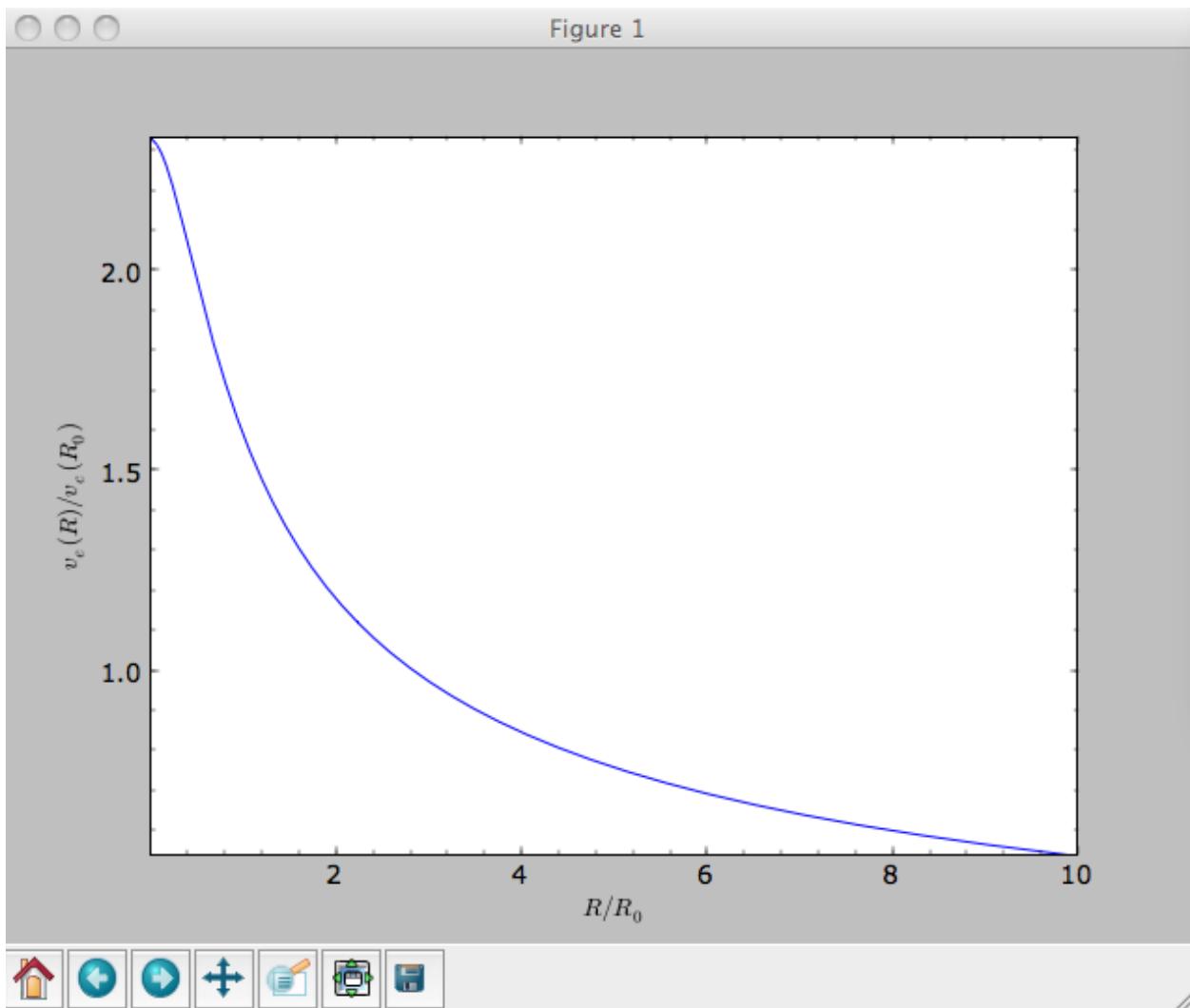
```
>>> o.plotE(xlabel=r'$t$', ylabel=r'$E(t)/E(0)$')
```



#### 1.2.4 Escape velocity curves

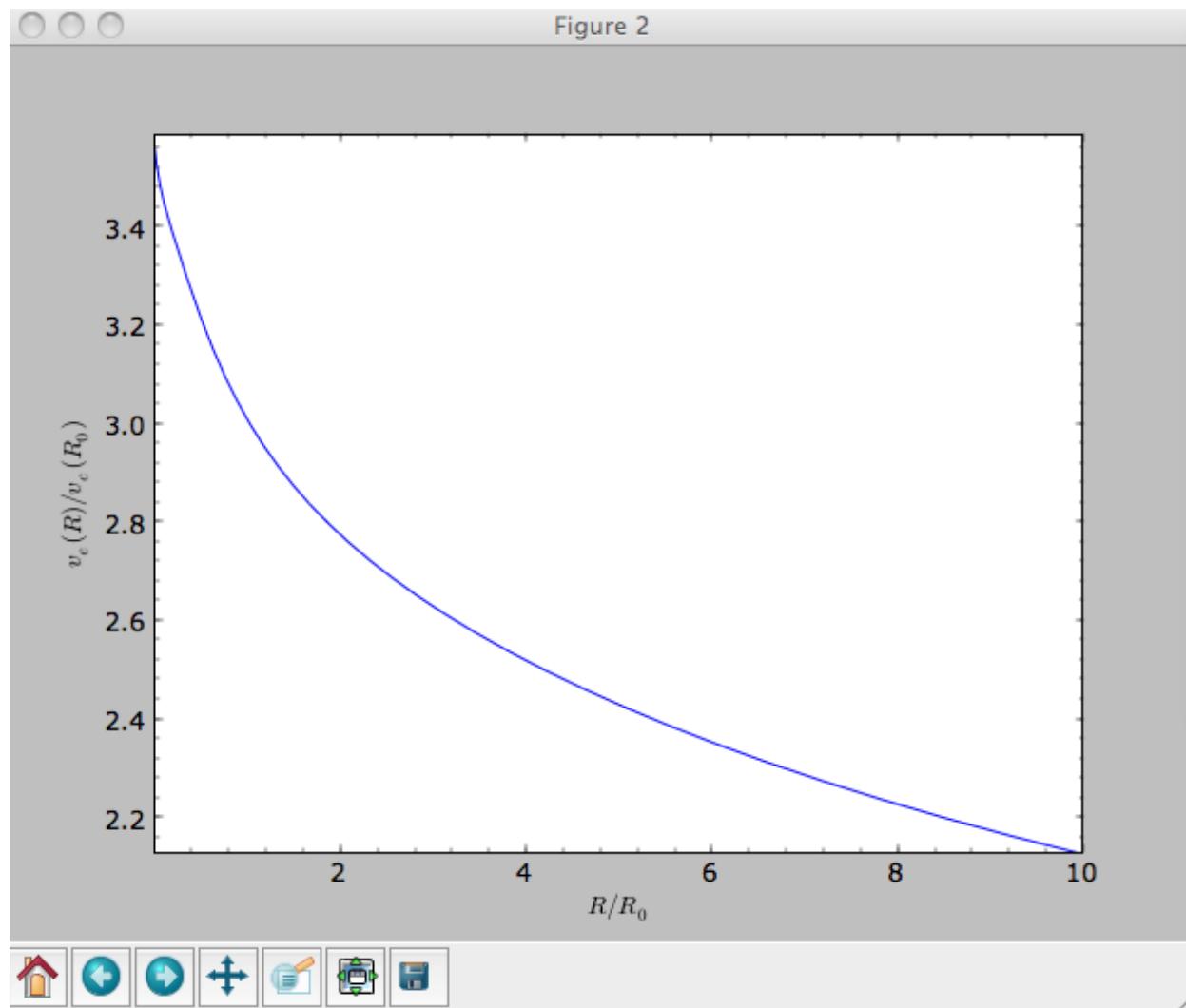
Just like we can plot the rotation curve for a potential or a combination of potentials, we can plot the escape velocity curve. For example, the escape velocity curve for the Miyamoto-Nagai disk defined above

```
>>> mp.plotEscapecurve(Rrange=[0.01,10.],grid=1001)
```



or of the combination of potentials defined above

```
>>> from galpy.potential import plotEscapecurve  
>>> plotEscapecurve([mp, hp, np], Rrange=[0.01, 10.], grid=1001)
```



## 1.3 Potentials in galpy

galpy contains a large variety of potentials in `galpy.potential` that can be used for orbit integration, the calculation of action-angle coordinates, as part of steady-state distribution functions, and to study the properties of gravitational potentials. This section introduces some of these features.

### 1.3.1 Potentials and forces

Various 3D and 2D potentials are contained in galpy, list in the *API page*. Another way to list the latest overview of potentials included with galpy is to run

```
>>> import galpy.potential
>>> print [p for p in dir(galpy.potential) if 'Potential' in p]
['CosmphiDiskPotential',
 'DehnenBarPotential',
 'DoubleExponentialDiskPotential',
 'EllipticalDiskPotential',
 'FlattenedPowerPotential',
```

```
'HernquistPotential',
....]
```

(list cut here for brevity). Section *Rotation curves* explains how to initialize potentials and how to display the rotation curve of single Potential instances or of combinations of such instances. Similarly, we can evaluate a Potential instance

```
>>> from galpy.potential import MiyamotoNagaiPotential
>>> mp= MiyamotoNagaiPotential(a=0.5,b=0.0375,normalize=1.)
>>> mp(1.,0.)
-1.2889062500000001
```

Most member functions of Potential instances have corresponding functions in the galpy.potential module that allow them to be evaluated for lists of multiple Potential instances. galpy.potential.MWPotential is such a list of three Potential instances

```
>>> from galpy.potential import MWPotential
>>> print MWPotential
[<galpy.potential_src.MiyamotoNagaiPotential.MiyamotoNagaiPotential instance at 0x1078d5c20>, <galpy.
```

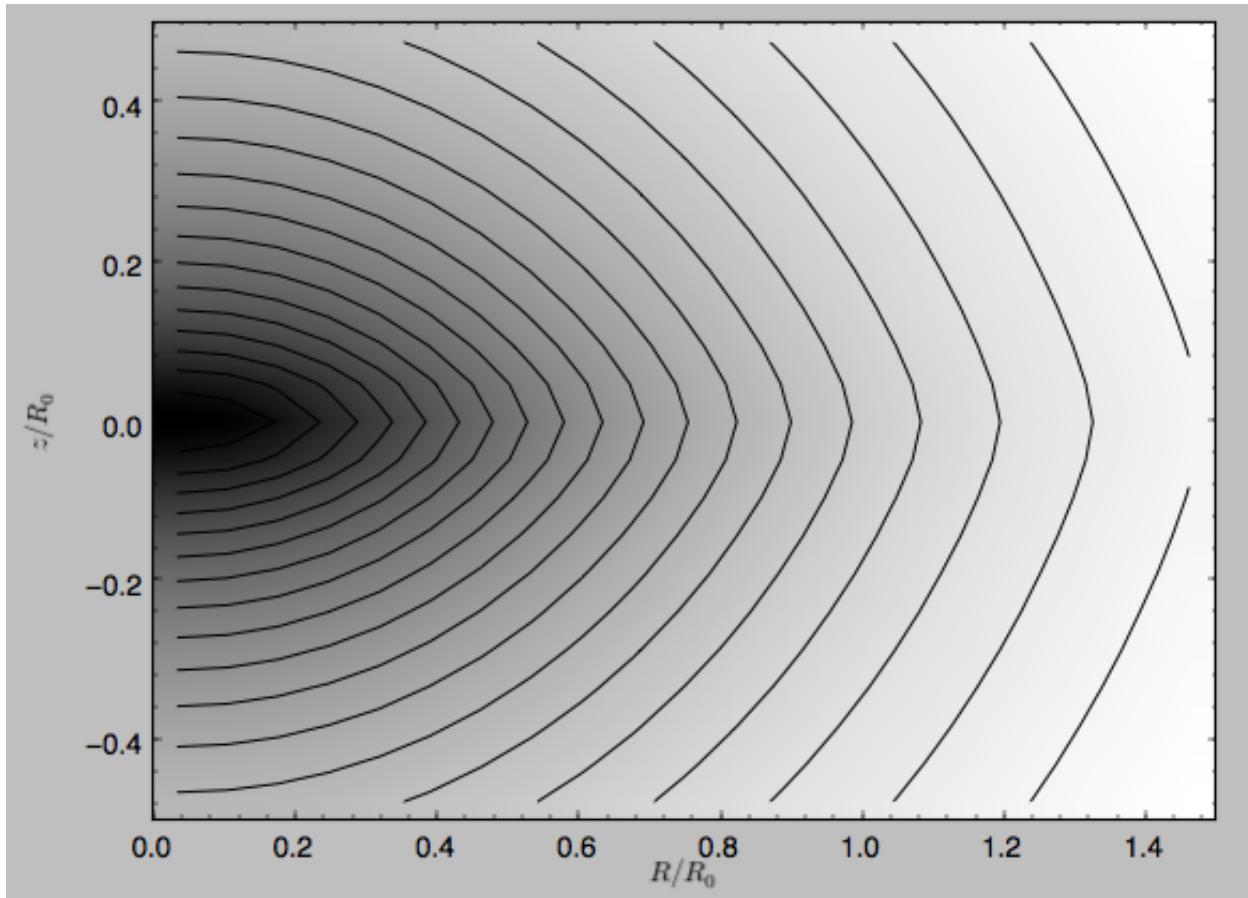
and we can evaluate the potential by using the evaluatePotentials function

```
>>> from galpy.potential import evaluatePotentials
>>> evaluatePotentials(1.,0.,MWPotential)
-4.5525780402192924
```

We can plot the potential of axisymmetric potentials (or of non-axisymmetric potentials at phi=0) using the plot member function

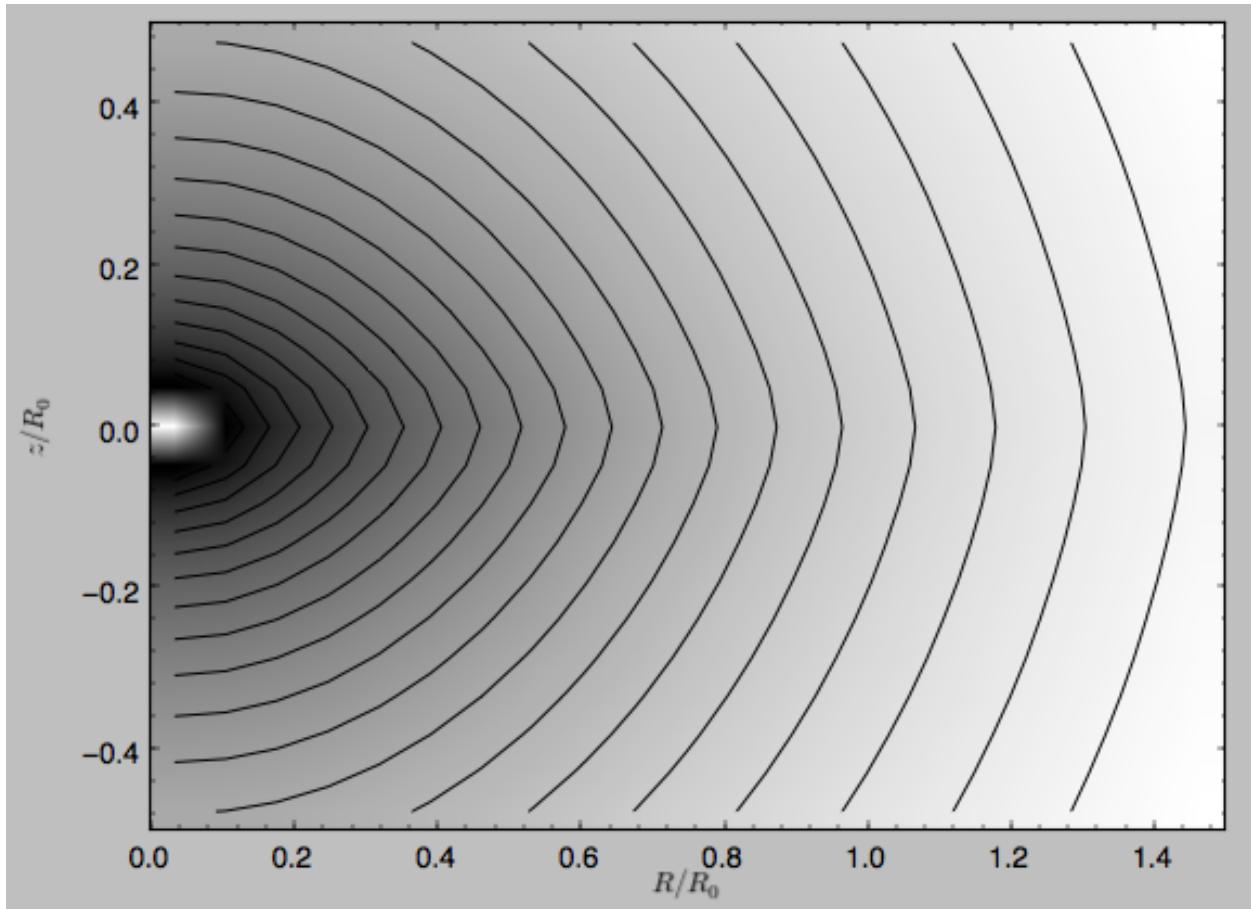
```
>>> mp.plot()
```

which produces the following plot



Similarly, we can plot combinations of Potentials using `plotPotentials`, e.g.,

```
>>> plotPotentials(MWPotential)
```



These functions have arguments that can provide custom  $R$  and  $z$  ranges for the plot, the number of grid points, the number of contours, and many other parameters determining the appearance of these figures.

galpy also allows the forces corresponding to a gravitational potential to be calculated. Again for the Miyamoto-Nagai Potential instance from above

```
>>> mp.Rforce(1., 0.)
-1.0
```

This value of -1.0 is due to the normalization of the potential such that the circular velocity is 1. at  $R=1$ . Similarly, the vertical force is zero in the mid-plane

```
>>> mp.zforce(1., 0.)
-0.0
```

but not further from the mid-plane

```
>>> mp.zforce(1., 0.125)
-0.53488743705310848
```

As explained in *Units in galpy*, these forces are in standard galpy units, and we can convert them to physical units using methods in the `galpy.util.bovy_conversion` module. For example, assuming a physical circular velocity of 220 km/s at  $R=8$  kpc

```
>>> from galpy.util import bovy_conversion
>>> mp.zforce(1., 0.125)*bovy_conversion.force_in_kmsMyr(220., 8.)
-3.3095671288657584 #km/s/Myr
>>> mp.zforce(1., 0.125)*bovy_conversion.force_in_2piGmsolpc2(220., 8.)
```

```
-119.72021771473301 #2 \pi G Msol / pc^2
```

Again, there are functions in `galpy.potential` that allow for the evaluation of the forces for lists of Potential instances, such that

```
>>> from galpy.potential import evaluateRforces
>>> evaluateRforces(1.,0.,MWPotential)
-1.0
>>> from galpy.potential import evaluatezforces
>>> evaluatezforces(1.,0.125,MWPotential)*bovy_conversion.force_in_2piGmsolpc2(220.,8.)
>>> -82.898379883714099 #2 \pi G Msol / pc^2
```

We can evaluate the flattening of the potential as  $\sqrt{|z F_R/R F_Z|}$  for a Potential instance as well as for a list of such instances

```
>>> mp.flattening(1.,0.125)
0.4549542914935209
>>> from galpy.potential import flattening
>>> flattening(MWPotential,1.,0.125)
0.5593251065691105
```

### 1.3.2 Densities

galpy can also calculate the densities corresponding to gravitational potentials. For many potentials, the densities are explicitly implemented, but if they are not, the density is calculated using the Poisson equation (second derivatives of the potential have to be implemented for this). For example, for the Miyamoto-Nagai potential, the density is explicitly implemented

```
>>> mp.dens(1.,0.)
1.1145444383277576
```

and we can also calculate this using the Poisson equation

```
>>> mp.dens(1.,0.,forcepoisson=True)
1.1145444383277574
```

which are the same to machine precision

```
>>> mp.dens(1.,0.,forcepoisson=True)-mp.dens(1.,0.)
-2.2204460492503131e-16
```

Similarly, all of the potentials in `galpy.potential.MWPotential` have explicitly-implemented densities, so we can do

```
>>> from galpy.potential import evaluateDensities
>>> evaluateDensities(1.,0.,MWPotential)
0.71812049194200644
```

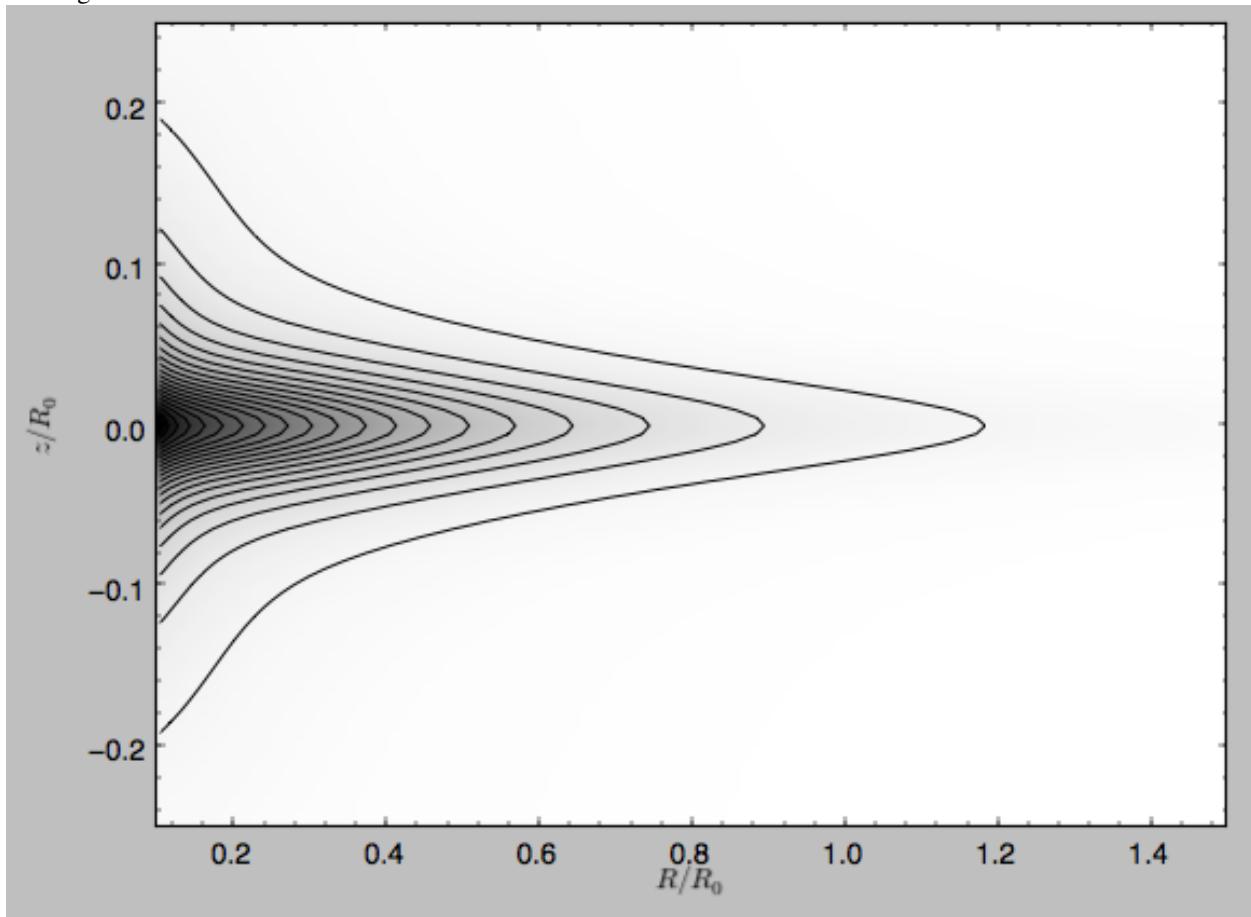
In physical coordinates, this becomes

```
>>> evaluateDensities(1.,0.,MWPotential)*bovy_conversion.dens_in_msolpc3(220.,8.)
0.1262386383150029 #Msol / pc^3
```

We can also plot densities

```
>>> from galpy.potential import plotDensities
>>> plotDensities(MWPotential,rmin=0.1,zmax=0.25,zmin=-0.25,nrs=101,nzs=101)
```

which gives



Another example of this is for an exponential disk potential

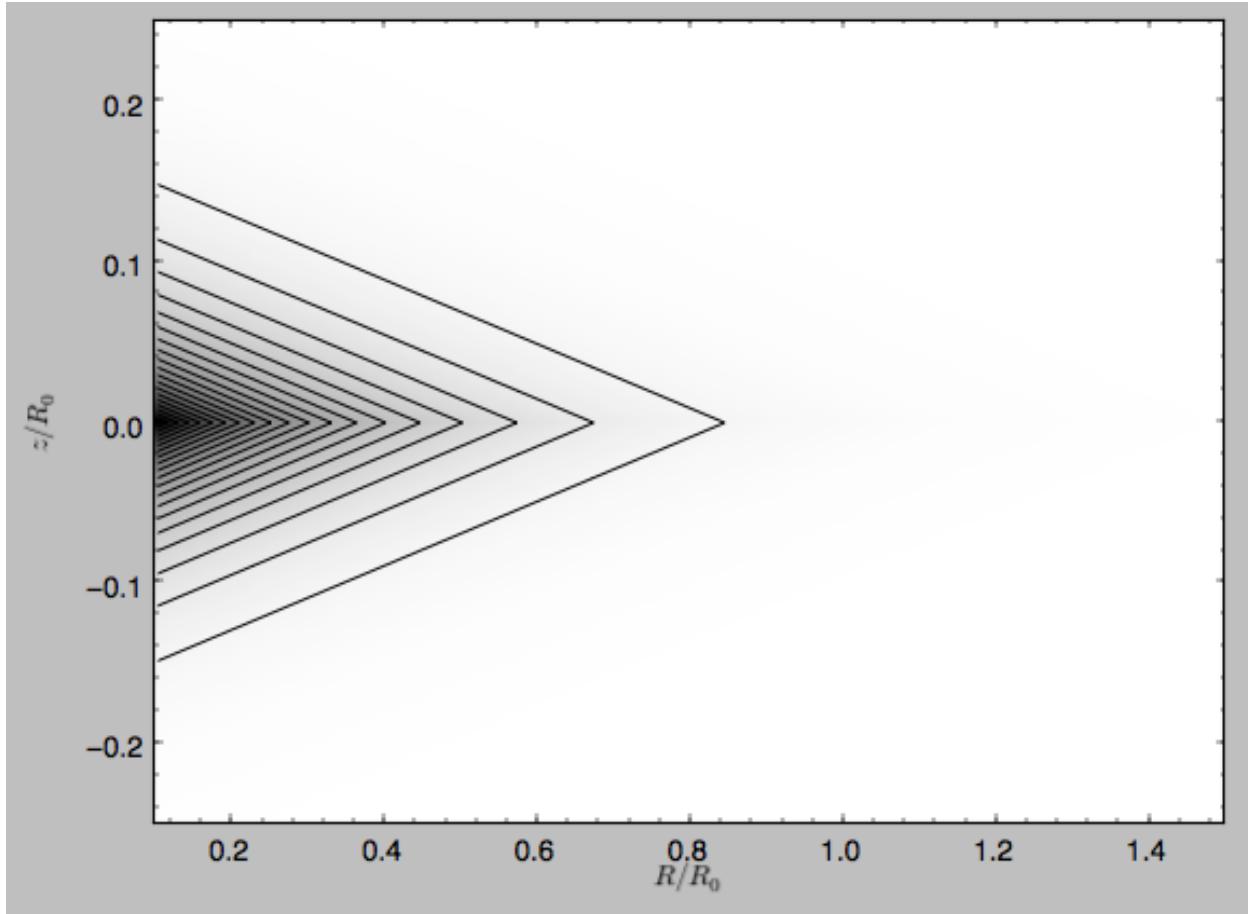
```
>>> from galpy.potential import DoubleExponentialDiskPotential
>>> dp= DoubleExponentialDiskPotential(hr=1./4.,hz=1./20.,normalize=1.)
```

The density computed using the Poisson equation now requires multiple numerical integrations, so the agreement between the analytical density and that computed using the Poisson equation is slightly less good, but still better than a percent

```
>>> (dp.dens(1.,0.,forcepoisson=True)-dp.dens(1.,0.))/dp.dens(1.,0.)
0.0032522956769123019
```

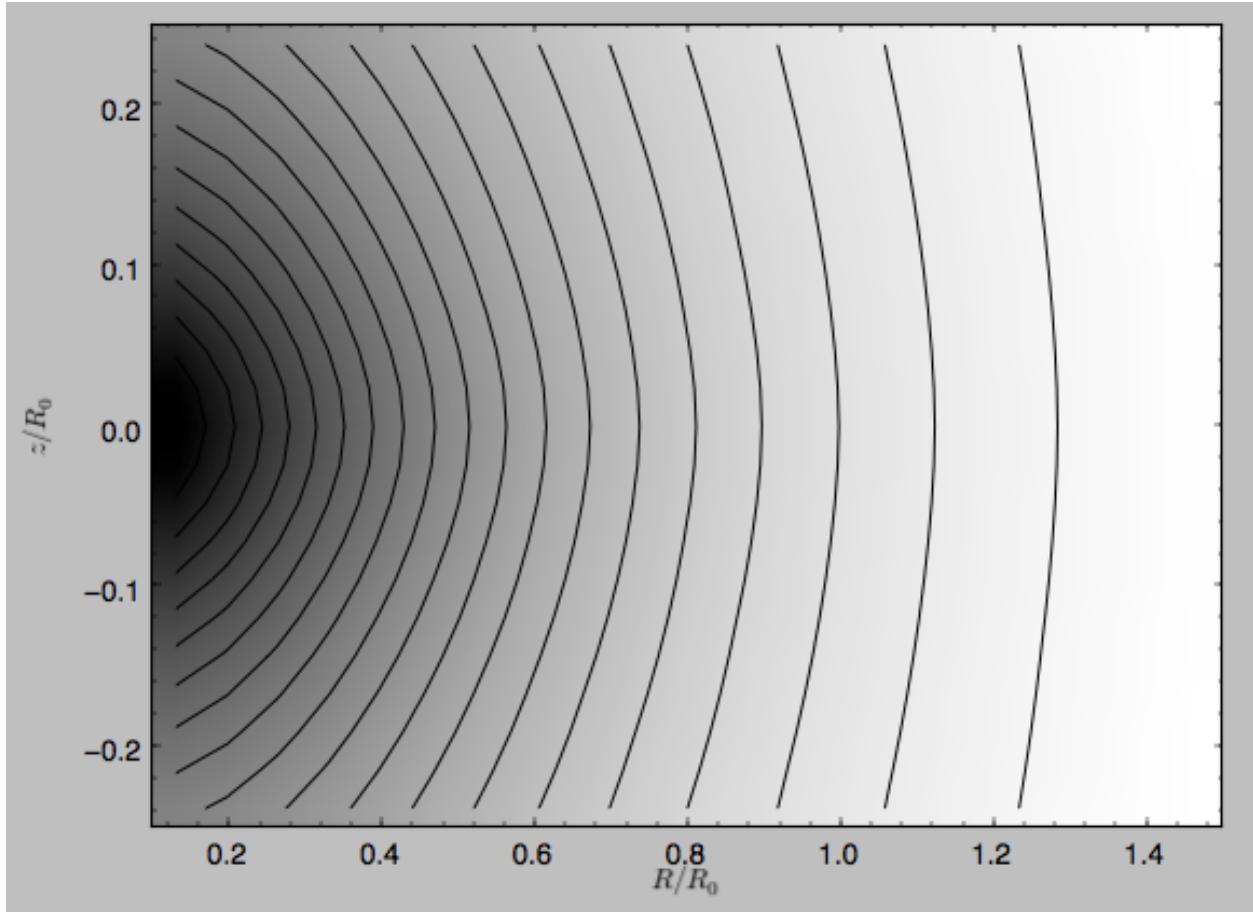
The density is

```
>>> dp.plotDensity(rmin=0.1,zmax=0.25,zmin=-0.25,nrs=101,nzs=101)
```



and the potential is

```
>>> dp.plot(rmin=0.1, zmin=-0.25, zmax=0.25)
```



Clearly, the potential is much less flattened than the density.

### 1.3.3 Close-to-circular orbits and orbital frequencies

We can also compute the properties of close-to-circular orbits. First of all, we can calculate the circular velocity and its derivative

```
>>> mp.vcirc(1.)
1.0
>>> mp.dvcircdR(1.)
-0.163777427566978
```

or, for lists of Potential instances

```
>>> from galpy.potential import vcirc
>>> vcirc(MWPotential,1.)
1.0
>>> from galpy.potential import dvcircdR
>>> dvcircdR(MWPotential,1.)
0.012084123754590059
```

We can also calculate the various frequencies for close-to-circular orbits. For example, the rotational frequency

```
>>> mp.omegac(0.8)
1.2784598203204887
>>> from galpy.potential import omegac
```

```
>>> omegac(MWPotential,0.8)
1.2389547535552212
```

and the epicycle frequency

```
>>> mp.epifreq(0.8)
1.7774973530267848
>>> from galpy.potential import epifreq
>>> epifreq(MWPotential,0.8)
1.8144833328444094
```

as well as the vertical frequency

```
>>> mp.verticalfreq(1.0)
3.7859388972001828
>>> from galpy.potential import verticalfreq
>>> verticalfreq(MWPotential,1.)
3.0000000000000004
```

For close-to-circular orbits, we can also compute the radii of the Lindblad resonances. For example, for a frequency similar to that of the Milky Way's bar

```
>>> mp.lindbladR(5./3.,m='corotation') #args are pattern speed and m of pattern
0.6027911166042229 #~ 5kpc
>>> print mp.lindbladR(5./3.,m=2)
None
>>> mp.lindbladR(5./3.,m=-2)
0.9906190683480501
```

The None here means that there is no inner Lindblad resonance, the m=-2 resonance is in the Solar neighborhood (see the section on the *Hercules stream* in this documentation).

### 1.3.4 Adding potentials to the galpy framework

Potentials in galpy can be used in many places such as orbit integration, distribution functions, or the calculation of action-angle variables, and in most cases any instance of a potential class that inherits from the general Potential class (or a list of such instances) can be given. For example, all orbit integration routines work with any list of instances of the general Potential class. Adding new potentials to galpy therefore allows them to be used everywhere in galpy where general Potential instances can be used. Adding a new class of potentials to galpy consists of the following series of steps (some of these are also given in the file README.dev in the galpy distribution):

1. Implement the new potential in a class that inherits from galpy.potential.Potential. The new class should have an `__init__` method that sets up the necessary parameters for the class. An amplitude parameter `amp=` should be taken as an argument for this class and before performing any other setup, the `galpy.potential.Potential.__init__(self, amp=amp)` method should be called to setup the amplitude. To add support for normalizing the potential to standard galpy units, one can call the `galpy.potential.Potential.normalize` function at the end of the `__init__` function.

The new potential class should implement some of the following functions:

- `_evaluate(R, z, phi=0, t=0, dR=0, dphi=0)` which evaluates the potential itself (*without* the amp factor, which is added in the `__call__` method of the general Potential class). This function should also call the relevant derivatives if `dR` or `dphi` is not equal to zero (this is used only in some of the razor-thin disk distribution functions, so doing this properly is not that important).
- `_Rforce(self, R, z, phi=0., t=0.)` which evaluates the radial force in cylindrical coordinates (-d potential / d R).

- `_zforce(self,R,z,phi=0.,t=0.)` which evaluates the vertical force in cylindrical coordinates (-d potential / d z).
- `_R2deriv(self,R,z,phi=0.,t=0.)` which evaluates the second (cylindrical) radial derivative of the potential ( $d^2$  potential / d  $R^2$ ).
- `_z2deriv(self,R,z,phi=0.,t=0.)` which evaluates the second (cylindrical) vertical derivative of the potential ( $d^2$  potential / d  $z^2$ ).
- `_Rzderiv(self,R,z,phi=0.,t=0.)` which evaluates the mixed (cylindrical) radial and vertical derivative of the potential ( $d^2$  potential / d  $R$  d  $z$ ).
- `_dens(self,R,z,phi=0.,t=0.)` which evaluates the density. If not given, the density is computed using the Poisson equation from the first and second derivatives of the potential (if all are implemented).
- `_phiforce(self,R,z,phi=0.,t=0.)`: the azimuthal force in cylindrical coordinates (assumed zero if not implemented).
- `_phi2deriv(self,R,z,phi=0.,t=0.)`: the second azimuthal derivative of the potential in cylindrical coordinates ( $d^2$  potential / d  $\phi^2$ ; assumed zero if not given).
- `_Rphideriv(self,R,z,phi=0.,t=0.)`: the mixed radial and azimuthal derivative of the potential in cylindrical coordinates ( $d^2$  potential / d  $R$  d  $\phi$ ; assumed zero if not given).

The code for `galpy.potential.MiyamotoNagaiPotential` gives a good template to follow for 3D axisymmetric potentials. Similarly, the code for `galpy.potential.CosmphiDiskPotential` provides a good template for 2D, non-axisymmetric potentials.

After this step, the new potential will work in any part of galpy that uses pure python potentials. To get the potential to work with the C implementations of orbit integration or action-angle calculations, the potential also has to be implemented in C and the potential has to be passed from python to C.

2. To add a C implementation of the potential, implement it in a .c file under `potential_src/potential_c_ext`. Look at `potential_src/potential_c_ext/LogarithmicHaloPotential.c` for the right format for 3D, axisymmetric potentials, or at `potential_src/potential_c_ext/LopsidedDiskPotential.c` for 2D, non-axisymmetric potentials.

For orbit integration, the functions such as:

- double `LogarithmicHaloPotentialRforce(double R,double Z, double phi,double t,struct potentialArg * potentialArgs)`
- double `LogarithmicHaloPotentialzforce(double R,double Z, double phi,double t,struct potentialArg * potentialArgs)`

are most important. For some of the action-angle calculations

- double `LogarithmicHaloPotentialEval(double R,double Z, double phi,double t,struct potentialArg * potentialArgs)`

is most important (i.e., for those algorithms that evaluate the potential). The arguments of the potential are passed in a `potentialArgs` structure that contains `args`, which are the arguments that should be unpacked. Again, looking at some example code will make this clear. The `potentialArgs` structure is defined in `potential_src/potential_c_ext/galpy_potentials.h`.

3. Add the potential's function declarations to `potential_src/potential_c_ext/galpy_potentials.h`
4. (4. and 5. for planar orbit integration) Edit the code under `orbit_src/orbit_c_ext/integratePlanarOrbit.c` to set up your new potential (in the `parse_leapFuncArgs` function).

5. Edit the code in `orbit_src/integratePlanarOrbit.py` to set up your new potential (in the `_parse_pot` function).
6. Edit the code under `orbit_src/orbit_c_ext/integrateFullOrbit.c` to set up your new potential (in the `parse_leapFuncArgs_Full` function).
7. Edit the code in `orbit_src/integrateFullOrbit.py` to set up your new potential (in the `_parse_pot` function).
8. (for using the `actionAngleStaeckel` methods in C) Edit the code in `actionAngle_src/actionAngle_c_ext/actionAngle.c` to parse the new potential (in the `parse_actionAngleArgs` function).
9. Finally, add `self.hasC= True` to the initialization of the potential in question (after the initialization of the super class, or otherwise it will be undone).

After following the relevant steps, the new potential class can be used in any galpy context in which C is used to speed up computations.

## 1.4 Two-dimensional disk distribution functions

galpy contains various disk distribution functions, both in two and three dimensions. This section introduces the two-dimensional distribution functions, useful for studying the dynamics of stars that stay relatively close to the mid-plane of a galaxy. The vertical motions of these stars may be approximated as being entirely decoupled from the motion in the plane.

### 1.4.1 Types of disk distribution functions

galpy contains the following distribution functions for razor-thin disks: `galpy.df.dehnendf` and `galpy.df.shudf`. These are the distribution functions of Dehnen (1999AJ....118.1201D) and Shu (1969ApJ...158..505S). Everything shown below for `dehnendf` can also be done for `shudf`.

These disk distribution functions are functions of the energy and the angular momentum alone. They can be evaluated for orbits, or for a given energy and angular momentum. At this point, only power-law rotation curves are supported. A `dehnendf` instance is initialized as follows

```
>>> from galpy.df import dehnendf  
>>> dfc= dehnendf(beta=0.)
```

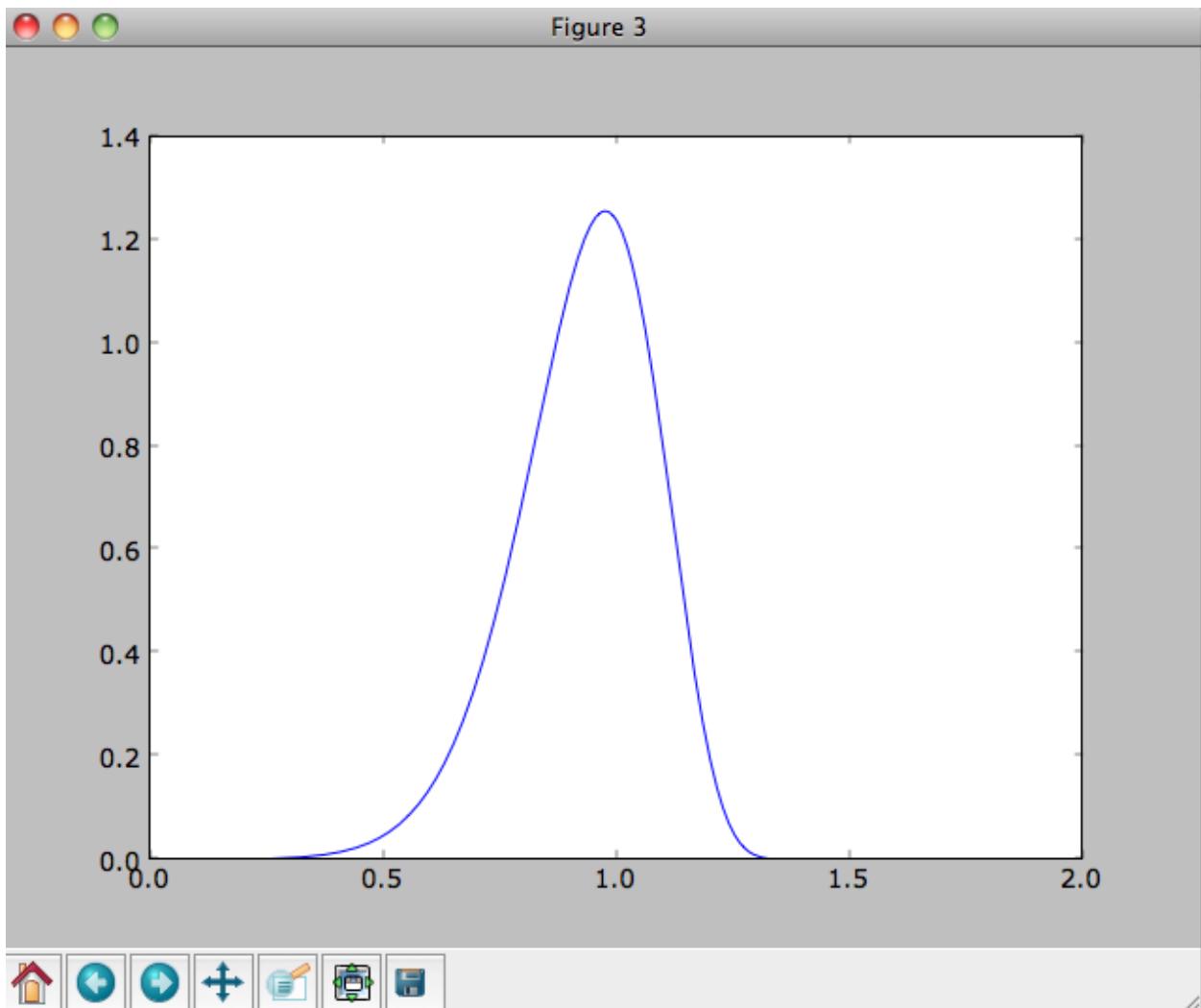
This initializes a `dehnendf` instance based on an exponential surface-mass profile with scale-length 1/3 and an exponential radial-velocity-dispersion profile with scale-length 1 and a value of 0.2 at R=1. Different parameters for these profiles can be provided as an initialization keyword. For example,

```
>>> dfc= dehnendf(beta=0.,profileParams=(1./4.,1.,0.2))
```

initializes the distribution function with a radial scale length of 1/4 instead.

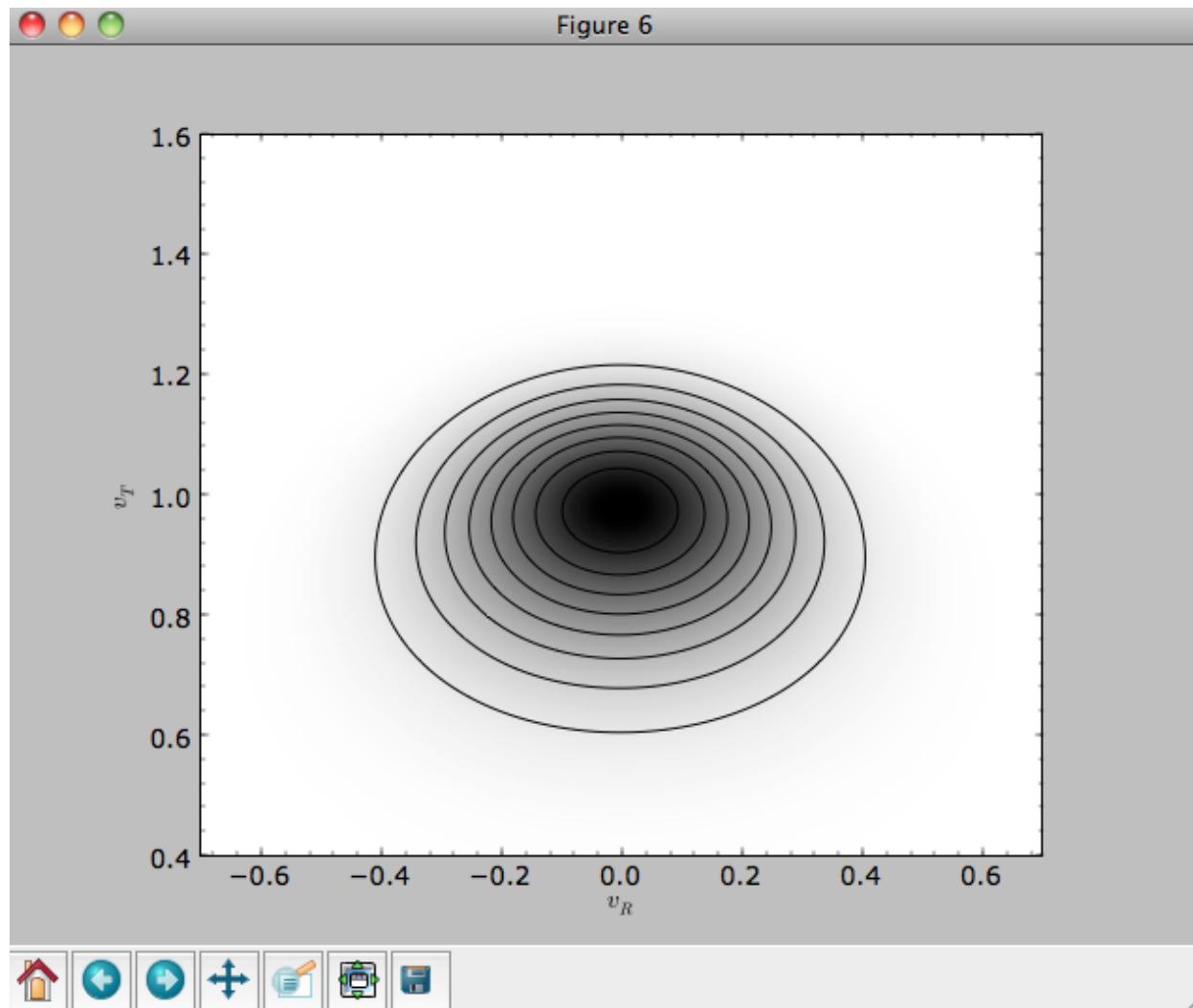
We can show that these distribution functions have an asymmetric drift built-in by evaluating the DF at R=1. We first create a set of orbit-instances and then evaluate the DF at them

```
>>> from galpy.orbit import Orbit  
>>> os= [Orbit([1.,0.,1.+-0.9+1.8/1000*ii]) for ii in range(1001)]  
>>> dfro= [dfc(o) for o in os]  
>>> plot([1.+-0.9+1.8/1000*ii for ii in range(1001)],dfro)
```



Or we can plot the two-dimensional density at  $R=1$ .

```
>>> dfro= [[dfc(Orbit([1.,-0.7+1.4/200*jj,1.-0.6+1.2/200*ii])) for jj in range(201)]for ii in range(201)]
>>> dfro= numpy.array(dfro)
>>> from galpy.util.bovy_plot import bovy_dens2d
>>> bovy_dens2d(dfro,origin='lower',cmap='gist_yarg',contours=True,xrange=[-0.7,0.7],yrange=[0.4,1.6])
```



### 1.4.2 Evaluating moments of the DF

galpy can evaluate various moments of the disk distribution functions. For example, we can calculate the mean velocities (for the DF with a scale length of 1/3 above)

```
>>> dfc.meanvT(1.)
0.91715276979447324
>>> dfc.meanvR(1.)
0.0
```

and the velocity dispersions

```
>>> numpy.sqrt(dfc.sigmaR2(1.))
0.19321086259083936
>>> numpy.sqrt(dfc.sigmat2(1.))
0.15084122011271159
```

and their ratio

```
>>> dfc.sigmaR2(1.)/dfc.sigmat2(1.)
1.6406766813028968
```

In the limit of zero velocity dispersion (the epicycle approximation) this ratio should be equal to 2, which we can check as follows

```
>>> dfccold= dehnendif(beta=0.,profileParams=(1./3.,1.,0.02))
>>> dfccold.sigmaR2(1.)/dfccold.sigmaT2(1.)
1.9947493895454664
```

We can also calculate higher order moments

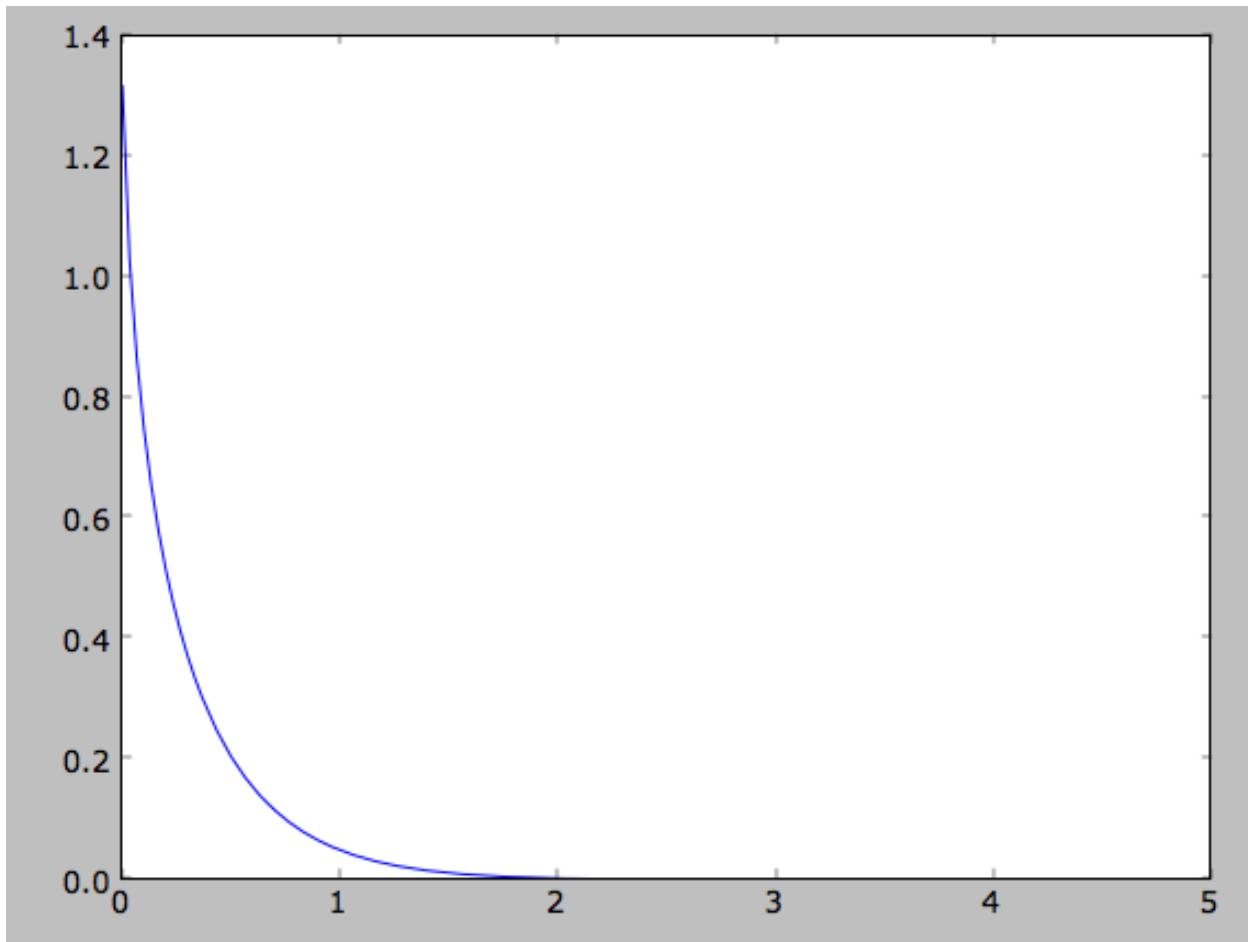
```
>>> dfc.skewvT(1.)
-0.48617143862047763
>>> dfc.kurtosisvT(1.)
0.13338978593181494
>>> dfc.kurtosisvR(1.)
-0.12159407676394096
```

We already saw above that the velocity dispersion at R=1 is not exactly equal to the input velocity dispersion (0.19321086259083936 vs. 0.2). Similarly, the whole surface-density and velocity-dispersion profiles are not quite equal to the exponential input profiles. We can calculate the resulting surface-mass density profile using `surfacemass`, `sigmaR2`, and `sigma2surfacemass`. The latter calculates the product of the velocity dispersion squared and the surface-mass density. E.g.,

```
>>> dfc.surfacemass(1.)
0.050820867101511534
```

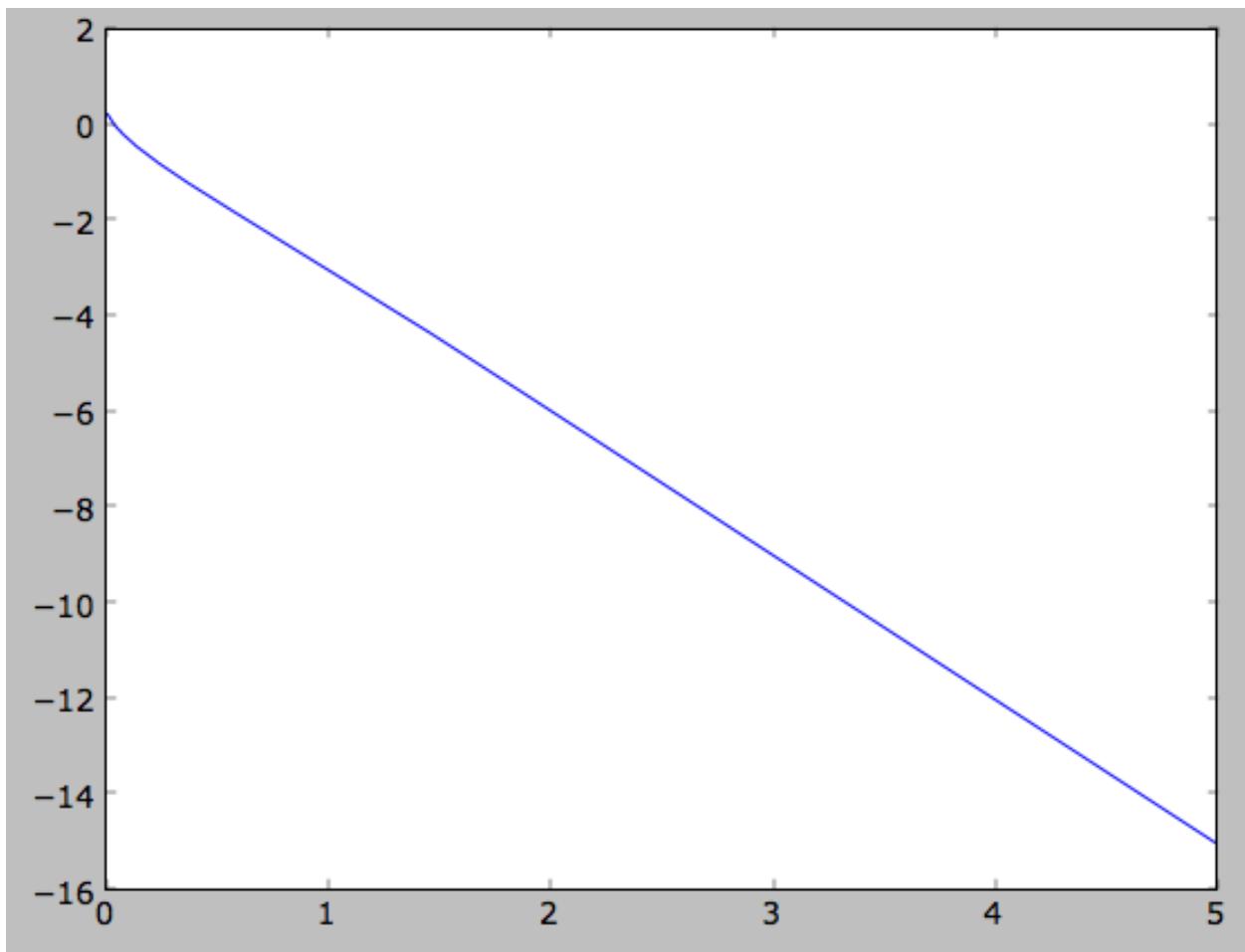
We can plot the surface-mass density as follows

```
>>> Rs= numpy.linspace(0.01,5.,151)
>>> out= [dfc.surfacemass(r) for r in Rs]
>>> plot(Rs, out)
```



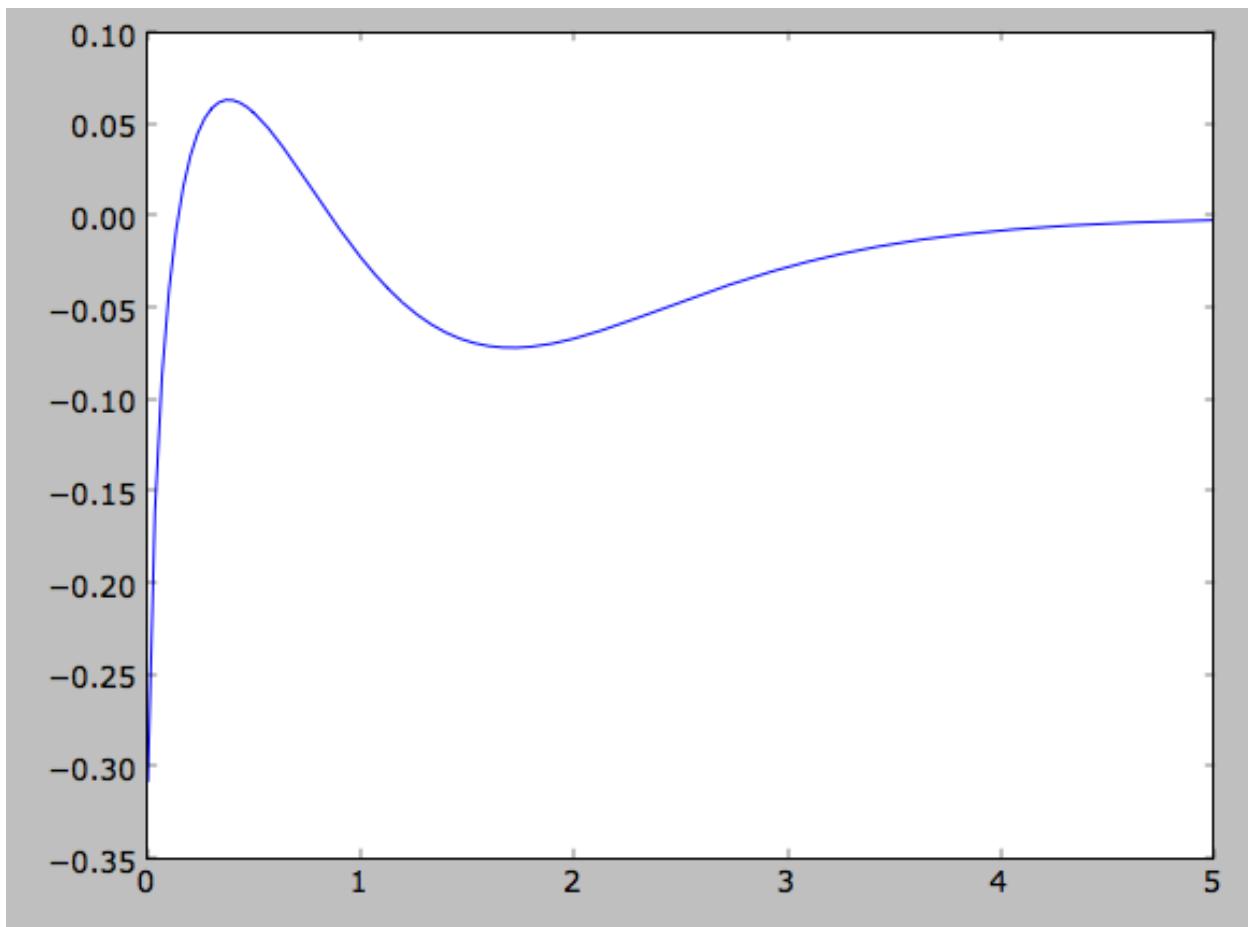
or

```
>>> plot(Rs, numpy.log(out))
```



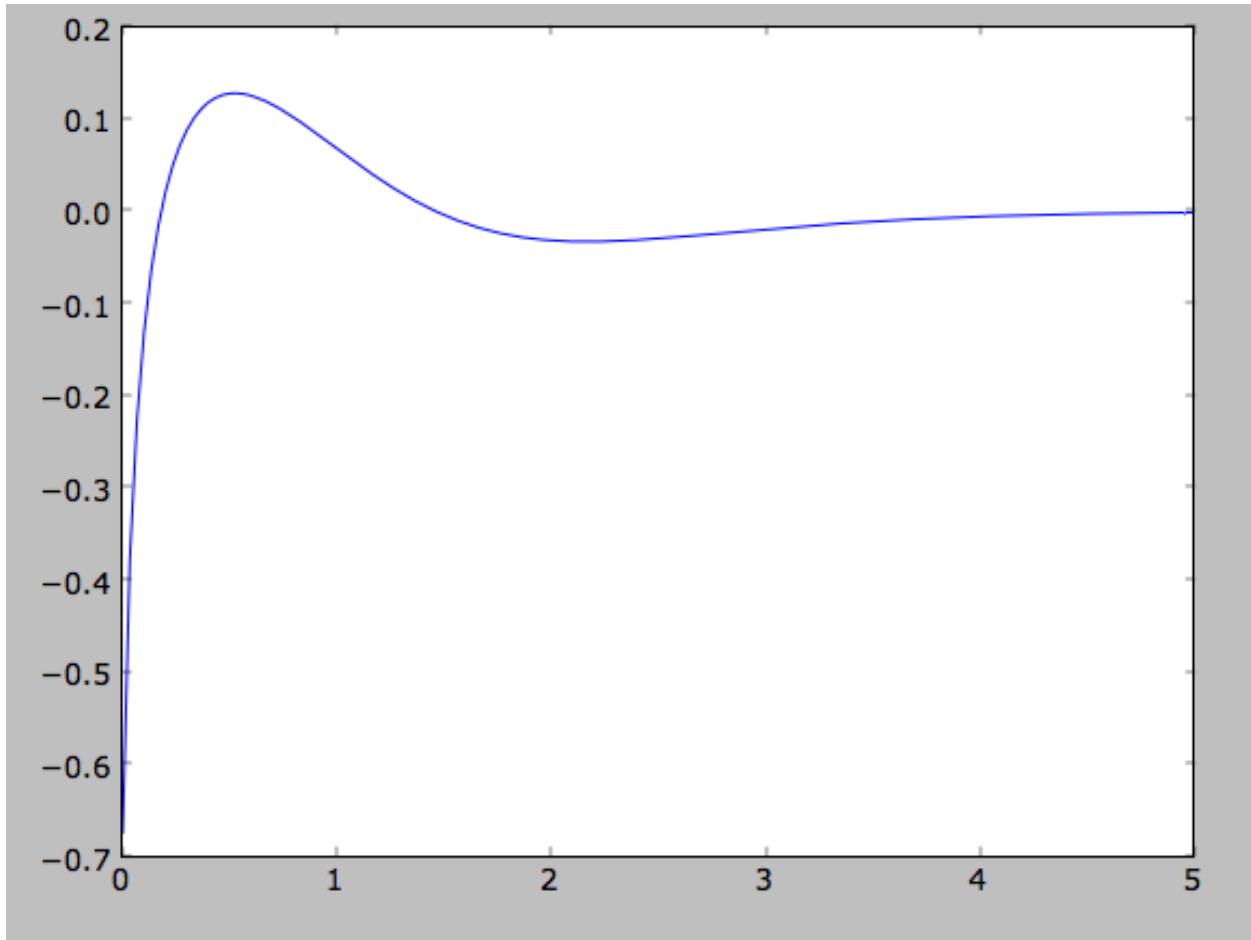
which shows the exponential behavior expected for an exponential disk. We can compare this to the input surface-mass density

```
>>> input_out= [dfc.targetSurfacemass(r) for r in Rs]
>>> plot(Rs, numpy.log(input_out)-numpy.log(out))
```



which shows that there are significant differences between the desired surface-mass density and the actual surface-mass density. We can do the same for the velocity-dispersion profile

```
>>> out= [dfc.sigmaR2(r) for r in Rs]
>>> input_out= [dfc.targetSigma2(r) for r in Rs]
>>> plot(Rs, numpy.log(input_out)-numpy.log(out))
```



That the input surface-density and velocity-dispersion profiles are not the same as the output profiles, means that estimates of DF properties based on these profiles will not be quite correct. Obviously this is the case for the surface-density and velocity-dispersion profiles themselves, which have to be explicitly calculated by integration over the DF rather than by evaluating the input profiles. This also means that estimates of the asymmetric drift based on the input profiles will be wrong. We can calculate the asymmetric drift at  $R=1$  using the asymmetric drift equation derived from the Jeans equation (eq. 4.228 in Binney & Tremaine 2008), using the input surface-density and velocity dispersion profiles

```
>>> dfc.asymmetricdrift(1.)
0.09000000000000024
```

which should be equal to the circular velocity minus the mean rotational velocity

```
>>> 1.-dfc.meanvT(1.)
0.082847230205526756
```

These are not the same in part because of the difference between the input and output surface-density and velocity-dispersion profiles (and because the `asymmetricdrift` method assumes that the ratio of the velocity dispersions squared is two using the epicycle approximation; see above).

### 1.4.3 Using corrected disk distribution functions

As shown above, for a given surface-mass density and velocity dispersion profile, the two-dimensional disk distribution functions only do a poor job of reproducing the desired profiles. We can correct this by calculating a set of *corrections* to the input profiles such that the output profiles more closely resemble the desired profiles (see 1999AJ....118.1201D).

galpy supports the calculation of these corrections, and comes with some pre-calculated corrections (these can be found [here](#)). For example, the following initializes a `dehnendf` with corrections up to 20th order (the default)

```
>>> dfc= dehnendf(beta=0., correct=True)
```

The following figure shows the difference between the actual surface-mass density profile and the desired profile for 1, 2, 3, 4, 5, 10, 15, and 20 iterations

and the same for the velocity-dispersion profile

galpy will automatically save any new corrections that you calculate.

All of the methods for an uncorrected disk DF can be used for the corrected DFs as well. For example, the velocity dispersion is now

```
>>> numpy.sqrt(dfc.sigmaR2(1.))
0.19999985069451526
```

and the mean rotation velocity is

```
>>> dfc.meanvT(1.)
0.90355161181498711
```

and (correct) asymmetric drift

```
>>> 1.-dfc.meanvT(1.)
0.09644838818501289
```

That this still does not agree with the simple `dfc.asymmetricdrift` estimate is because of the latter's using the epicycle approximation for the ratio of the velocity dispersions.

#### 1.4.4 Oort constants and functions

galpy also contains methods to calculate the Oort functions for two-dimensional disk distribution functions. These are known as the *Oort constants* when measured in the solar neighborhood. They are combinations of the mean velocities and derivatives thereof. galpy calculates these by direct integration over the DF and derivatives of the DF. Thus, we can calculate

```
>>> dfc= dehnendf(beta=0.)
>>> dfc.oortA(1.)
0.43190780889218749
>>> dfc.oortB(1.)
-0.48524496090228575
```

The  $K$  and  $C$  Oort constants are zero for axisymmetric DFs

```
>>> dfc.oortC(1.)
0.0
>>> dfc.oortK(1.)
0.0
```

In the epicycle approximation, for a flat rotation curve  $A = -B = 0.5$ . The explicit calculates of  $A$  and  $B$  for warm DFs quantify how good (or bad) this approximation is

```
>>> dfc.oortA(1.)+dfc.oortB(1.)
-0.053337152010098254
```

For the cold DF from above the approximation is much better

```
>>> dfccold= dehnendif(beta=0.,profileParams=(1./3.,1.,0.02))
>>> dfccold.oortA(1.), dfccold.oortB(1.)
(0.49917556666144003, -0.49992824742490816)
```

### 1.4.5 Sampling data from the DF

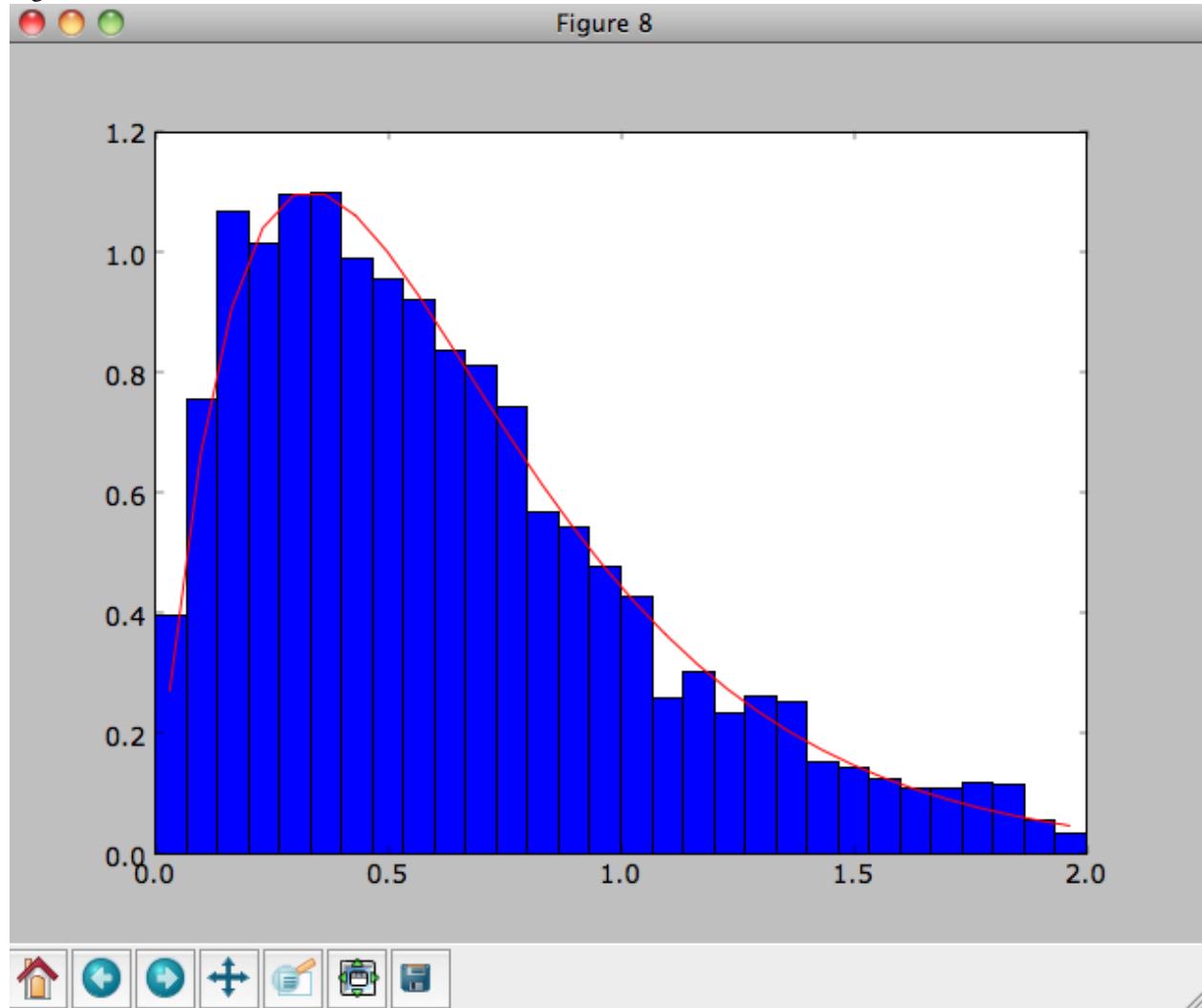
We can sample from the disk distribution functions using `sample`. `sample` can return either an energy-angular-momentum pair, or a full orbit initialization. We can sample 4000 orbits for example as (could take two minutes)

```
>>> o= dfc.sample(n=4000,returnOrbit=True,nphi=1)
```

We can then plot the histogram of the sampled radii and compare it to the input surface-mass density profile

```
>>> Rs= [e.R() for e in o]
>>> hists, bins, edges= hist(Rs,range=[0,2],normed=True,bins=30)
>>> xs= numpy.array([(bins[ii+1]+bins[ii])/2. for ii in range(len(bins)-1)])
>>> plot(xs, xs*exp(-xs*3.)*9.,'r-')
```

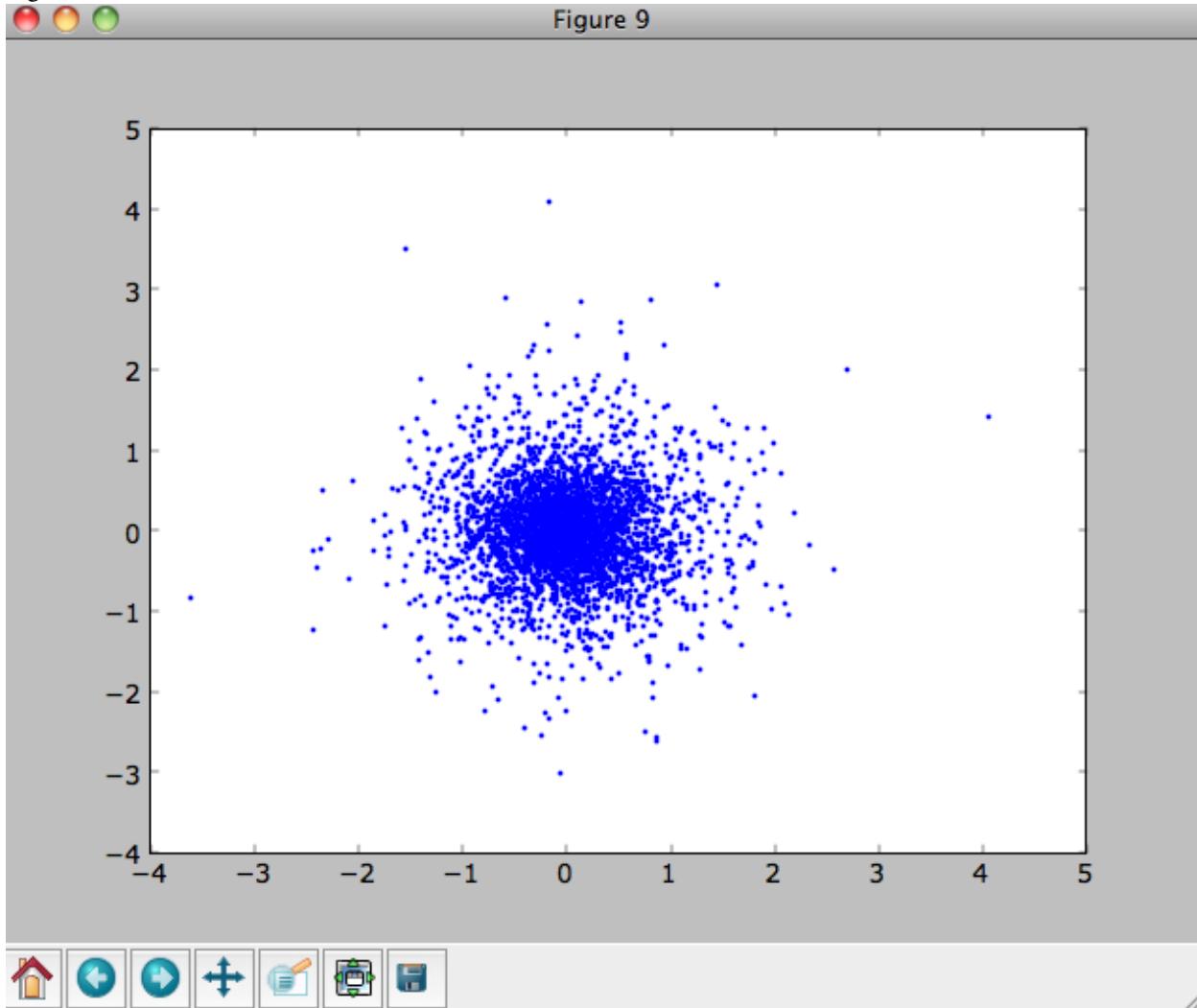
E.g.,



We can also plot the spatial distribution of the sampled disk

```
>>> xs= [e.x() for e in o]
>>> ys= [e.y() for e in o]
>>> figure()
>>> plot(xs,ys,'.')
```

E.g.,

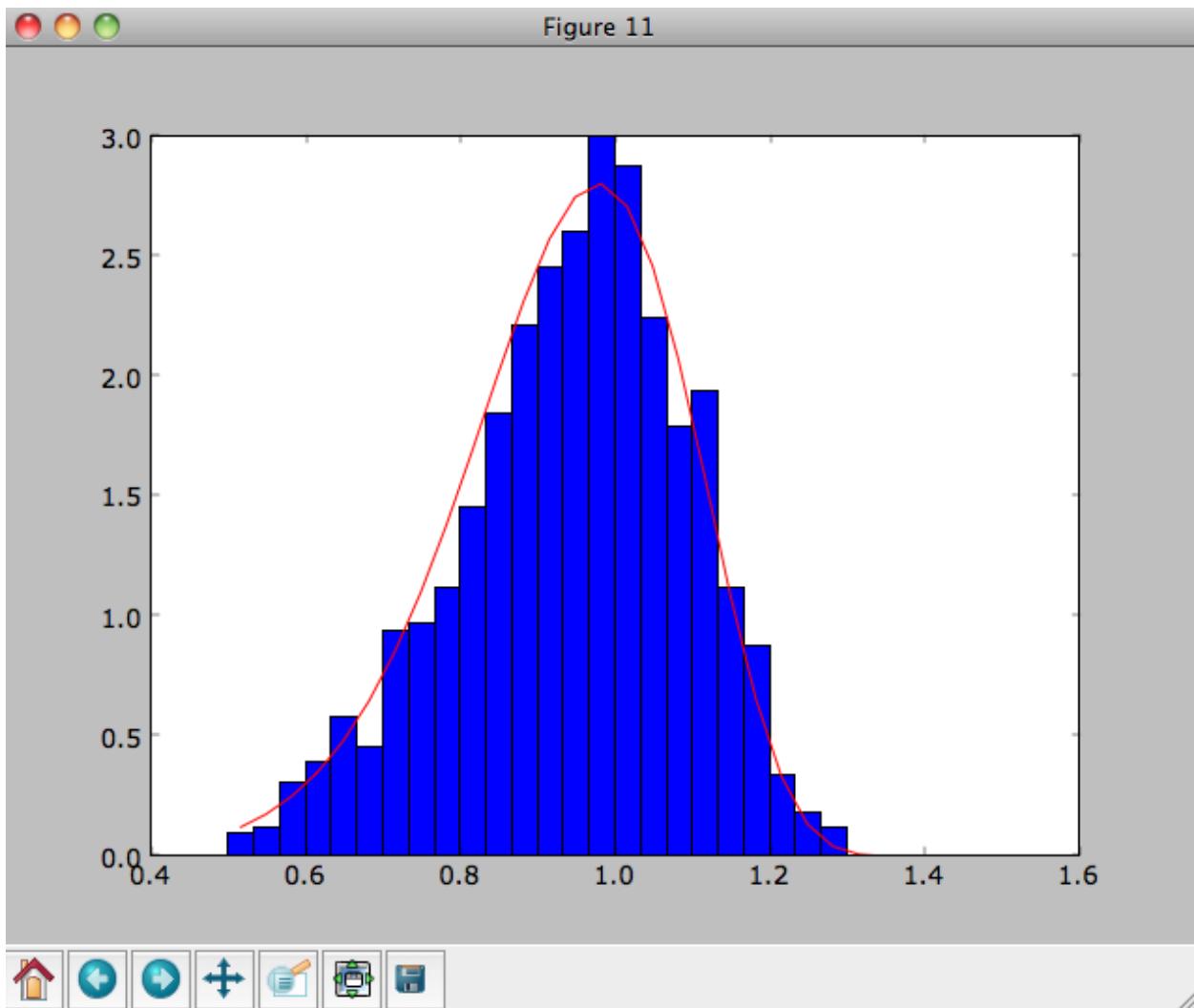


We can also sample points in a specific radial range (might take a few minutes)

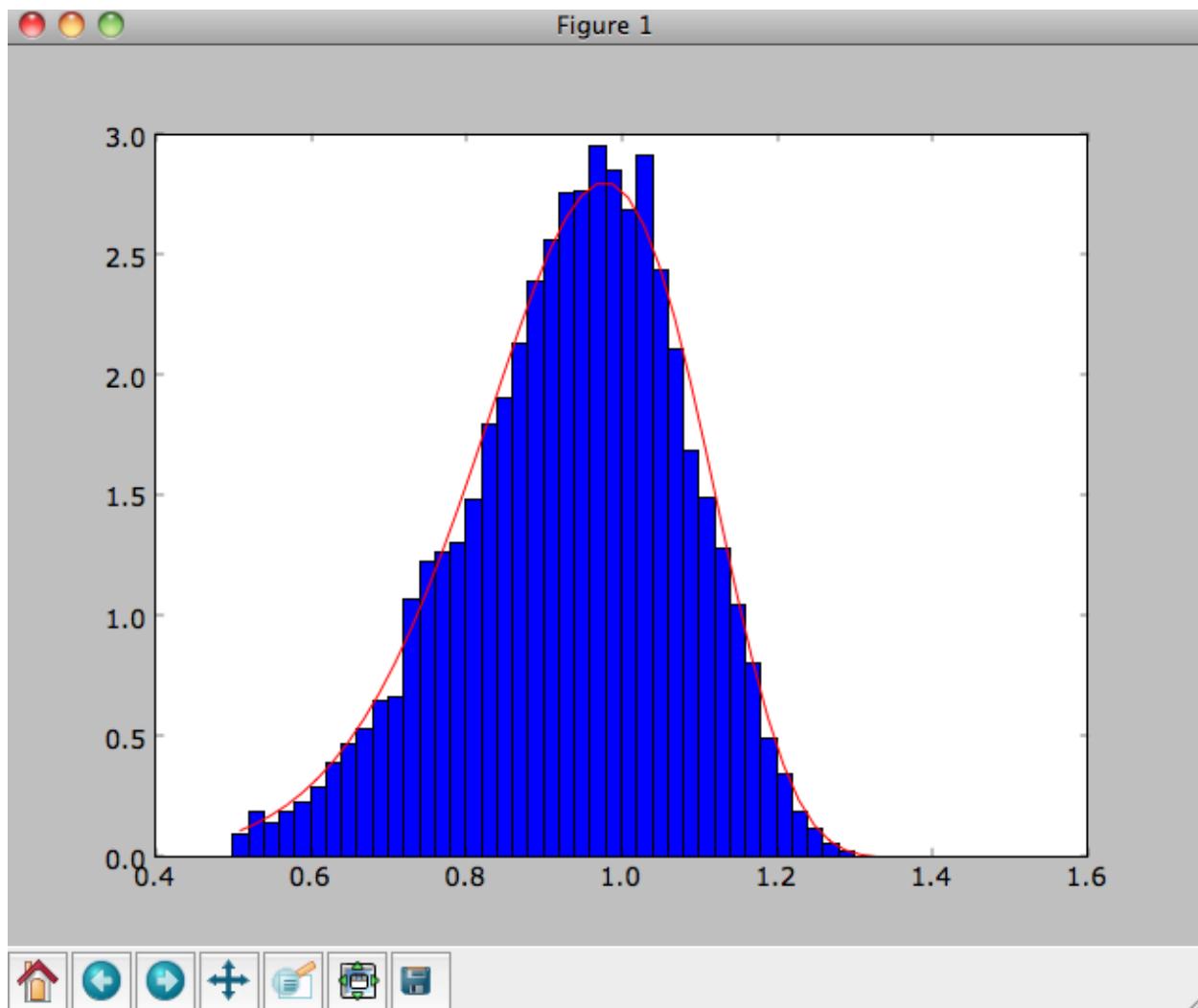
```
>>> o= dfc.sample(n=1000,returnOrbit=True,nphi=1,rrange=[0.8,1.2])
```

and we can plot the distribution of tangential velocities

```
>>> vTs= [e.vxvv[2] for e in o]
>>> hists, bins, edges= hist(vTs,range=[.5,1.5],normed=True,bins=30)
>>> xs= numpy.array([(bins[ii+1]+bins[ii])/2. for ii in range(len(bins)-1)])
>>> dfro= [dfc(Orbit([1.,0.,x]))/9./numpy.exp(-3.) for x in xs]
>>> plot(xs,dfro,'r-')
```

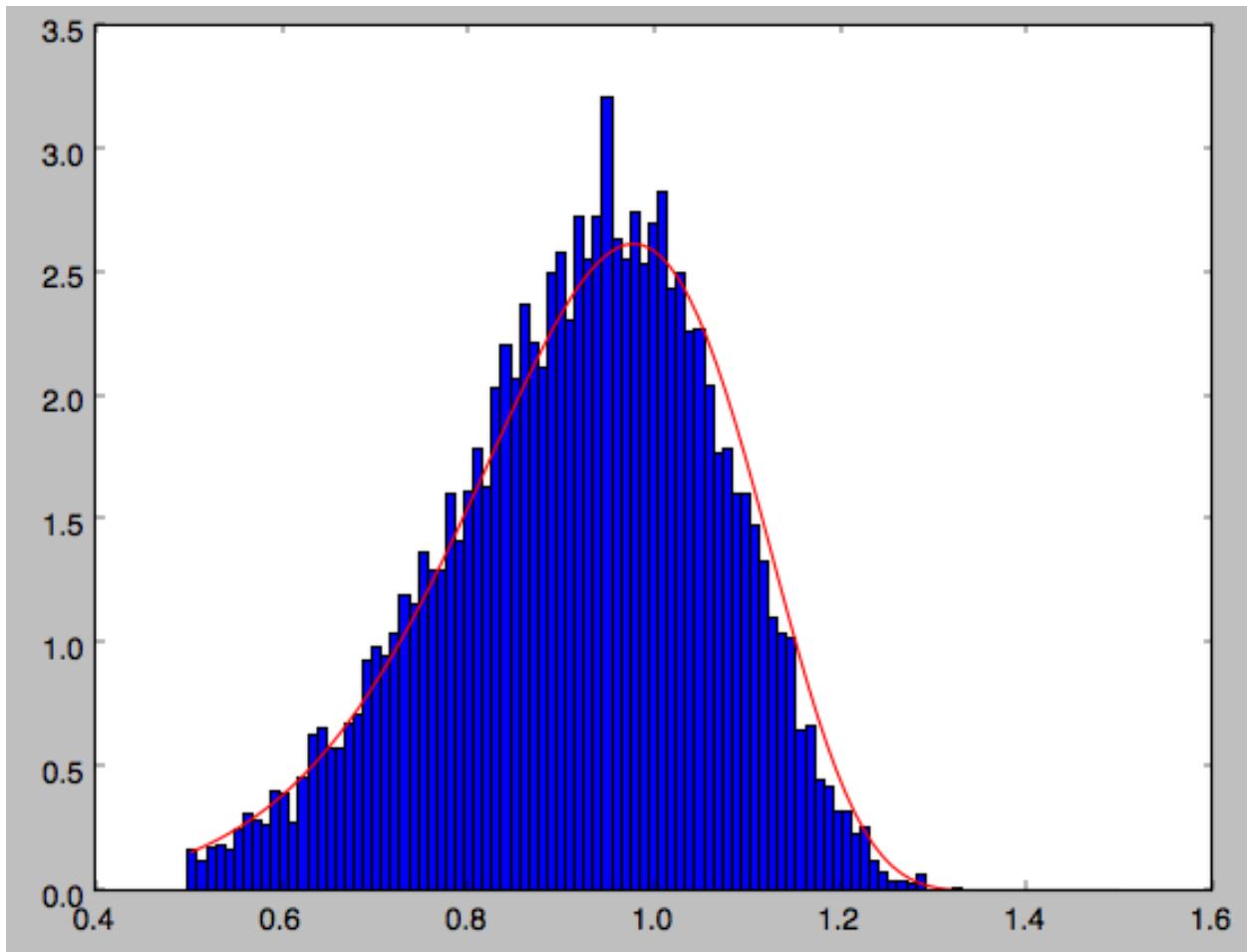


The agreement between the sampled distribution and the theoretical curve is not as good because the sampled distribution has a finite radial range. If we sample 10,000 points in `rrange=[0.95, 1.05]` the agreement is better (this takes a long time):



We can also directly sample velocities at a given radius rather than in a range of radii. Doing this for a correct DF gives

```
>>> dfc= dehnendf(beta=0.,correct=True)
>>> vrvt= dfc.sampleVRVT(1.)
>>> hists, bins, edges= hist(vrvt[:,1],range=[.5,1.5],normed=True,bins=101)
>>> xs= numpy.array([(bins[ii+1]+bins[ii])/2. for ii in range(len(bins)-1)])
>>> dfro= [dfc(Orbit([1.,0.,x])) for x in xs]
>>> plot(xs,dfro/numpy.sum(dfro)/(xs[1]-xs[0]),'r-')
```



galpy further has support for sampling along a given line of sight in the disk, which is useful for interpreting surveys consisting of a finite number of pointings. For example, we can sample distances along a given line of sight

```
>>> ds= dfc.sampledSurfacemassLOS(30./180.*numpy.pi,n=10000)
```

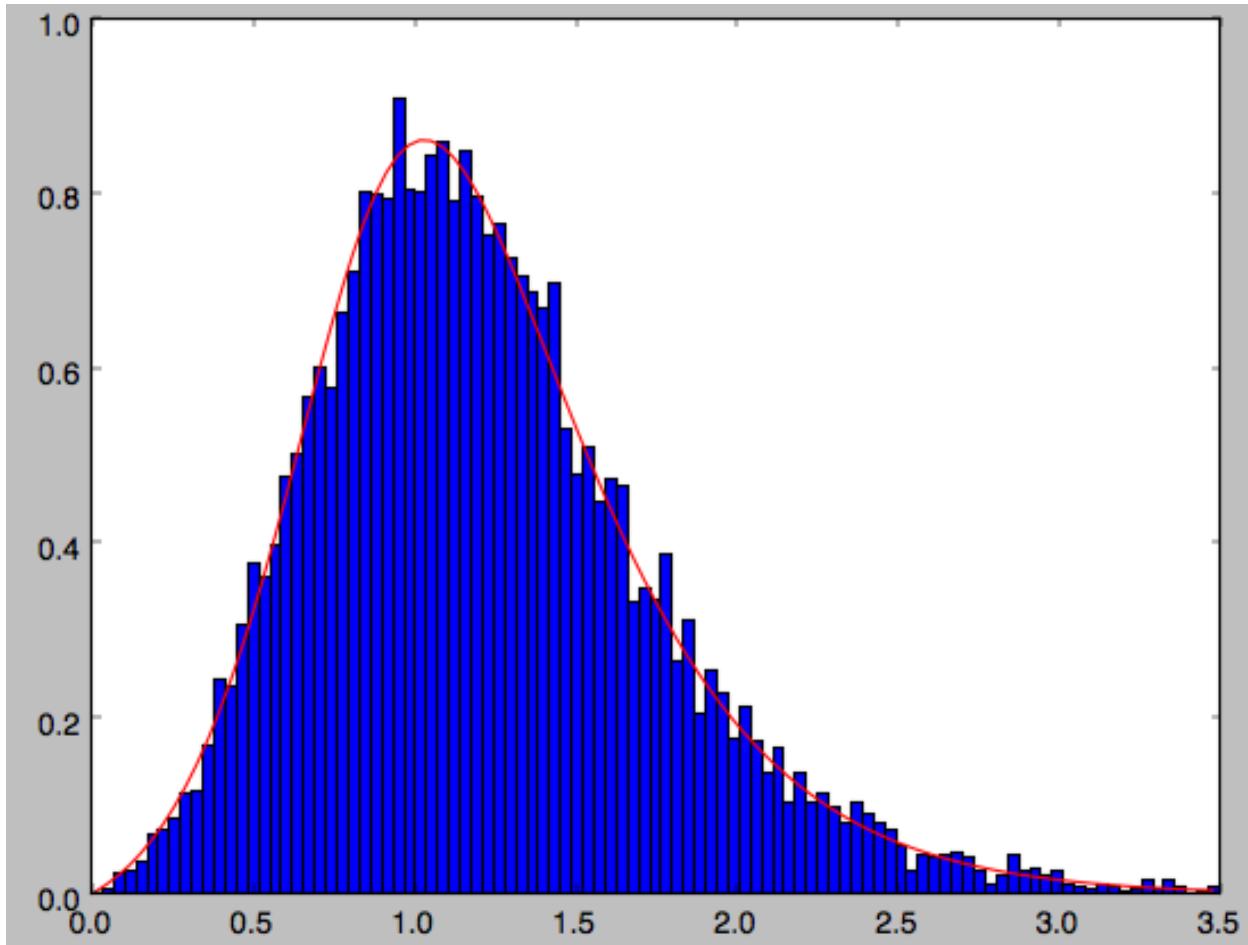
which is very fast. We can histogram these

```
>>> hists, bins, edges= hist(ds,range=[0., 3.5],normed=True,bins=101)
```

and compare it to the predicted distribution, which we can calculate as

```
>>> xs= numpy.array([(bins[ii+1]+bins[ii])/2. for ii in range(len(bins)-1)])
>>> fd= numpy.array([dfc.surfacemassLOS(d,30.) for d in xs])
>>> plot(xs,fd/numpy.sum(fd)/(xs[1]-xs[0]),'r-')
```

which shows very good agreement with the sampled distances



galpy can further sample full 4D phase-space coordinates along a given line of sight through `dfc.sampleLOS`.

#### 1.4.6 Example: The Hercules stream in the Solar neighborhood as a result of the Galactic bar

We can combine the orbit integration capabilities of galpy with the provided distribution functions and see the effect of the Galactic bar on stellar velocities. By backward integrating orbits starting at the Solar position in a potential that includes the Galactic bar we can evaluate what the velocity distribution is that we should see today if the Galactic bar stirred up a steady-state disk. For this we initialize a flat rotation curve potential and Dehnen's bar potential

```
>>> from galpy.potential import LogarithmicHaloPotential, DehnenBarPotential
>>> lp= LogarithmicHaloPotential(normalize=1.)
>>> dp= DehnenBarPotential()
```

The Dehnen bar potential is initialized to start bar formation four bar periods before the present day and to have completely formed the bar two bar periods ago. We can integrate back to the time before bar-formation:

```
>>> ts= numpy.linspace(0,dp.tform(),1000)
```

where `dp.tform()` is the time of bar-formation (in the usual time-coordinates).

We initialize orbits on a grid in velocity space and integrate them

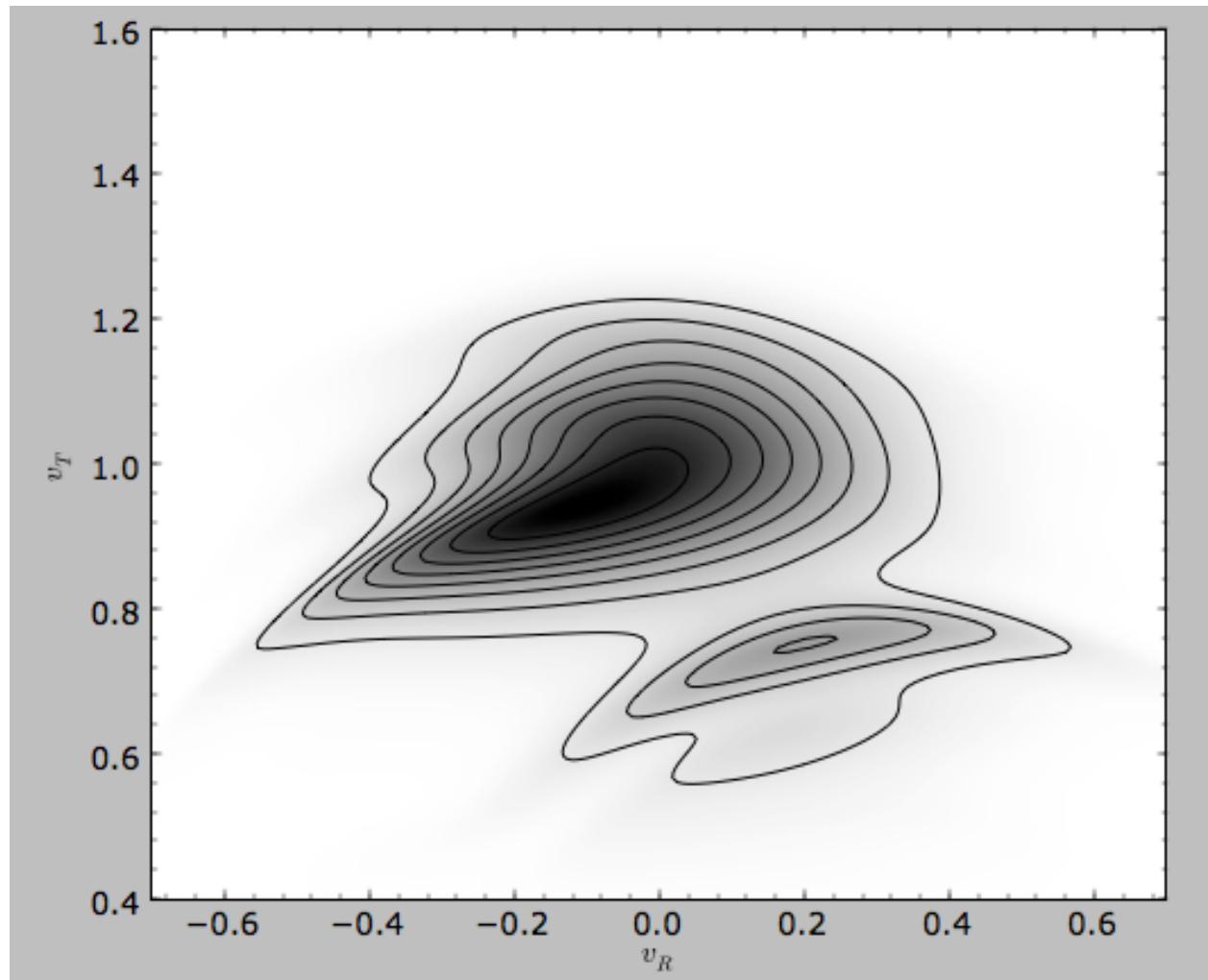
```
>>> ins=[[Orbit([1.,-0.7+1.4/100*jj,1.-0.6+1.2/100*ii,0.]) for jj in range(101)] for ii in range(101)]
>>> int=[[o.integrate(ts,[lp,dp]) for o in j] for j in ins]
```

We can then evaluate the weight of these orbits by assuming that the disk was in a steady-state before bar-formation with a Dehnen distribution function. We evaluate the Dehnen distribution function at `dp.tform()` for each of the orbits

```
>>> dfc= dehnendf(beta=0.,correct=True)
>>> out= [[dfc(o(dp.tform()))] for o in j] for j in ins]
>>> out= numpy.array(out)
```

This gives

```
>>> from galpy.util.bovy_plot import bovy_dens2d
>>> bovy_dens2d(out,origin='lower',cmap='gist_yarg',contours=True,xrange=[-0.7,0.7],yrange=[0.4,1.6])
```



For more information see [2000AJ....119..800D](#) and [2010ApJ...725.1676B](#). Note that the x-axis in the Figure above is defined as minus the x-axis in these papers.

## 1.5 A closer look at orbit integration

### 1.5.1 Orbit initialization

Orbits can be initialized in various coordinate frames. The simplest initialization gives the initial conditions directly in the Galactocentric cylindrical coordinate frame (or in the rectangular coordinate frame in one dimension). `Orbit()`

automatically figures out the dimensionality of the space from the initial conditions in this case. In three dimensions initial conditions are given either as `vxvv=[R, vR, vT, z, vz, phi]` or one can choose not to specify the azimuth of the orbit and initialize with `vxvv=[R, vR, vT, z, vz]`. Since potentials in galpy are easily initialized to have a circular velocity of one at a radius equal to one, initial coordinates are best given as a fraction of the radius at which one specifies the circular velocity, and initial velocities are best expressed as fractions of this circular velocity. For example,

```
>>> o= Orbit(vxvv=[1., 0.1, 1.1, 0., 0.1, 0.])
```

initializes a fully three-dimensional orbit, while

```
>>> o= Orbit(vxvv=[1., 0.1, 1.1, 0., 0.1])
```

initializes an orbit in which the azimuth is not tracked, as might be useful for axisymmetric potentials.

In two dimensions, we can similarly specify fully two-dimensional orbits `vxvv=[R, vR, vT, phi]` or choose not to track the azimuth and initialize as `vxvv=[R, vR, vT]`.

In one dimension we simply initialize as `vxvv=[x, vx]`.

For orbit integration and characterization of observed stars or clusters, initial conditions can also be specified directly as observed quantities when `radec=True` is set. In this case a full three-dimensional orbit is initialized as `vxvv=[RA, Dec, distance, pmRA, pmDec, Vlos]` where RA and Dec are expressed in degrees, the distance is expressed in kpc, proper motions are expressed in mas/yr (`pmra = pmra' * cos[Dec]`), and the line-of-sight velocity is given in km/s. These observed coordinates are translated to the Galactocentric cylindrical coordinate frame by assuming a Solar motion that can be specified as either `solarmotion=hogg` (default; 2005ApJ...629..268H), `solarmotion=dehnen` (1998MNRAS.298..387D) or `solarmotion=shoenrich` (2010MNRAS.403.1829S). A circular velocity can be specified as `vo=235` in km/s and a value for the distance between the Galactic center and the Sun can be given as `ro=8.5` in kpc. While the inputs are given in physical units, the orbit is initialized assuming a circular velocity of one at the distance of the Sun.

When `radec=True` is set, velocities can also be specified in Galactic coordinates if `UVW=True` is set. The input is then `vxvv=[RA, Dec, distance, U, V, W]`, where the velocities are expressed in km/s. U is, as usual, defined as `-vR` (minus `vR`).

## 1.5.2 Orbit integration

After an orbit is initialized, we can integrate it for a set of times `ts`, given as a numpy array. For example, in a simple logarithmic potential we can do the following

```
>>> from galpy.potential import LogarithmicHaloPotential
>>> lp= LogarithmicHaloPotential(normalize=1.)
>>> o= Orbit(vxvv=[1., 0.1, 1.1, 0., 0.1, 0.])
>>> import numpy
>>> ts= numpy.linspace(0, 100, 10000)
>>> o.integrate(ts, lp)
```

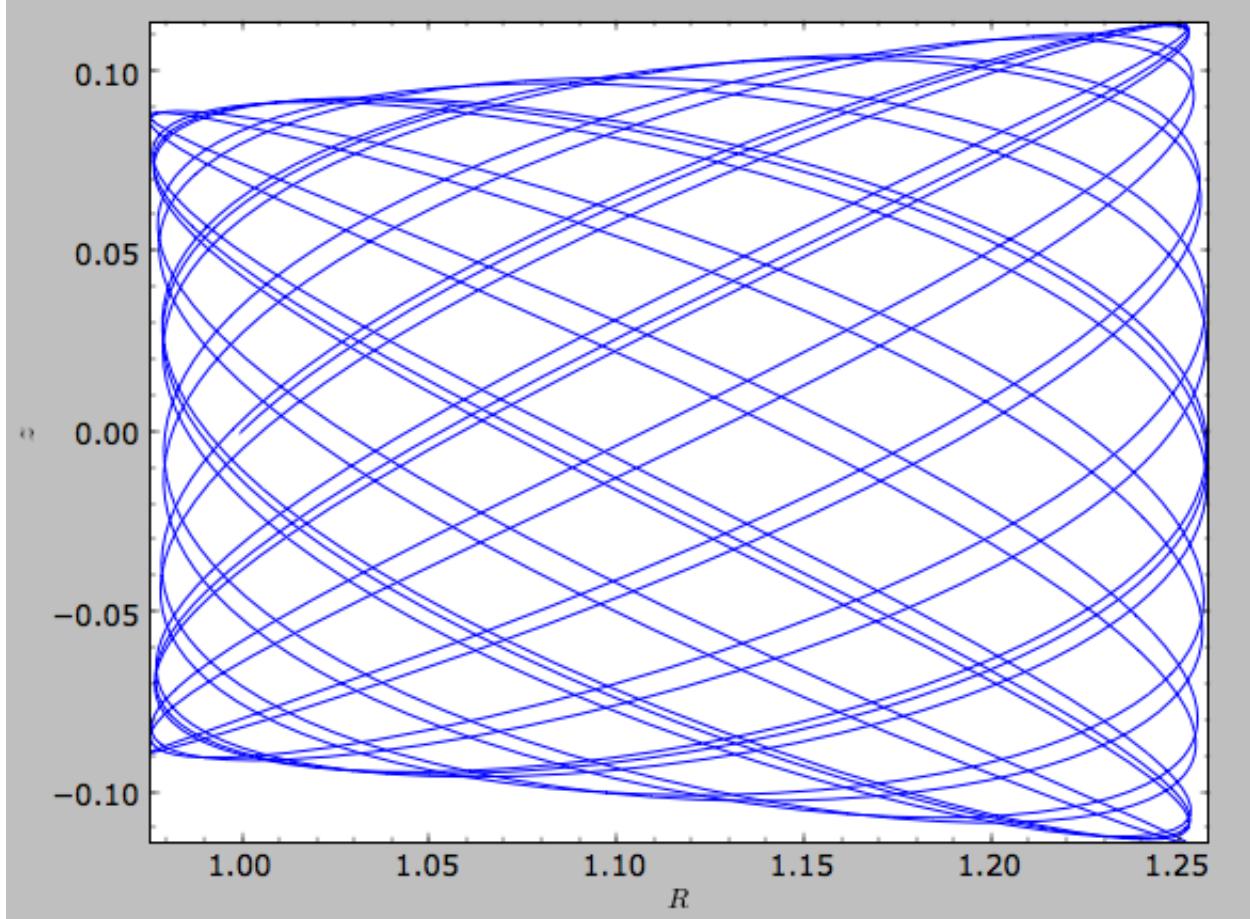
to integrate the orbit from `t=0` to `t=100`, saving the orbit at 10000 instances.

## 1.5.3 Displaying the orbit

After integrating the orbit, it can be displayed by using the `plot()` function. The quantities that are plotted when `plot()` is called depend on the dimensionality of the orbit: in 3D the (R,z) projection of the orbit is shown; in 2D either (X,Y) is plotted if the azimuth is tracked and (R,vR) is shown otherwise; in 1D (x,vx) is shown. E.g., for the example given above,

```
>>> o.plot()
```

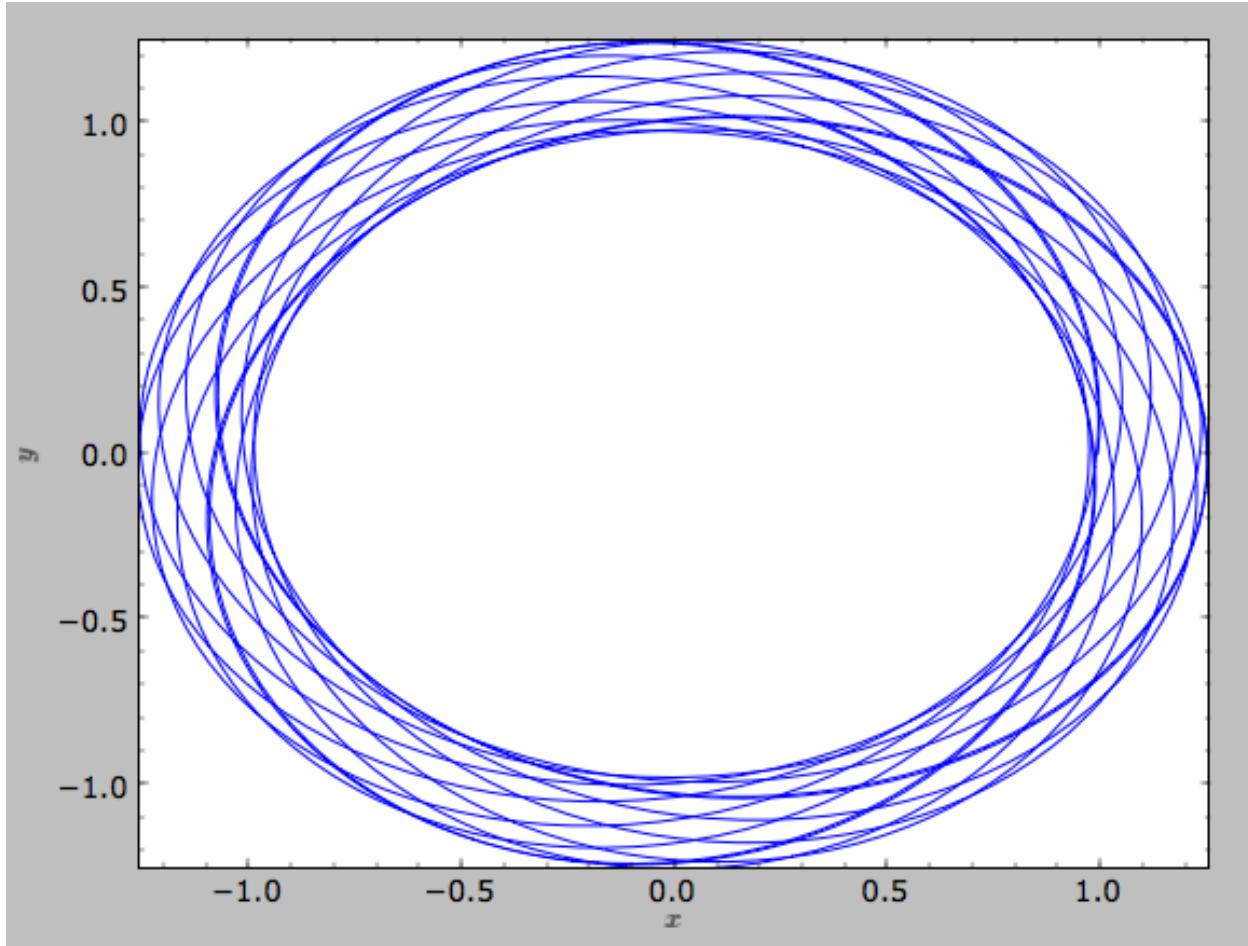
gives



Other projections of the orbit can be displayed by specifying the quantities to plot. E.g.,

```
>>> o.plot(d1='x', d2='y')
```

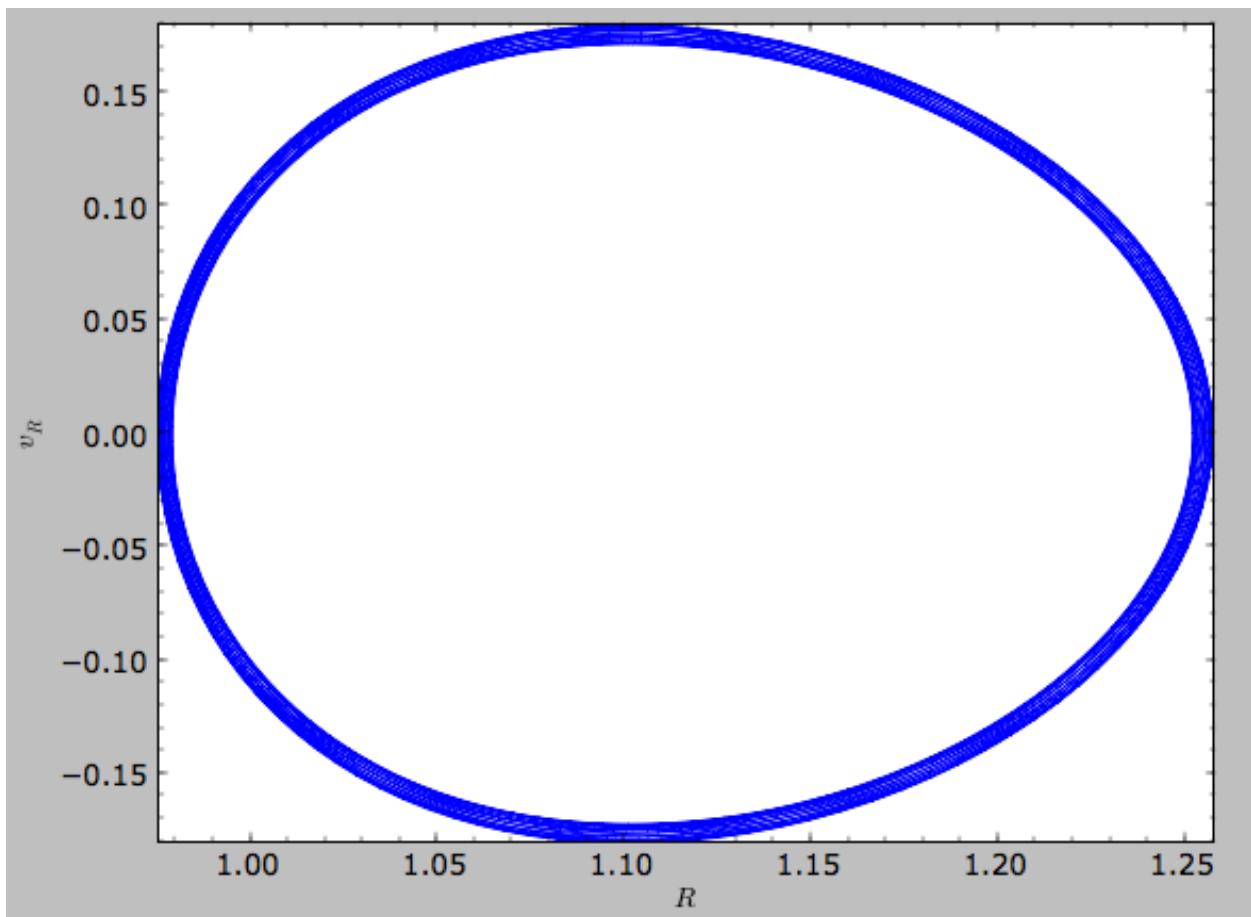
gives the projection onto the plane of the orbit:



while

```
>>> o.plot(d1='R', d2='vR')
```

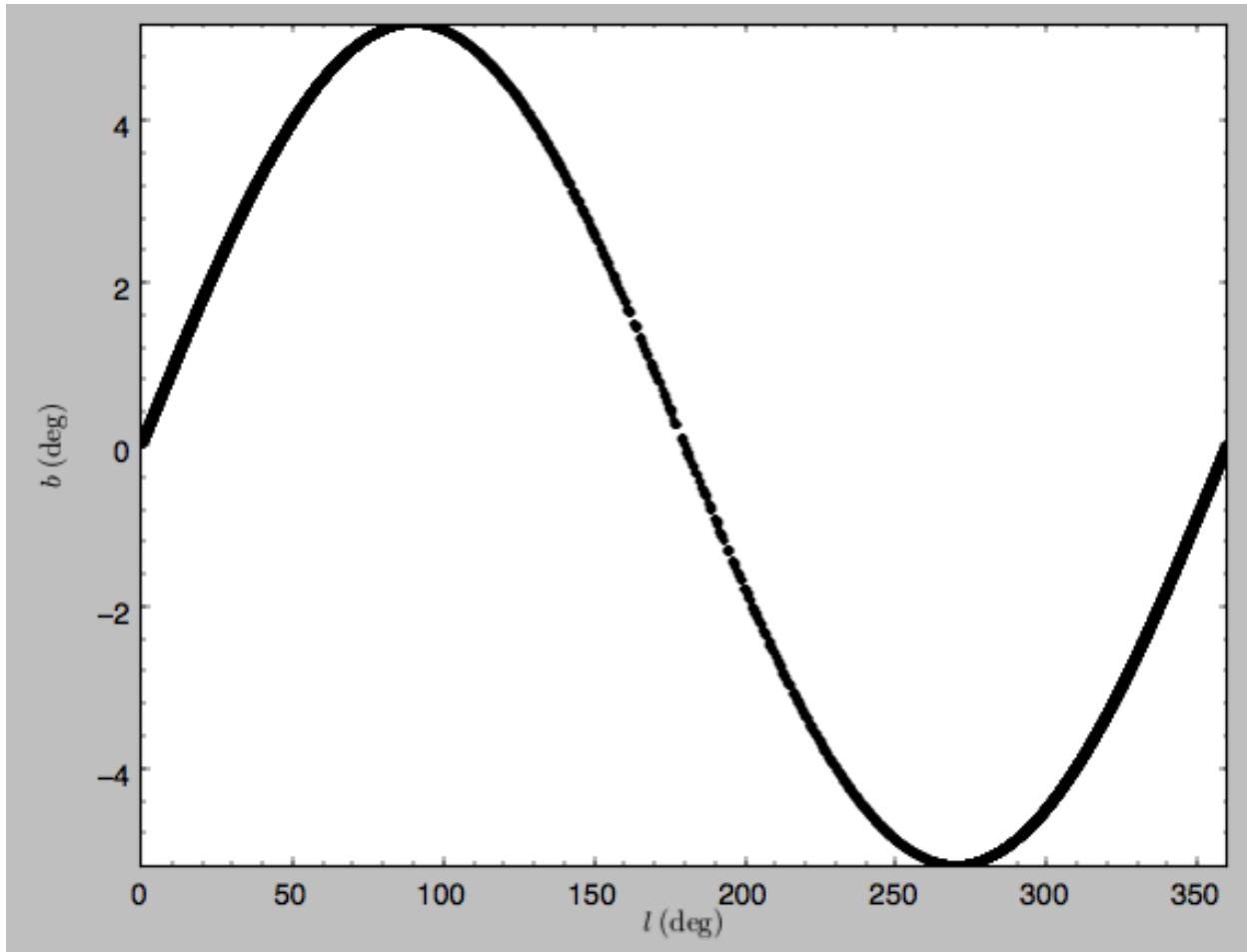
gives the projection onto (R,vR):



We can also plot the orbit in other coordinate systems such as Galactic longitude and latitude

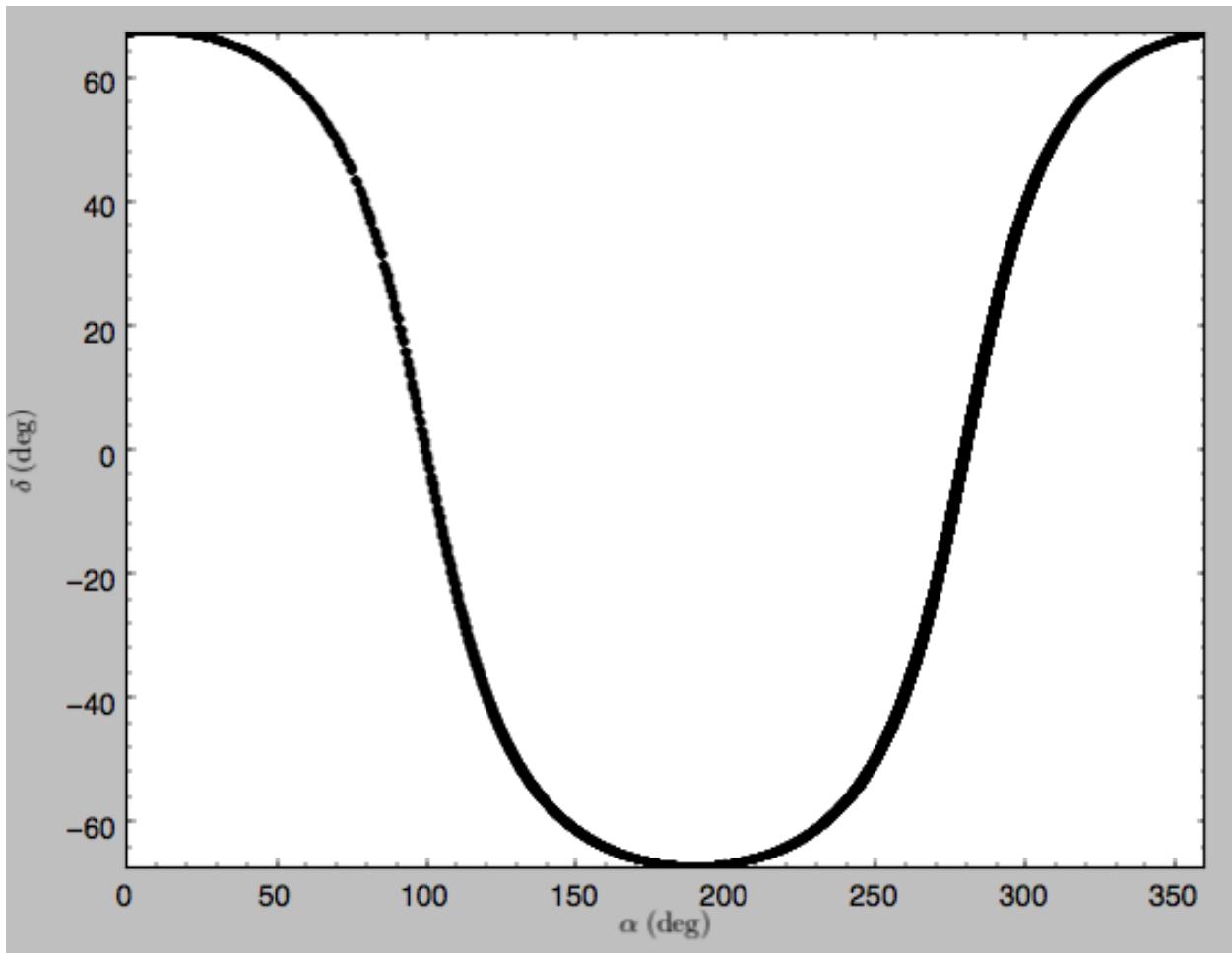
```
>>> o.plot('k.', d1='ll', d2='bb')
```

which shows



or RA and Dec

```
>>> o.plot('k.', d1='ra', d2='dec')
```



See the documentation of the `o.plot` function and the `o.ra()`, `o.ll()`, etc. functions on how to provide the necessary parameters for the coordinate transformations.

#### 1.5.4 Orbit characterization

The properties of the orbit can also be found using galpy. For example, we can calculate the peri- and apocenter radii of an orbit, its eccentricity, and the maximal height above the plane of the orbit

```
>>> o.rap(), o.rperi(), o.e(), o.zmax()
(1.2581455175173673, 0.97981663263371377, 0.12436710999105324, 0.11388132751079502)
```

We can also calculate the energy of the orbit, either in the potential that the orbit was integrated in, or in another potential:

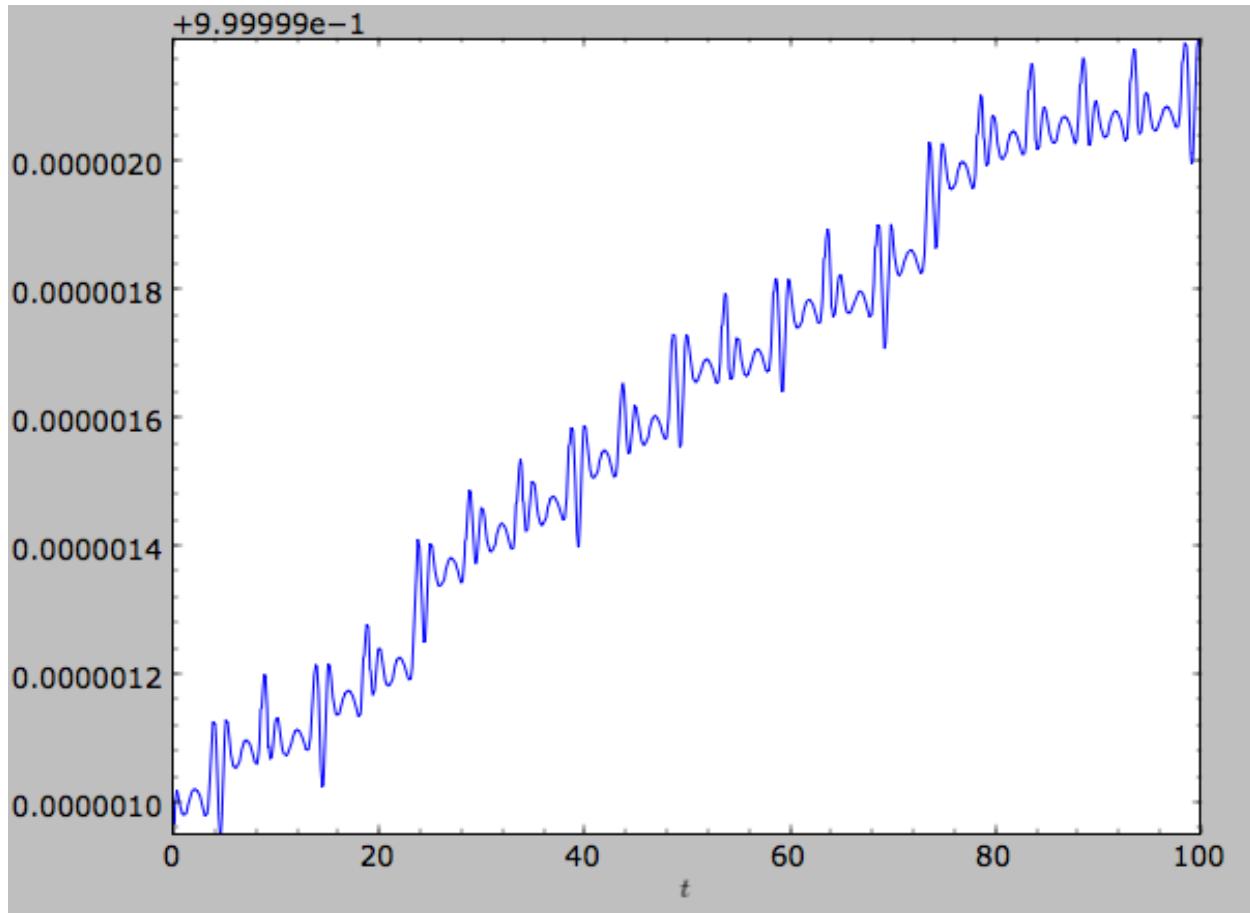
```
>>> o.E(), o.E(pot=mp)
(0.6150000000000001, -0.67390625000000015)
```

where `mp` is the Miyamoto-Nagai potential of *Introduction: Rotation curves*.

We can also show the energy as a function of time (to check energy conservation)

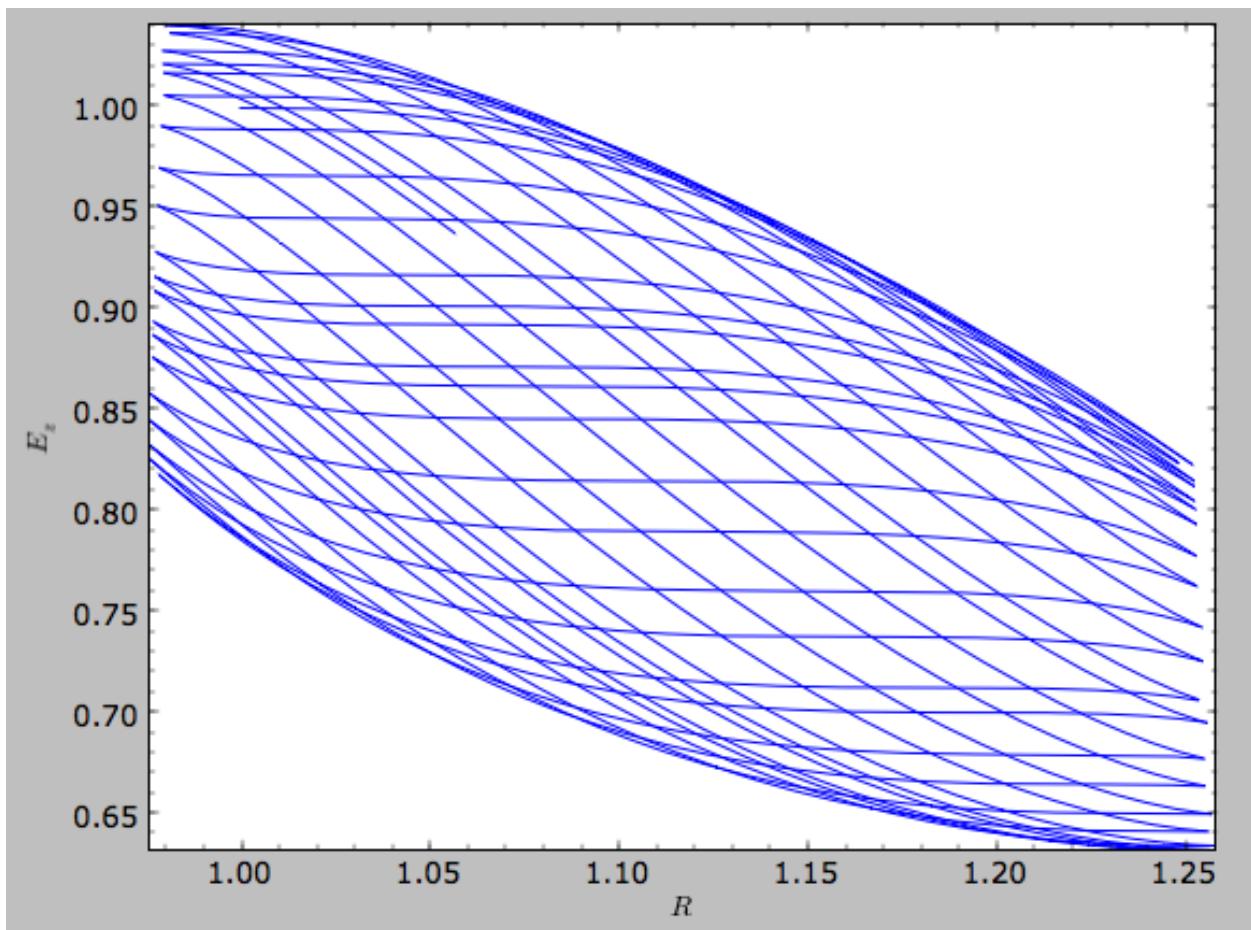
```
>>> o.plotE()
```

gives



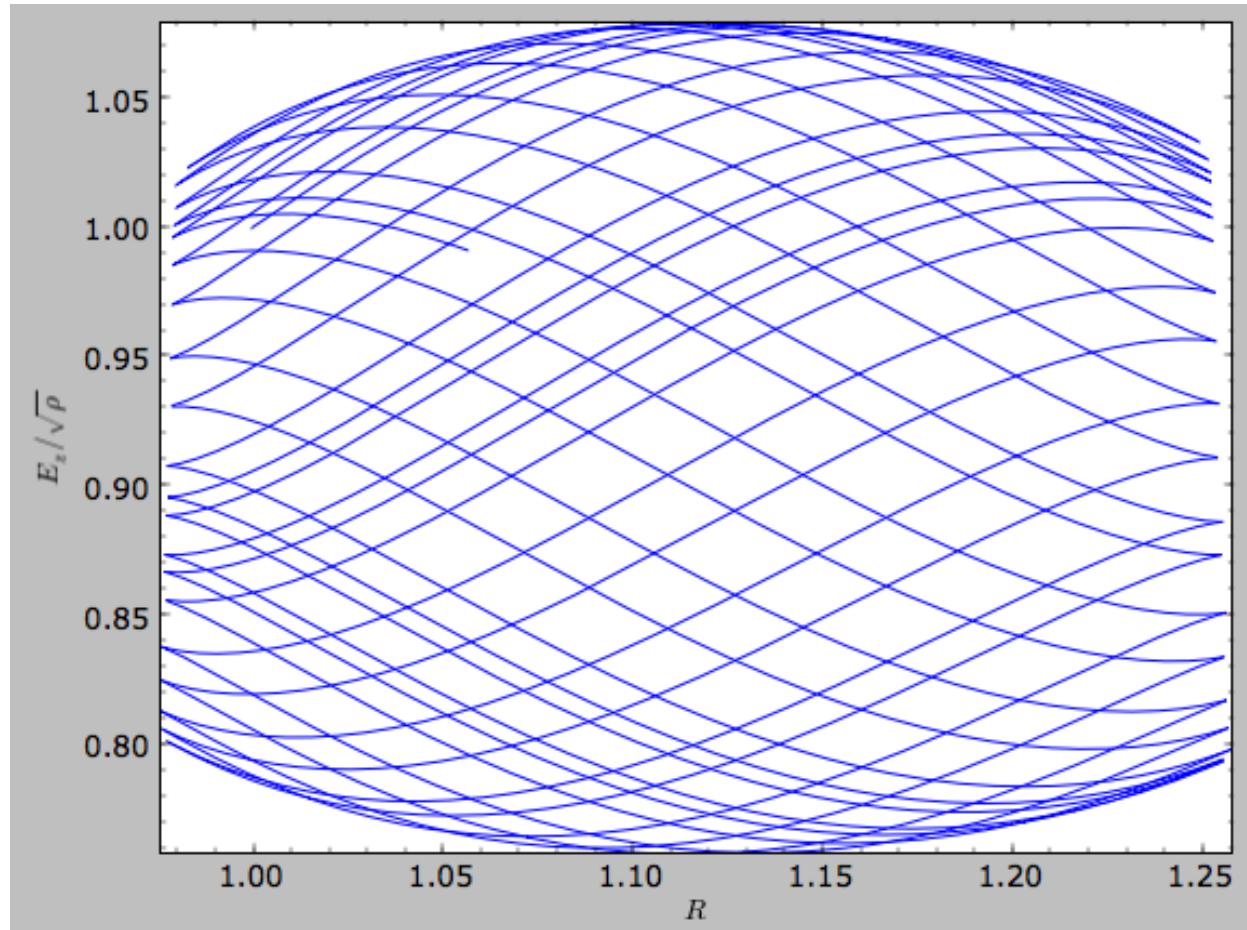
We can specify another quantity to plot the energy against by specifying `d1=`. We can also show the vertical energy, for example, as a function of  $R$

```
>>> o.plotEz(d1='R')
```



Often, a better approximation to an integral of the motion is given by  $E_z/\sqrt{\text{density}[R]}$ . We refer to this quantity as  $E_{zJz}$  and we can plot its behavior

```
>>> o.plotEzJz(d1='R')
```



### 1.5.5 Accessing the raw orbit

The value of `R`, `vR`, `vT`, `z`, `vz`, `x`, `vx`, `y`, `vy`, `phi`, and `vphi` at any time can be obtained by calling the corresponding function with as argument the time (the same holds for other coordinates `ra`, `dec`, `pmra`, `pmdec`, `vra`, `vdec`, `ll`, `bb`, `pml1`, `pmbb`, `vll`, `vbb`, `vlos`, `dist`, `helioX`, `helioY`, `helioZ`, `U`, `V`, and `W`). If no time is given the initial condition is returned, and if a time is requested at which the orbit was not saved spline interpolation is used to return the value. Examples include

```
>>> o.R(1.)
1.1545076874679474
>>> o.phi(99.)
88.105603035901169
>>> o.ra(2.,obs=[8.,0.,0.],ro=8.)
array([ 285.76403985])
>>> o.helioX(5.)
array([ 1.24888927])
>>> o.pml1(10.,obs=[8.,0.,0.,0.,245.,0.],ro=8.,vo=230.)
array([-6.45263888])
```

We can also initialize an `Orbit` instance using the phase-space position of another `Orbit` instance evaluated at time `t`. For example,

```
>>> newOrbit= o(10.)
```

will initialize a new `Orbit` instance with as initial condition the phase-space position of orbit `o` at `time=10..`

The whole orbit can also be obtained using the function `getOrbit`

```
>>> o.getOrbit()
```

which returns a matrix of phase-space points with dimensions [ntimes,ndim].

### 1.5.6 Fast orbit integration

The standard orbit integration is done purely in python using standard scipy integrators. When fast orbit integration is needed for batch integration of a large number of orbits, a set of orbit integration routines are written in C that can be accessed for most potentials, as long as they have C implementations, which can be checked by using the attribute `hasC`

```
>>> mp= MiyamotoNagaiPotential(a=0.5,b=0.0375,amp=1.,normalize=1.)
>>> mp.hasC
True
```

Fast C integrators can be accessed through the `method=` keyword of the `orbit.integrate` method. Currently available integrators are

- `rk4_c`
- `rk6_c`
- `dopr54_c`

which are Runge-Kutta and Dormand-Prince methods. There are also a number of symplectic integrators available

- `leapfrog_c`
- `symplec4_c`
- `symplec6_c`

The higher order symplectic integrators are described in Yoshida (1993).

For most applications I recommend `dopr54_c`. For example, compare

```
>>> o= Orbit(vxvv=[1.,0.1,1.1,0.,0.1])
>>> timeit(o.integrate(ts,mp))
1 loops, best of 3: 553 ms per loop
>>> timeit(o.integrate(ts,mp,method='dopr54_c'))
galpyWarning: Using C implementation to integrate orbits
10 loops, best of 3: 25.6 ms per loop
```

As this example shows, galpy will issue a warning that C is being used. Speed-ups by a factor of 20 are typical.

### 1.5.7 Example: The eccentricity distribution of the Milky Way's thick disk

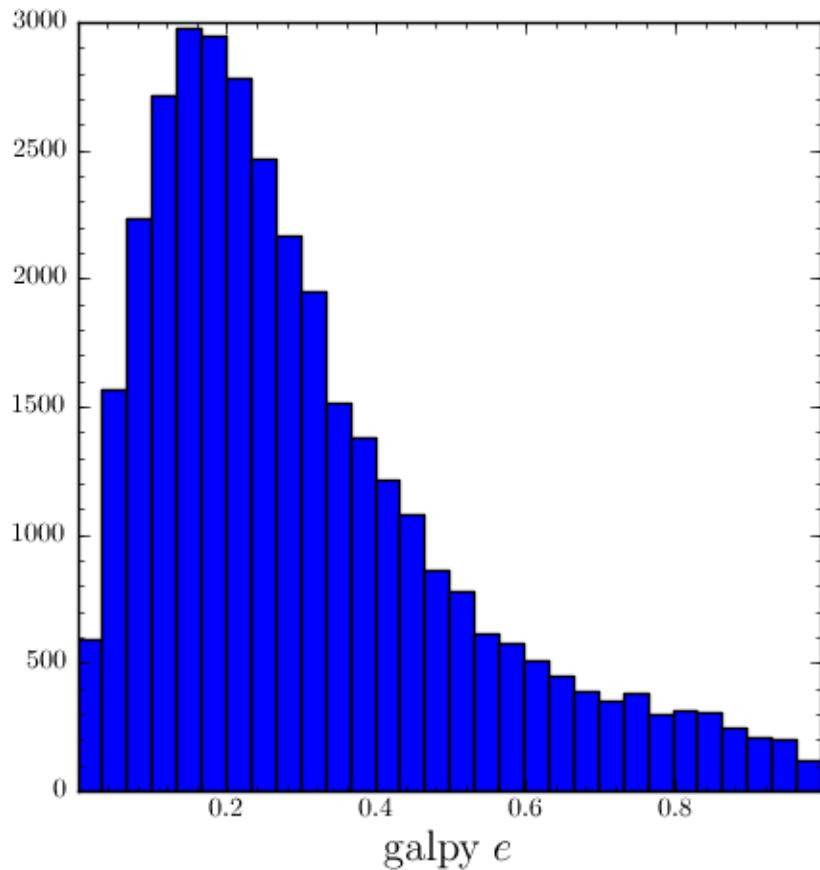
A straightforward application of galpy's orbit initialization and integration capabilities is to derive the eccentricity distribution of a set of thick disk stars. We start by downloading the sample of SDSS SEGUE ([2009AJ....137.4377Y](#)) thick disk stars compiled by Dierickx et al. ([2010arXiv1009.1616D](#)) at

<http://www.mpi-hd.mpg.de/homes/rix/Data/Dierickx-etal-tab2.txt>

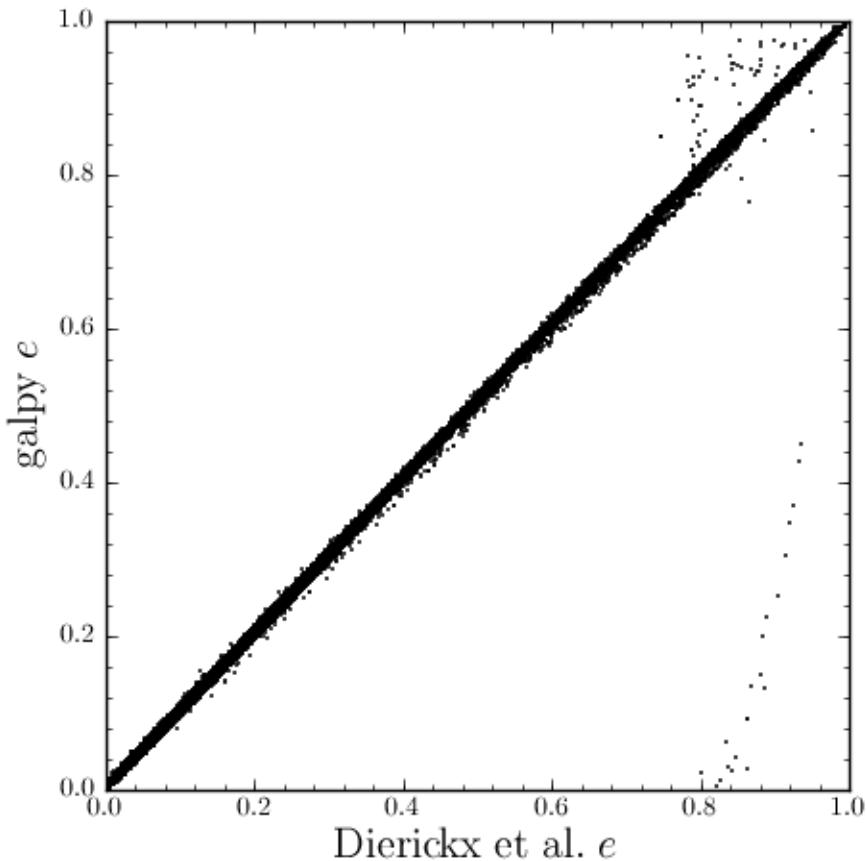
After reading in the data (RA,Dec,distance,pmRA,pmDec,vlos; see above) as a vector `vxvv` with dimensions [6,ndata] we (a) define the potential in which we want to integrate the orbits, and (b) integrate each orbit and save its eccentricity (running this for all 30,000-ish stars will take about half an hour)

```
>>> lp= LogarithmicHaloPotential(normalize=1.)
>>> ts= nu.linspace(0.,20.,10000)
>>> mye= nu.zeros(ndata)
>>> for ii in range(len(e)):
...     o= Orbit(vxvv[ii,:],radec=True,vo=220.,ro=8.) #Initialize
...     o.integrate(ts,lp) #Integrate
...     mye[ii]= o.e() #Calculate eccentricity
```

We then find the following eccentricity distribution



The eccentricity calculated by galpy compare well with those calculated by Dierickx et al., except for a few objects



The script that calculates and plots everything can be downloaded [here](#).

## 1.6 Action-angle coordinates

galpy can calculate actions and angles for a large variety of potentials (any time-independent potential in principle). These are implemented in a separate module `galpy.actionAngle`, and the preferred method for accessing them is through the routines in this module. There is also some support for accessing the `actionAngle` routines as methods of the `Orbit` class.

Action-angle coordinates can be calculated for the following potentials/approximations:

- Isochrone potential
- Spherical potentials
- Adiabatic approximation
- Staeckel approximation
- A general orbit-integration-based technique

There are classes corresponding to these different potentials/approximations and actions, frequencies, and angles can typically be calculated using these three methods:

- `__call__`: returns the actions

- actionsFreqs: returns the actions and the frequencies
- actionsFreqsAngles: returns the actions, frequencies, and angles

These are not all implemented for each of the cases above yet.

The adiabatic and Staeckel approximation have also been implemented in C, for extremely fast action-angle calculations (see below).

### 1.6.1 Action-angle coordinates for the isochrone potential

The isochrone potential is the only potential for which all of the actions, frequencies, and angles can be calculated analytically. We can do this in galpy by doing

```
>>> from galpy.potential import IsochronePotential
>>> from galpy.actionAngle import actionAngleIsochrone
>>> ip= IsochronePotential(b=1.,normalize=1.)
>>> aAI= actionAngleIsochrone(ip=ip)
```

aAI is now an instance that can be used to calculate action-angle variables for the specific isochrone potential ip. Calling this instance returns ( $J_R, L_Z, J_Z$ )

```
>>> aAI(1.,0.1,1.1,0.1,0.) #inputs R,vR,vT,z,vz
(array([ 0.00713759]), array([ 1.1]), array([ 0.00553155]))
```

or for a more eccentric orbit

```
>>> aAI(1.,0.5,1.3,0.2,0.1)
(array([ 0.13769498]), array([ 1.3]), array([ 0.02574507]))
```

Note that we can also specify phi, but this is not necessary

```
>>> aAI(1.,0.5,1.3,0.2,0.1,0.)
(array([ 0.13769498]), array([ 1.3]), array([ 0.02574507]))
```

We can likewise calculate the frequencies as well

```
>>> aAI.actionsFreqs(1.,0.5,1.3,0.2,0.1,0.)
(array([ 0.13769498]),
 array([ 1.3]),
 array([ 0.02574507]),
 array([ 1.29136096]),
 array([ 0.79093738]),
 array([ 0.79093738]))
```

The output is ( $J_R, L_Z, J_Z, \Omega_R, \Omega_\phi, \Omega_Z$ ). For any spherical potential,  $\Omega_\phi = \text{sgn}(L_Z)\Omega_Z$ , such that the last two frequencies are the same.

We obtain the angles as well by calling

```
>>> aAI.actionsFreqsAngles(1.,0.5,1.3,0.2,0.1,0.)
(array([ 0.13769498]),
 array([ 1.3]),
 array([ 0.02574507]),
 array([ 1.29136096]),
 array([ 0.79093738]),
 array([ 0.79093738]),
 array([ 0.57101518]),
 array([ 5.96238847]),
 array([ 1.24999949]))
```

The output here is  $(J_R, L_Z, J_Z, \Omega_R, \Omega_\phi, \Omega_Z, \theta_R, \theta_\phi, \theta_Z)$ .

To check that these are good action-angle variables, we can calculate them along an orbit

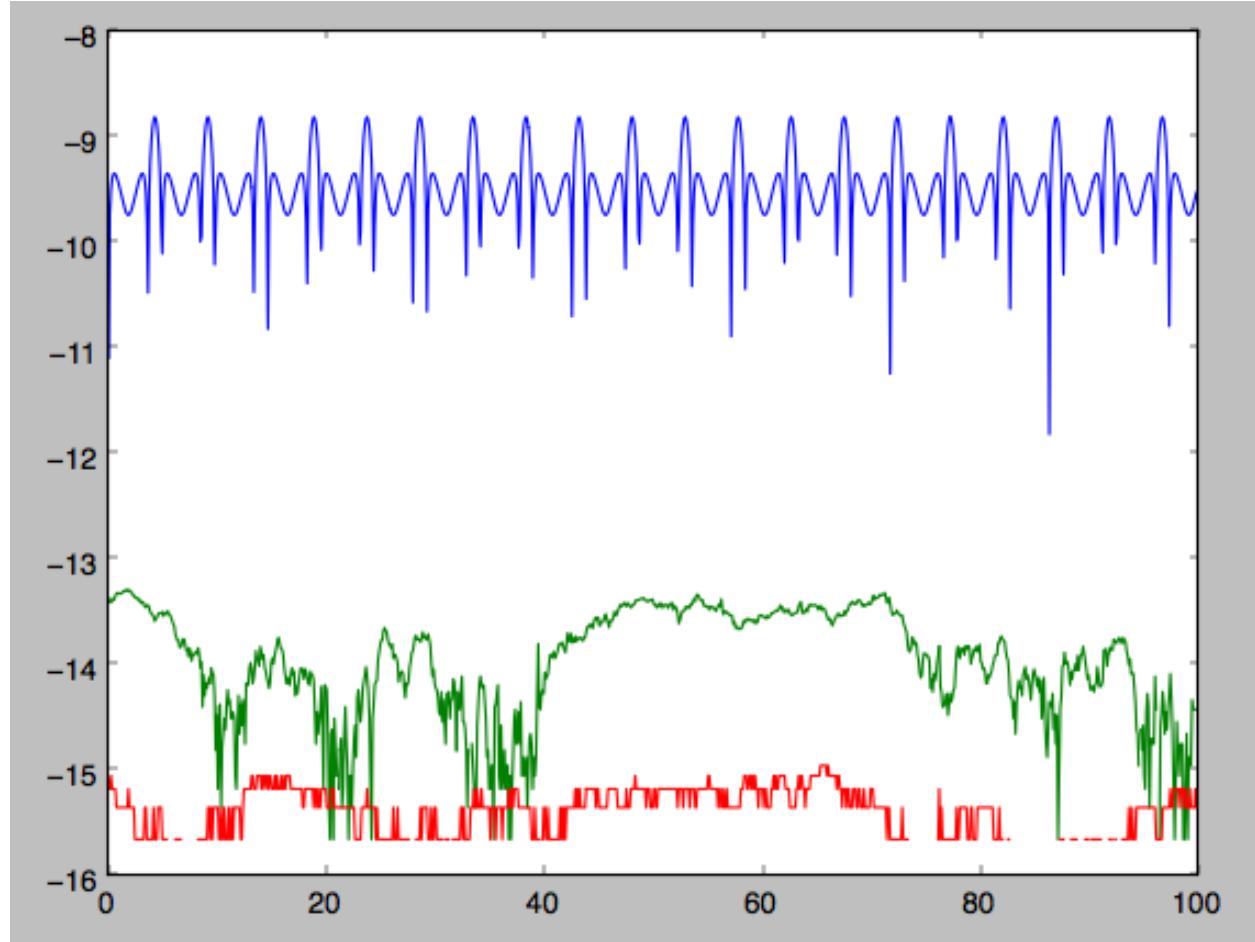
```
>>> from galpy.orbit import Orbit
>>> o= Orbit([1.,0.5,1.3,0.2,0.1,0.])
>>> ts= numpy.linspace(0.,100.,1001)
>>> o.integrate(ts,ip)
>>> jfa= aAI.actionsFreqsAngles(o.R(ts),o.vR(ts),o.vT(ts),o.z(ts),o.vz(ts),o.phi(ts))
```

which works because we can provide arrays for the R etc. inputs.

We can then check that the actions are constant over the orbit

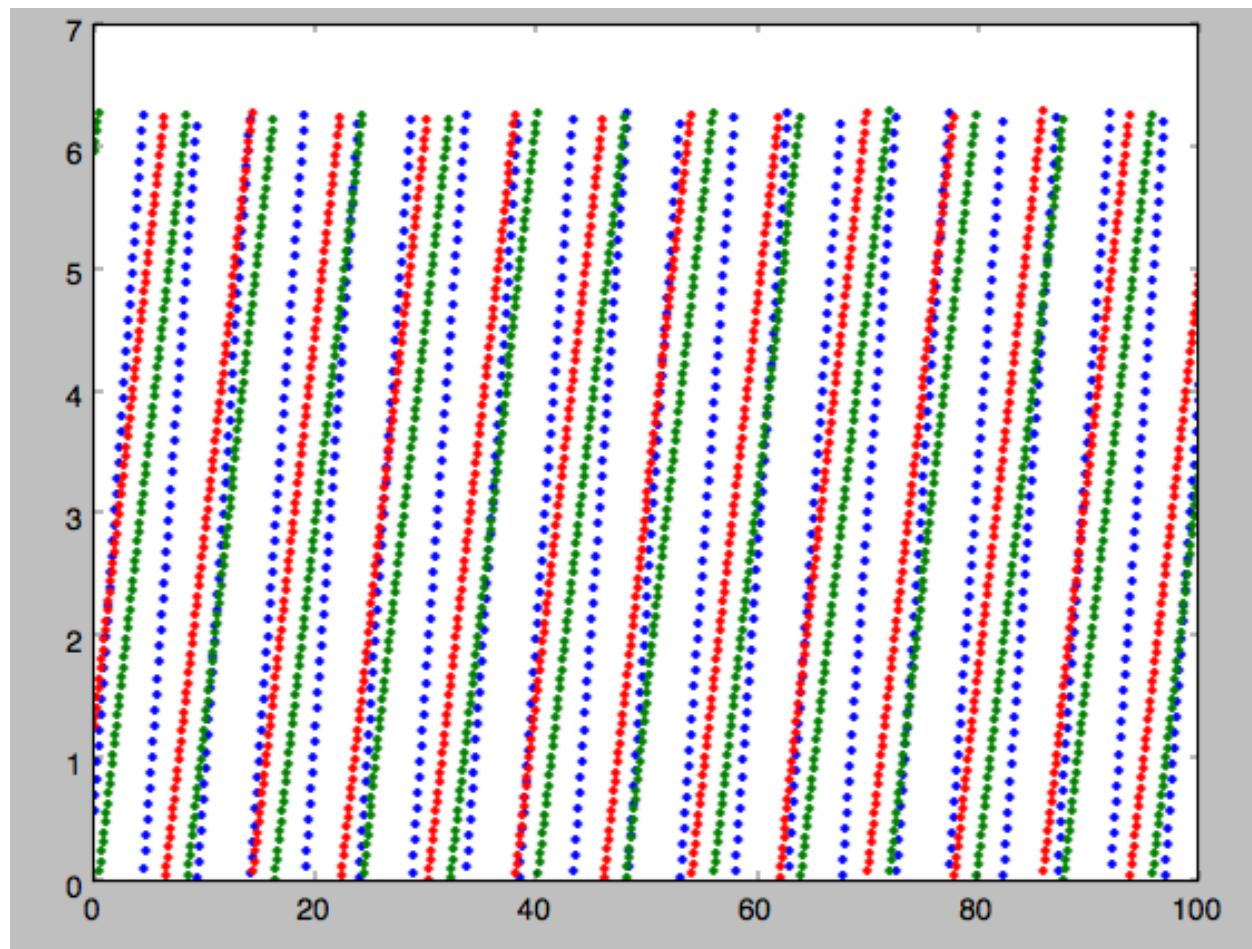
```
>>> plot(ts,numpy.log10(numpy.fabs((jfa[0]-numpy.mean(jfa[0])))))
>>> plot(ts,numpy.log10(numpy.fabs((jfa[1]-numpy.mean(jfa[1])))))
>>> plot(ts,numpy.log10(numpy.fabs((jfa[2]-numpy.mean(jfa[2])))))
```

which gives



The actions are all conserved. The angles increase linearly with time

```
>>> plot(ts,jfa[6],'b.')
>>> plot(ts,jfa[7],'g.')
>>> plot(ts,jfa[8],'r.')
```



## 1.6.2 Action-angle coordinates for spherical potentials

Action-angle coordinates for any spherical potential can be calculated using a few orbit integrations. These are implemented in galpy in the `actionAngleSpherical` module. For example, we can do

```
>>> from galpy.potential import LogarithmicHaloPotential
>>> lp= LogarithmicHaloPotential(normalize=1.)
>>> from galpy.actionAngle import actionAngleSpherical
>>> aAS= actionAngleSpherical(pot=lp)
```

For the same eccentric orbit as above we find

```
>>> aAS(1.,0.5,1.3,0.2,0.1,0.)
(array([ 0.22022112]), array([ 1.3]), array([ 0.02574507]))
>>> aAS.actionsFreqs(1.,0.5,1.3,0.2,0.1,0.)
(array([ 0.22022112]),
 array([ 1.3]),
 array([ 0.02574507]),
 array([ 0.87630459]),
 array([ 0.60872881]),
 array([ 0.60872881]))
>>> aAS.actionsFreqsAngles(1.,0.5,1.3,0.2,0.1,0.)
(array([ 0.22022112]),
 array([ 1.3]),
```

```
array([ 0.02574507]),
array([ 0.87630459]),
array([ 0.60872881]),
array([ 0.60872881]),
array([ 0.40443857]),
array([ 5.85965048]),
array([ 1.1472615]))
```

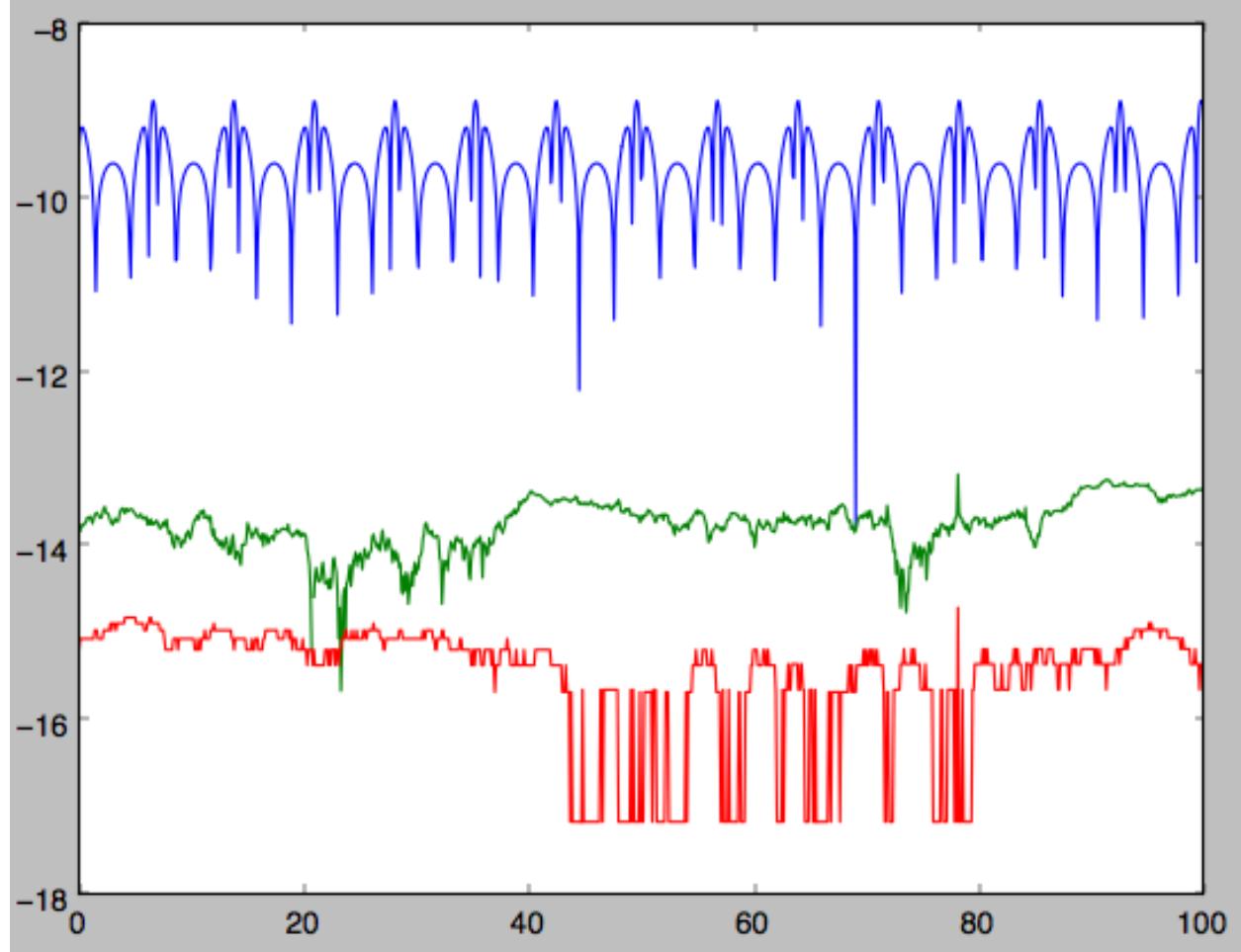
We can again check that the actions are conserved along the orbit and that the angles increase linearly with time:

```
>>> o.integrate(ts,lp)
>>> jfa= aAS.actionsFreqsAngles(o.R(ts),o.vR(ts),o.vT(ts),o.z(ts),o.vz(ts),o.phi(ts),fixed_quad=True)
```

where we use `fixed_quad=True` for a faster evaluation of the required one-dimensional integrals using Gaussian quadrature. We then plot the action fluctuations

```
>>> plot(ts,numpy.log10(numpy.fabs((jfa[0]-numpy.mean(jfa[0])))))
>>> plot(ts,numpy.log10(numpy.fabs((jfa[1]-numpy.mean(jfa[1])))))
>>> plot(ts,numpy.log10(numpy.fabs((jfa[2]-numpy.mean(jfa[2])))))
```

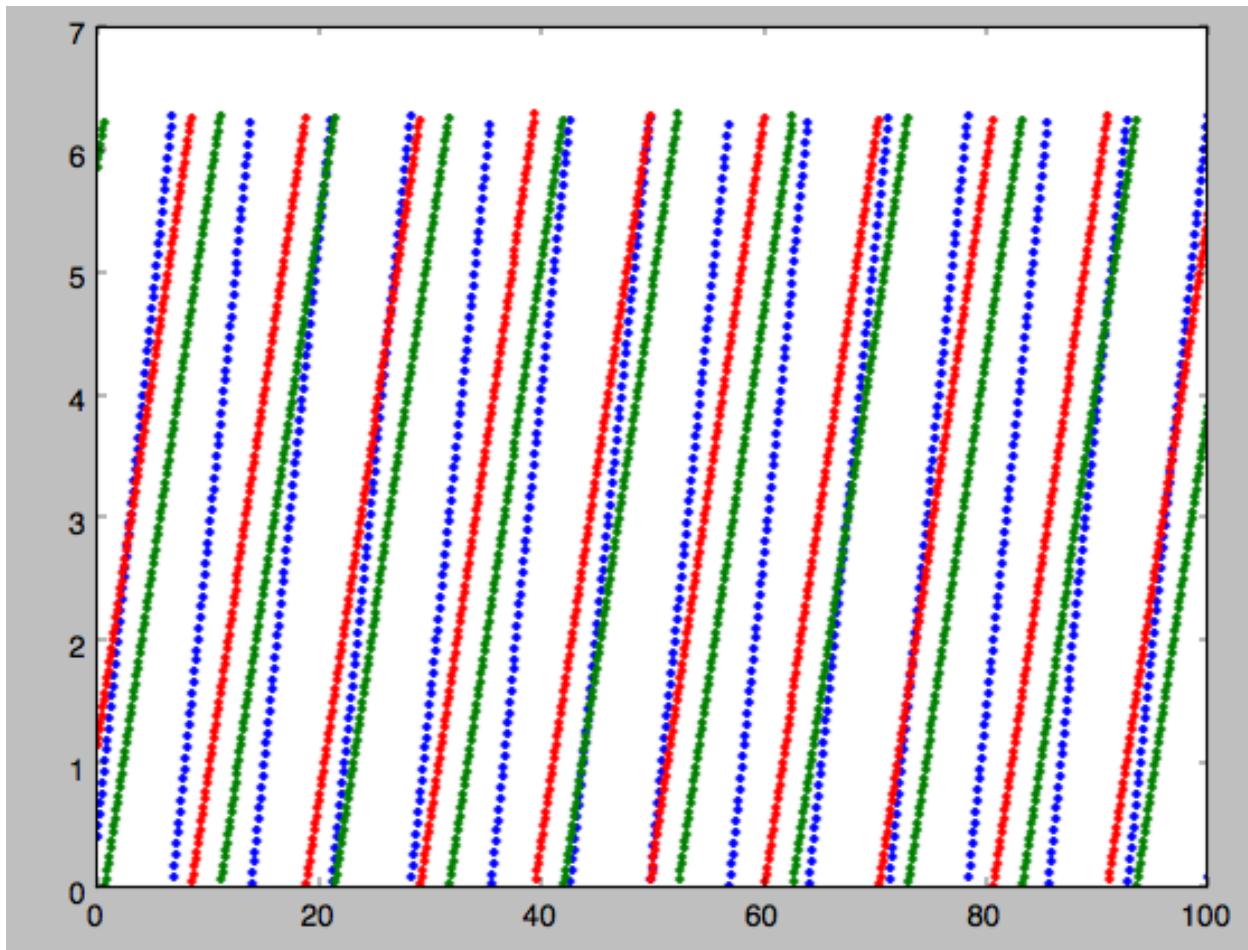
which gives



showing that the actions are all conserved. The angles again increase linearly with time

```
>>> plot(ts,jfa[6],'b.')
>>> plot(ts,jfa[7],'g.')
```

```
>>> plot(ts,jfa[8],'r.')
```



We can check the spherical action-angle calculations against the analytical calculations for the isochrone potential. Starting again from the isochrone potential used in the previous section

```
>>> ip= IsochronePotential(b=1.,normalize=1.)
>>> aAI= actionAngleIsochrone(ip=ip)
>>> aAS= actionAngleSpherical(pot=ip)
```

we can compare the actions, frequencies, and angles computed using both

```
>>> aAI.actionsFreqsAngles(1.,0.5,1.3,0.2,0.1,0.)
(array([ 0.13769498]),
 array([ 1.3]),
 array([ 0.02574507]),
 array([ 1.29136096]),
 array([ 0.79093738]),
 array([ 0.79093738]),
 array([ 0.57101518]),
 array([ 5.96238847]),
 array([ 1.24999949]))
>>> aAS.actionsFreqsAngles(1.,0.5,1.3,0.2,0.1,0.)
(array([ 0.13769498]),
 array([ 1.3]),
 array([ 0.02574507]),
 array([ 1.29136096]),
```

```
array([ 0.79093738]),
array([ 0.79093738]),
array([ 0.57101518]),
array([ 5.96238838]),
array([ 1.2499994]))
```

or more explicitly comparing the two

```
>>> [r-s for r,s in zip(aAI.actionsFreqsAngles(1.,0.5,1.3,0.2,0.1,0.),aAS.actionsFreqsAngles(1.,0.5,1.3,0.2,0.1,0.))]
[array([ 6.66133815e-16]),
array([ 0.]),
array([ 0.]),
array([-4.53851845e-10]),
array([ 4.74775219e-10]),
array([ 4.74775219e-10]),
array([-1.65965242e-10]),
array([ 9.04759645e-08]),
array([ 9.04759649e-08])]
```

### 1.6.3 Action-angle coordinates using the adiabatic approximation

For non-spherical, axisymmetric potentials galpy contains multiple methods for calculating approximate action–angle coordinates. The simplest of those is the adiabatic approximation, which works well for disk orbits that do not go too far from the plane, as it assumes that the vertical motion is decoupled from that in the plane (e.g., 2010MNRAS.401.2318B).

Setup is similar as for other actionAngle objects

```
>>> from galpy.potential import MWPotential
>>> from galpy.actionAngle import actionAngleAdiabatic
>>> aAA= actionAngleAdiabatic(pot=MWPotential)
```

and evaluation then proceeds similarly as before

```
>>> aAA(1.,0.1,1.1,0.,0.05)
(0.011551694768963469, 1.1, 0.00042376727426256727)
```

We can again check that the actions are conserved along the orbit

```
>>> from galpy.orbit import Orbit
>>> ts=numpy.linspace(0.,100.,1001)
>>> o= Orbit([1.,0.1,1.1,0.,0.05])
>>> o.integrate(ts,MWPotential)
>>> js= aAA(o.R(ts),o.vR(ts),o.vT(ts),o.z(ts),o.vz(ts))
```

This takes a while. The adiabatic approximation is also implemented in C, which leads to great speed-ups. Here is how to use it

```
>>> timeit(aAA(1.,0.1,1.1,0.,0.05))
10 loops, best of 3: 48.7 ms per loop
>>> aAA= actionAngleAdiabatic(pot=MWPotential,c=True)
>>> timeit(aAA(1.,0.1,1.1,0.,0.05))
1000 loops, best of 3: 1.2 ms per loop
```

or about a *40 times* speed-up. For arrays the speed-up is even more impressive

```
>>> s= numpy.ones(100)
>>> timeit(aAA(1.*s,0.1*s,1.1*s,0.*s,0.05*s))
```

```
1000 loops, best of 3: 1.8 ms per loop
>>> aAA= actionAngleAdiabatic(pot=MWPotential) #back to no C
>>> timeit(aAA(1.*s,0.1*s,1.1*s,0.*s,0.05*s))
1 loops, best of 3: 4.94 s per loop
```

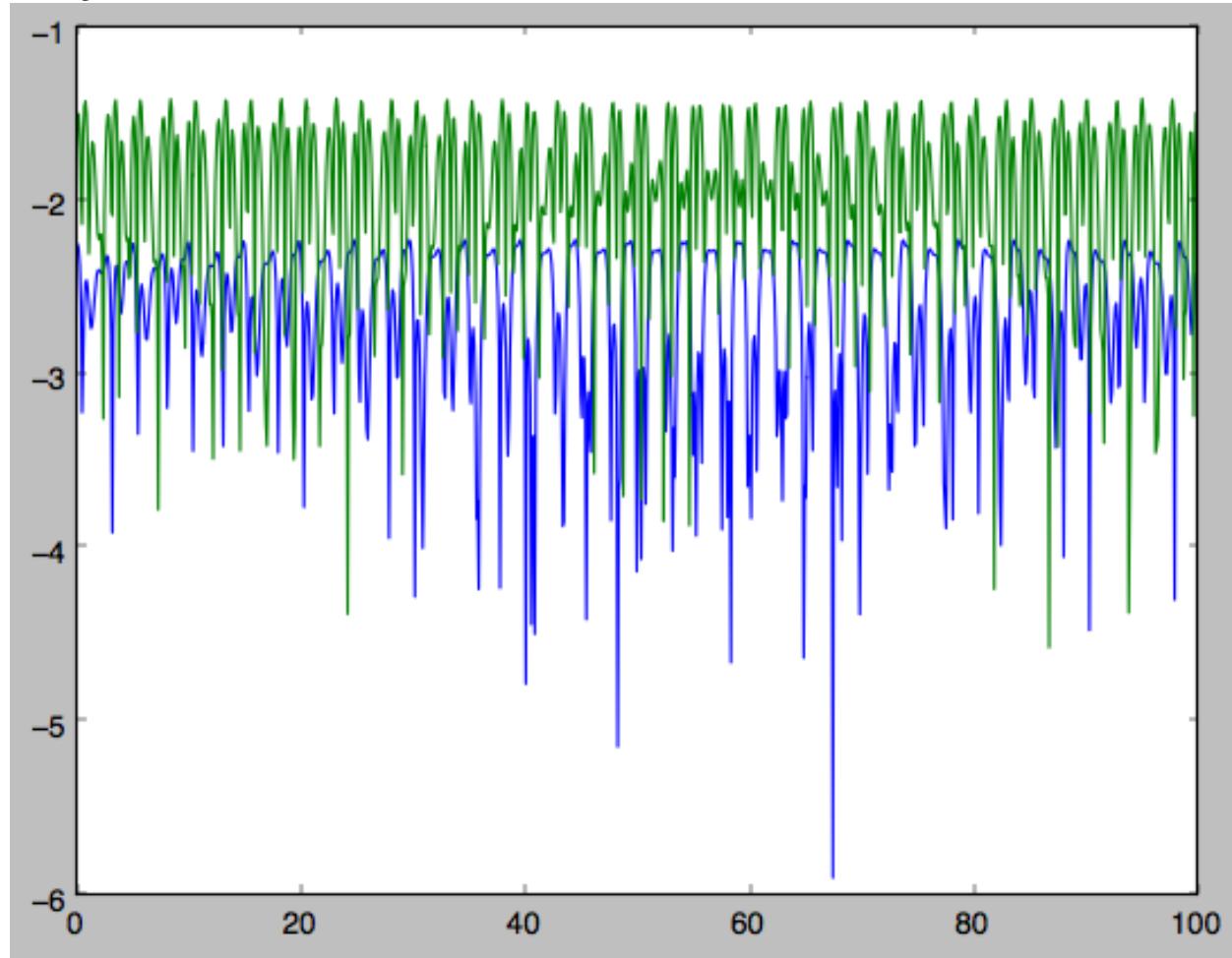
or a speed-up of 2700! Back to the previous example, you can run it with `c=True` to speed up the computation

```
>>> aAA= actionAngleAdiabatic(pot=MWPotential,c=True)
>>> js= aAA(o.R(ts),o.vR(ts),o.vT(ts),o.z(ts),o.vz(ts))
```

We can plot the radial- and vertical-action fluctuation as a function of time

```
>>> plot(ts,numpy.log10(numpy.fabs((js[0]-numpy.mean(js[0]))/numpy.mean(js[0]))))
>>> plot(ts,numpy.log10(numpy.fabs((js[2]-numpy.mean(js[2]))/numpy.mean(js[2]))))
```

which gives



The radial action is conserved to about half a percent, the vertical action to two percent.

The adiabatic approximation works well for orbits that stay close to the plane. The orbit we have been considering so far only reaches a height two percent of  $R_0$ , or about 150 pc for  $R_0 = 8$  kpc.

```
>>> o.zmax()*8.
0.1561562486879895
```

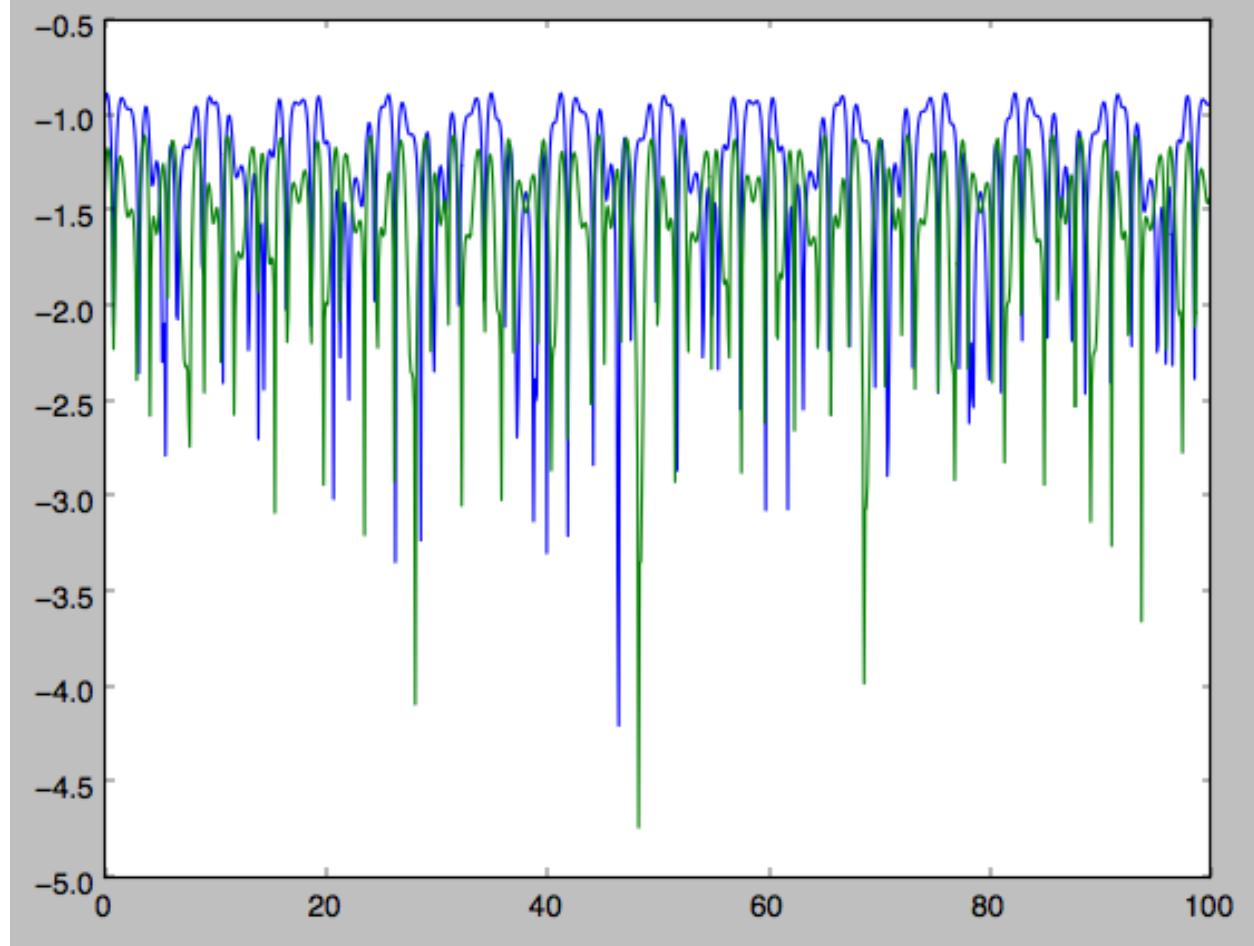
For orbits that reach distances of a kpc and more from the plane, the adiabatic approximation does not work as well. For example,

```
>>> o= Orbit([1.,0.1,1.1,0.,0.25])
>>> o.integrate(ts,MWPotential)
>>> o.zmax()*8.
1.1288142099238863
```

and we can again calculate the actions along the orbit

```
>>> js= aAA(o.R(ts),o.vR(ts),o.vT(ts),o.z(ts),o.vz(ts))
>>> plot(ts,np.log10(np.fabs((js[0]-np.mean(js[0]))/np.mean(js[0]))))
>>> plot(ts,np.log10(np.fabs((js[2]-np.mean(js[2]))/np.mean(js[2]))))
```

which gives



The radial action is now only conserved to about ten percent and the vertical action to approximately five percent.

**Warning:** Frequencies and angles using the adiabatic approximation are not implemented at this time.

#### 1.6.4 Action-angle coordinates using the Staeckel approximation

A better approximation than the adiabatic one is to locally approximate the potential as a Staeckel potential, for which actions, frequencies, and angles can be calculated through numerical integration. galpy contains an implementation of the algorithm of Binney (2012; [2012MNRAS.426.1324B](#)), which accomplishes the Staeckel approximation for disk-like (i.e., oblate) potentials without explicitly fitting a Staeckel potential. For all intents and purposes the adiabatic approximation is made obsolete by this new method, which is as fast and more precise. The only advantage of the

adiabatic approximation over the Staeckel approximation is that the Staeckel approximation requires the user to specify a *focal length*  $\Delta$  to be used in the Staeckel approximation. However, this focal length can be easily estimated from the second derivatives of the potential (see Sanders 2012; 2012MNRAS.426..128S).

Starting from the second orbit example in the adiabatic section above, we first estimate a good focal length of the `MWPotential` to use in the Staeckel approximation. We do this by averaging (through the median) estimates at positions around the orbit (which we integrated in the example above)

```
>>> from galpy.actionAngle import estimateDeltaStaeckel
>>> estimateDeltaStaeckel(o.R(ts),o.z(ts),pot=MWPotential)
0.54421090762027347
```

We will use  $\Delta = 0.55$  in what follows. We set up the `actionAngleStaeckel` object

```
>>> aAS= actionAngleStaeckel(pot=MWPotential,delta=0.55,c=False) #c=True is the default
```

and calculate the actions

```
>>> aAS(o.R(),o.vR(),o.vT(),o.z(),o.vz())
(0.015760720988339319, 1.1000000000000001, 0.013466290557851267)
```

The adiabatic approximation from above gives

```
>>> aAA(o.R(),o.vR(),o.vT(),o.z(),o.vz())
(0.0138915441284973, 1.1000000000000001, 0.01383357354294852)
```

The `actionAngleStaeckel` calculations are sped up in two ways. First, the action integrals can be calculated using Gaussian quadrature by specifying `fixed_quad=True`

```
>>> aAS(o.R(),o.vR(),o.vT(),o.z(),o.vz(),fixed_quad=True)
(0.015767954890517084, 1.1000000000000001, 0.013468235165983522)
```

which in itself leads to a ten times speed up

```
>>> timeit(aAS(o.R(),o.vR(),o.vT(),o.z(),o.vz(),fixed_quad=False))
10 loops, best of 3: 43.9 ms per loop
>>> timeit(aAS(o.R(),o.vR(),o.vT(),o.z(),o.vz(),fixed_quad=True))
100 loops, best of 3: 3.87 ms per loop
```

Second, the `actionAngleStaeckel` calculations have also been implemented in C, which leads to even greater speed-ups, especially for arrays

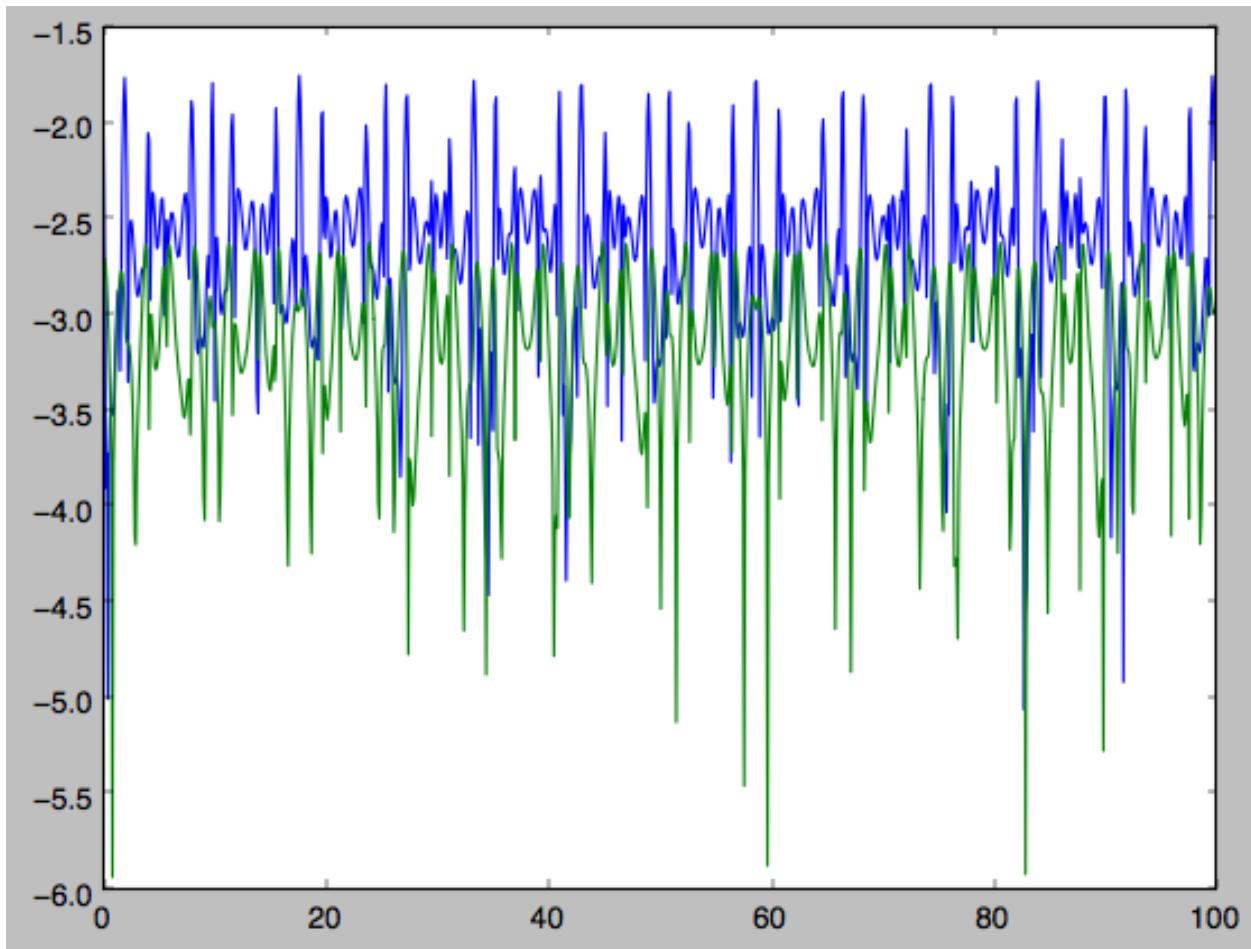
```
>>> aAS= actionAngleStaeckel(pot=MWPotential,delta=0.55,c=True)
>>> s= numpy.ones(100)
>>> timeit(aAS(1.*s,0.1*s,1.1*s,0.*s,0.05*s))
100 loops, best of 3: 2.37 ms per loop
>>> aAS= actionAngleStaeckel(pot=MWPotential,delta=0.55,c=False) #back to no C
>>> timeit(aAS(1.*s,0.1*s,1.1*s,0.*s,0.05*s,fixed_quad=True))
1 loops, best of 3: 410 ms per loop
```

or a *two hundred times* speed up.

We can now go back to checking that the actions are conserved along the orbit

```
>>> js= aAS(o.R(ts),o.vR(ts),o.vT(ts),o.z(ts),o.vz(ts),fixed_quad=True)
>>> plot(ts,numpy.log10(numpy.fabs((js[0]-numpy.mean(js[0]))/numpy.mean(js[0]))))
>>> plot(ts,numpy.log10(numpy.fabs((js[2]-numpy.mean(js[2]))/numpy.mean(js[2]))))
```

which gives



The radial action is now conserved to better than a percent and the vertical action to only a fraction of a percent. Clearly, this is much better than the five to ten percent errors found for the adiabatic approximation above.

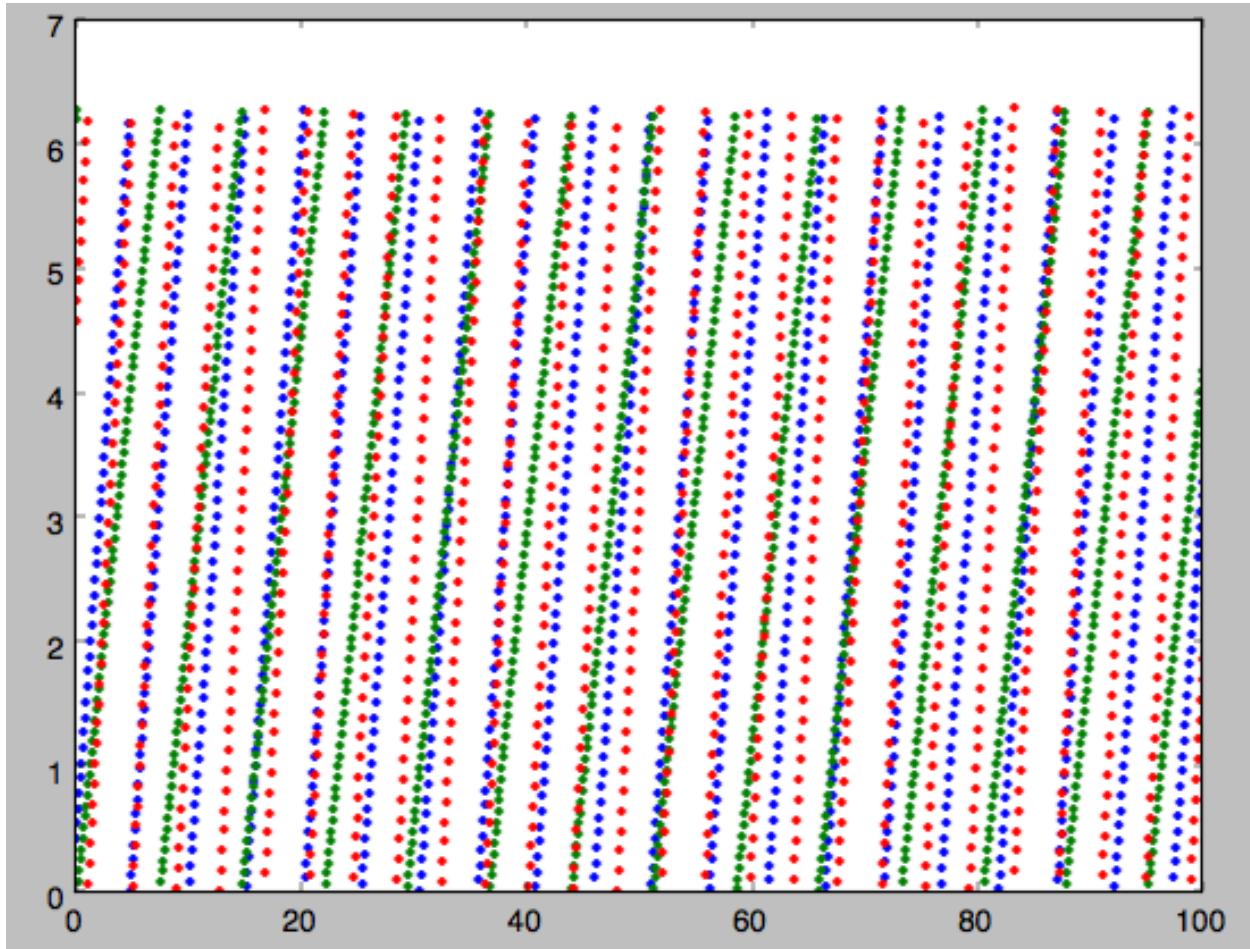
For the Staeckel approximation we can also calculate frequencies and angles through the `actionsFreqs` and `actionsFreqsAngles` methods.

**Warning:** Frequencies and angles using the Staeckel approximation are *only* implemented in C. So use `c=True` in the setup of the `actionAngleStaeckel` object.

```
>>> aAS= actionAngleStaeckel(pot=MWPotential,delta=0.55,c=True)
>>> o= Orbit([1.,0.1,1.1,0.,0.25,0.]) #need to specify phi for angles
>>> aAS.actionsFreqsAngles(o.R(),o.vR(),o.vT(),o.z(),o.vz(),o.phi())
(array([ 0.01576795]),
 array([ 1.1]),
 array([ 0.01346824]),
 array([ 1.22171491]),
 array([ 0.85773142]),
 array([ 1.60476805]),
 array([ 0.41881231]),
 array([ 6.18908605]),
 array([ 4.57359281]))
```

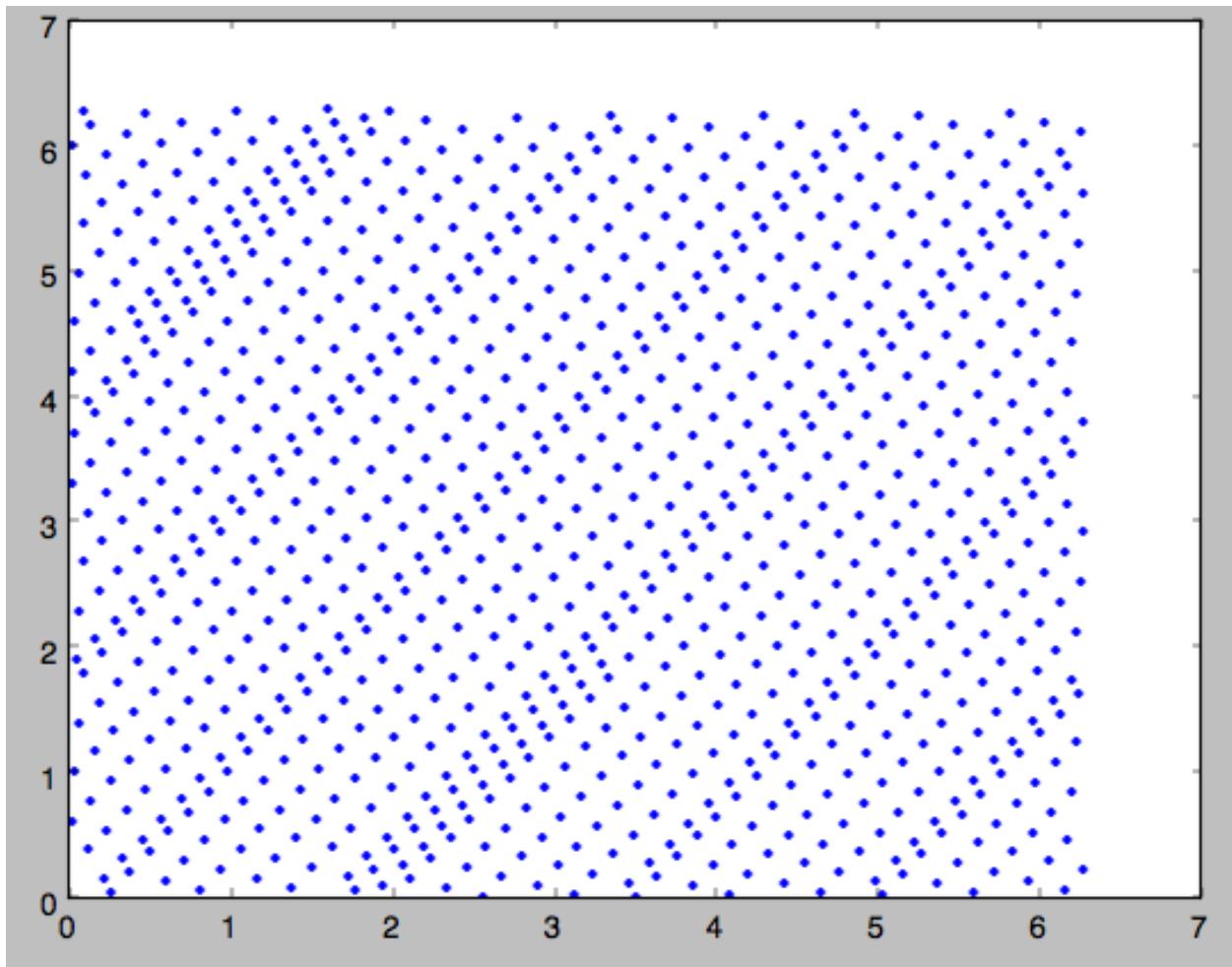
and we can check that the angles increase linearly along the orbit

```
>>> o.integrate(ts,MWPotential)
>>> jfa= aAS.actionsFreqsAngles(o.R(ts),o.vR(ts),o.vT(ts),o.z(ts),o.vz(ts),o.phi(ts))
>>> plot(ts,jfa[6],'b.')
>>> plot(ts,jfa[7],'g.')
>>> plot(ts,jfa[8],'r.')
```



or

```
>>> plot(jfa[6],jfa[8],'b.') 
```



### 1.6.5 Action-angle coordinates using an orbit-integration-based approximation

The adiabatic and Staeckel approximations used above are good for stars on close-to-circular orbits, but they break down for more eccentric orbits (specifically, orbits for which the radial and/or vertical action is of a similar magnitude as the angular momentum). This is because the approximations made to the potential in these methods (that it is separable in  $R$  and  $z$  for the adiabatic approximation and that it is close to a Staeckel potential for the Staeckel approximation) break down for such orbits. Unfortunately, these methods cannot be refined to provide better approximations for eccentric orbits.

galpy contains a new method for calculating actions, frequencies, and angles that is completely general for any static potential. It can calculate the actions to any desired precision for any orbit in such potentials. The method works by employing an auxiliary isochrone potential and calculates action-angle variables by arithmetic operations on the actions and angles calculated in the auxiliary potential along an orbit (integrated in the true potential). Full details can be found in Appendix A of Bovy (2014).

We setup this method for a logarithmic potential as follows

```
>>> from galpy.actionAngle import actionAngleIsochroneApprox
>>> from galpy.potential import LogarithmicHaloPotential
>>> lp= LogarithmicHaloPotential(normalize=1.,q=0.9)
>>> aAIA= actionAngleIsochroneApprox(pot=lp,b=0.8)
```

$b=0.8$  here sets the scale parameter of the auxiliary isochrone potential; this potential can also be specified as an

IsochronePotential instance through `ip=`). We can now calculate the actions for an orbit similar to that of the GD-1 stream

```
>>> obs= numpy.array([1.56148083, 0.35081535, -1.15481504, 0.88719443, -0.47713334, 0.12019596]) #orbit s
>>> aAIA(*obs)
(array([ 0.16605011]), array([-1.80322155]), array([ 0.50704439]))
```

An essential requirement of this method is that the angles calculated in the auxiliary potential go through the full range  $[0, 2\pi]$ . If this is not the case, galpy will raise a warning

```
>>> aAIA= actionAngleIsochroneApprox(pot=lp,b=10.8)
>>> aAIA(*obs)
galpyWarning: Full radial angle range not covered for at least one object; actions are likely not reliable
(array([ 0.08985167]), array([-1.80322155]), array([ 0.50849276]))
```

Therefore, some care should be taken to choosing a good auxiliary potential. galpy contains a method to estimate a decent scale parameter for the auxiliary scale parameter, which works similar to `estimateDeltaStaeckel` above except that it also gives a minimum and maximum b if multiple R and z are given

```
>>> from galpy.actionAngle import estimateBIsochrone
>>> from galpy.orbit import Orbit
>>> o= Orbit(obs)
>>> ts= numpy.linspace(0.,100.,1001)
>>> o.integrate(ts,lp)
>>> estimateBIsochrone(o.R(ts),o.z(ts),pot=lp)
(0.78065062339131952, 1.2265541473461612, 1.4899326335155412) #bmin,bmedian,bmax over the orbit
```

Experience shows that a scale parameter somewhere in the range returned by this function makes sure that the angles go through the full  $[0, 2\pi]$  range. However, even if the angles go through the full range, the closer the angles increase to linear, the better the convergence of the algorithm is (and especially, the more accurate the calculation of the frequencies and angles is, see below). For example, for the scale parameter at the upper end of the range

```
>>> aAIA= actionAngleIsochroneApprox(pot=lp,b=1.5)
>>> aAIA(*obs)
(array([ 0.01120145]), array([-1.80322155]), array([ 0.50788893]))
```

which does not agree with the previous calculation. We can inspect how the angles increase and how the actions converge by using the `aAIA.plot` function. For example, we can plot the radial versus the vertical angle in the auxiliary potential

```
>>> aAIA.plot(*obs,type='araz')
```

which gives

and this clearly shows that the angles increase *very* non-linearly, because the auxiliary isochrone potential used is too far from the real potential. This causes the actions to converge only very slowly. For example, for the radial action we can plot the converge as a function of integration time

```
>>> aAIA.plot(*obs,type='jr')
```

which gives

This Figure clearly shows that the radial action has not converged yet. We need to integrate *much* longer in this auxiliary potential to obtain convergence and because the angles increase so non-linearly, we also need to integrate the orbit much more finely:

```
>>> aAIA= actionAngleIsochroneApprox(pot=lp,b=1.5,tintJ=1000,ntintJ=800000)
>>> aAIA(*obs)
(array([ 0.01711635]), array([-1.80322155]), array([ 0.51008058]))
>>> aAIA.plot(*obs,type='jr')
```

which shows slow convergence

Finding a better auxiliary potential makes convergence *much* faster and also allows the frequencies and the angles to be calculated by removing the small wiggles in the auxiliary angles vs. time (in the angle plot above, the wiggles are much larger, such that removing them is hard). The auxiliary potential used above had  $b=0.8$ , which shows very quick convergenge and good behavior of the angles

```
>>> aAIA= actionAngleIsochroneApprox(pot=lp,b=0.8)
>>> aAIA.plot(*obs,type='jr')
```

gives

and

```
>>> aAIA.plot(*obs,type='araz')
```

gives

We can remove the periodic behavior from the angles, which clearly shows that they increase close-to-linear with time

```
>>> aAIA.plot(*obs,type='araz',deperiod=True)
```

We can then calculate the frequencies and the angles for this orbit as

```
>>> aAIA.actionsFreqsAngles(*obs)
(array([ 0.16392384]),
 array([-1.80322155]),
 array([ 0.50999882]),
 array([ 0.55808933]),
 array([-0.38475753]),
 array([ 0.42199713]),
 array([ 0.18739688]),
 array([ 0.3131815]),
 array([ 2.18425661]))
```

This function takes as an argument `maxn`= the maximum  $n$  for which to remove sinusoidal wiggles. So we can raise this, for example to 4 from 3

```
>>> aAIA.actionsFreqsAngles(*obs,maxn=4)
(array([ 0.16392384]),
 array([-1.80322155]),
 array([ 0.50999882]),
 array([ 0.55808776]),
 array([-0.38475733]),
 array([ 0.4219968]),
 array([ 0.18732009]),
 array([ 0.31318534]),
 array([ 2.18421296]))
```

Clearly, there is very little change, as most of the wiggles are of low  $n$ .

**Warning:** While the orbit-based `actionAngle` technique in principle works for triaxial potentials, angles and frequencies for non-axisymmetric potentials are not implemented yet.

This technique also works for triaxial potentials, but using those requires the code to also use the azimuthal angle variable in the auxiliary potential (this is unnecessary in axisymmetric potentials as the  $z$  component of the angular momentum is conserved). We can calculate actions for triaxial potentials by specifying that `nonaxi=True`:

```
>>> aAIA(*obs,nonaxi=True)
(array([ 0.16605011]), array([-1.80322155]), array([ 0.50704439]))
```

galpy currently does not contain any triaxial potentials, so we cannot illustrate this here with any real triaxial potentials.

## 1.6.6 Accessing action-angle coordinates for Orbit instances

While the recommended way to access the `actionAngle` routines is through the methods in the `galpy.actionAngle` modules, action-angle coordinates can also be calculated for `galpy.orbit.Orbit` instances. This is illustrated here briefly. We initialize an `Orbit` instance

```
>>> from galpy.orbit import Orbit
>>> from galpy.potential import MWPotential
>>> o= Orbit([1.,0.1,1.1,0.,0.25,0.])
```

and we can then calculate the actions (default is to use the adiabatic approximation)

```
>>> o.jr(MWPotential), o.jp(MWPotential), o.jz(MWPotential)
(0.0138915441284973, 1.1, 0.01383357354294852)
```

`o.jp` here gives the azimuthal action (which is the  $z$  component of the angular momentum for axisymmetric potentials). We can also use the other methods described above, but note that these require extra parameters related to the approximation to be specified (see above):

```
>>> o.jr(MWPotential,type='staeckel',delta=0.55), o.jp(MWPotential,type='staeckel',delta=0.55), o.jz(MWPotential,type='staeckel',delta=0.55)
(array([ 0.01576795]), array([ 1.1]), array([ 0.01346824]))
>>> o.jr(MWPotential,type='isochroneApprox',b=0.8), o.jp(MWPotential,type='isochroneApprox',b=0.8), o.jz(MWPotential,type='isochroneApprox',b=0.8)
(array([ 0.0155484]), array([ 1.1]), array([ 0.01350128]))
```

These two methods give very precise actions for this orbit (both are converged to about 1%) and they agree very well

```
>>> (o.jr(MWPotential,type='staeckel',delta=0.55)-o.jr(MWPotential,type='isochroneApprox',b=0.8))/o.jr(MWPotential,type='staeckel',delta=0.55)
array([-0.01412076])
>>> (o.jz(MWPotential,type='staeckel',delta=0.55)-o.jz(MWPotential,type='isochroneApprox',b=0.8))/o.jz(MWPotential,type='staeckel',delta=0.55)
array([-0.00244754])
```

**Warning:** Once an action, frequency, or angle is calculated for a given type of calculation (e.g., `staeckel`), the parameters for that type are fixed in the `Orbit` instance. Call `o.resetA()` to reset the action-angle instance used when using different parameters (i.e., different `delta=` for `staeckel` or different `b=` for `isochroneApprox`).

We can also calculate the frequencies and the angles. This requires using the Staeckel or Isochrone approximations, because frequencies and angles are currently not supported for the adiabatic approximation. For example, the radial frequency

```
>>> o.Or(MWPotential,type='staeckel',delta=0.55)
1.2217149111363643
>>> o.Or(MWPotential,type='isochroneApprox',b=0.8)
1.222457055706389
```

and the radial angle

```
>>> o.wr(MWPotential,type='staeckel',delta=0.55)
0.4188123062144965
>>> o.wr(MWPotential,type='isochroneApprox',b=0.8)
0.42281897179881867
```

which again agree to 1%. We can also calculate the other frequencies, angles, as well as periods using the functions `o.Op`, `o.oz`, `o.wp`, `o.wz`, `o.Tr`, `o.Tp`, `o.Tz`.

## 1.6.7 Example: Evidence for a Lindblad resonance in the Solar neighborhood

We can use galpy to calculate action-angle coordinates for a set of stars in the Solar neighborhood and look for unexplained features. For this we download the data from the Geneva-Copenhagen Survey (2009A&A...501..941H; data available at [viZier](#)). Since the velocities in this catalog are given as U,V, and W, we use the `radec` and `UVW` keywords to initialize the orbits from the raw data. For each object `ii`

```
>>> o= Orbit(vxvv[ii,:],rapec=True,uvw=True,vo=220.,ro=8.)
```

We then calculate the actions and angles for each object in a flat rotation curve potential

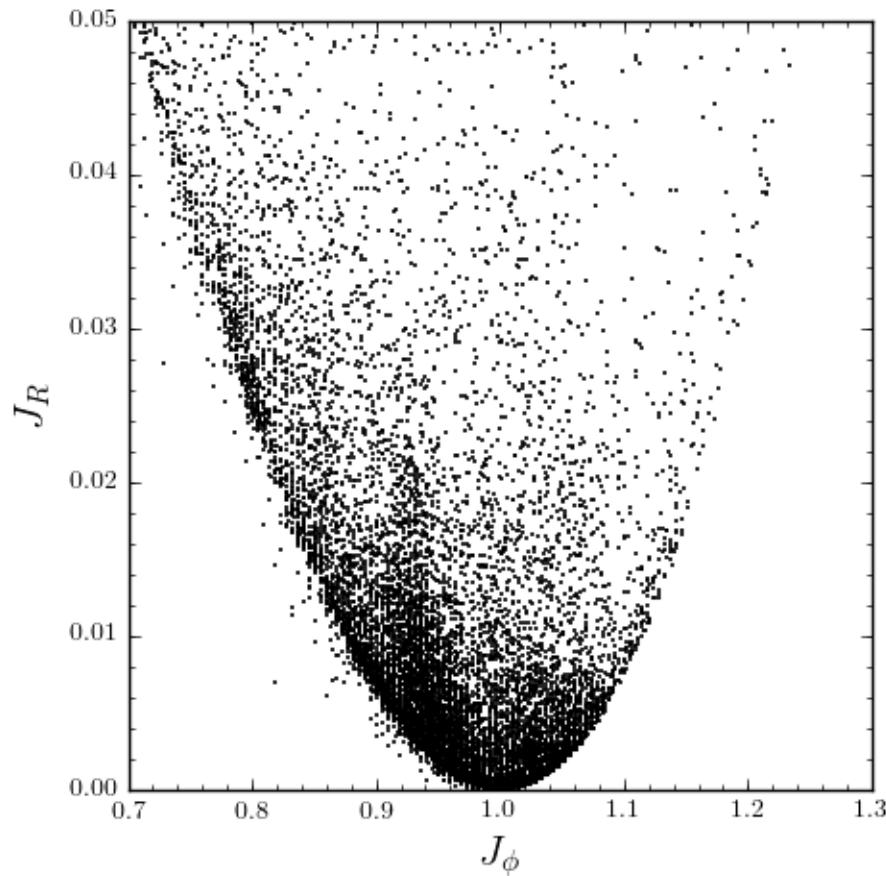
```
>>> lp= LogarithmicHaloPotential(normalize=1.)
>>> myjr[ii]= o.jr(lp)
```

etc.

Plotting the radial action versus the angular momentum

```
>>> plot.bovy_plot(myjp,myjr,'k.',ms=2.,xlabel=r'$J_{\phi}$',ylabel=r'$J_R$',xrange=[0.7,1.3],yrange=
```

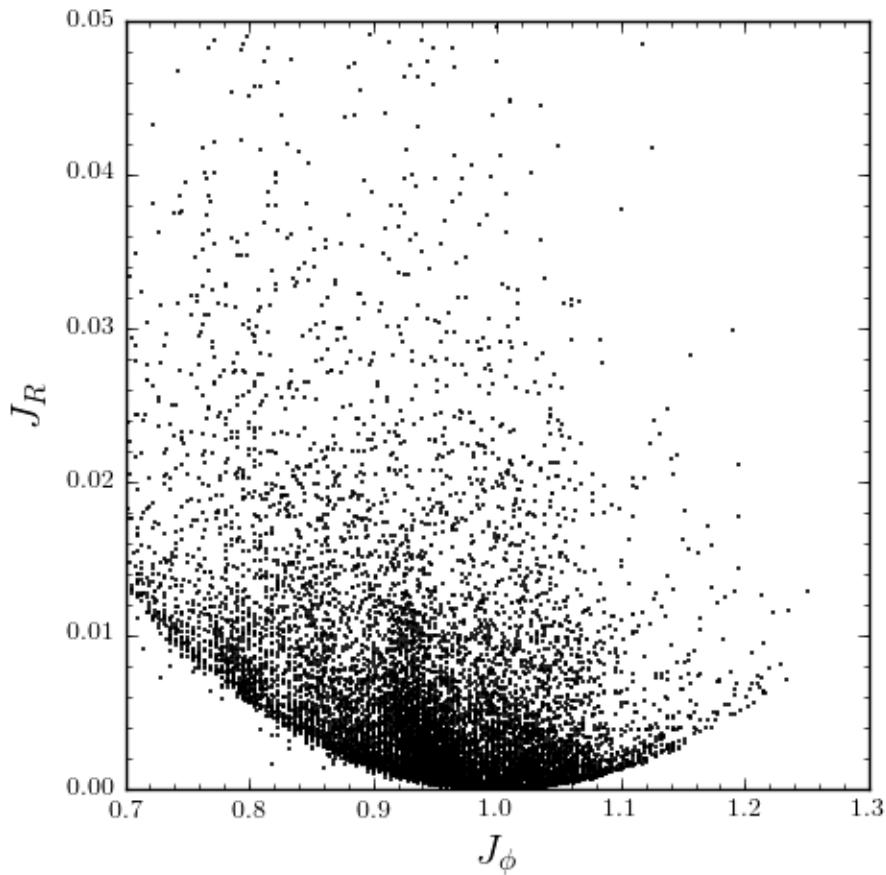
shows a feature in the distribution



If instead we use a power-law rotation curve with power-law index 1

```
>>> pp= PowerSphericalPotential(normalize=1.,alpha=-2.)
>>> myjr[ii]= o.jr(pp)
```

We find that the distribution is stretched, but the feature remains



Code for this example can be found [here](#) (note that this code uses a particular download of the GCS data set; if you use your own version, you will need to modify the part of the code that reads the data). For more information see [2010MNRAS.409..145S](#).

## 1.7 Three-dimensional disk distribution functions

galpy contains a fully three-dimensional disk distribution: `galpy.df.quasiisothermaldf`, which is an approximately isothermal distribution function expressed in terms of action-angle variables (see [2010MNRAS.401.2318B](#) and [2011MNRAS.413.1889B](#)). Recent research shows that this distribution function provides a good model for the DF of mono-abundance sub-populations (MAPs) of the Milky Way disk (see [2013MNRAS.434..652T](#) and [2013ApJ...779..115B](#)). This distribution function family requires action-angle coordinates to evaluate the DF, so `galpy.df.quasiisothermaldf` makes heavy use of the routines in `galpy.actionAngle` (in particular those in `galpy.actionAngleAdiabatic` and `galpy.actionAngle.actionAngleStaeckel`).

### 1.7.1 Setting up the DF and basic properties

The quasi-isothermal DF is defined by a gravitational potential and a set of parameters describing the radial surface-density profile and the radial and vertical velocity dispersion as a function of radius. In addition, we have to provide an instance of a `galpy.actionAngle` class to calculate the actions for a given position and velocity. For example,

for a `galpy.potential.MWPotential` potential using the adiabatic approximation for the actions, we import and define the following

```
>>> from galpy.potential import MWPotential
>>> from galpy.actionAngle import actionAngleAdiabatic
>>> from galpy.df import quasiisothermaldf
>>> aA= actionAngleAdiabatic(pot=MWPotential,c=True)
```

and then setup the `quasiisothermaldf` instance

```
>>> qdf= quasiisothermaldf(1./3.,0.2,0.1,1.,1.,pot=MWPotential,aA=aA,cutcounter=True)
```

which sets up a DF instance with a radial scale length of  $R_0/3$ , a local radial and vertical velocity dispersion of  $0.2 V_c(R_0)$  and  $0.1 V_c(R_0)$ , respectively, and a radial scale lengths of the velocity dispersions squared of  $R_0$ . `cutcounter=True` specifies that counter-rotating stars are explicitly excluded (normally these are just exponentially suppressed). As for the two-dimensional disk DFs, these parameters are merely input (or target) parameters; the true density and velocity dispersion profiles calculated by evaluating the relevant moments of the DF (see below) are not exactly exponential and have scale lengths and local normalizations that deviate slightly from these input parameters. We can estimate the DF's actual radial scale length near  $R_0$  as

```
>>> qdf.estimate_hr(1.)
0.33843243662586048
```

which is quite close to the input value of 1/3. Similarly, we can estimate the scale lengths of the dispersions squared

```
>>> qdf.estimate_hsr(1.)
1.1527209864858059
>>> qdf.estimate_hsz(1.)
1.0441867587783933
```

The vertical profile is fully specified by the velocity dispersions and radial density / dispersion profiles under the assumption of dynamical equilibrium. We can estimate the scale height of this DF at a given radius and height as follows

```
>>> qdf.estimate_hz(1.,0.125)
0.018715154050080292
```

Near the mid-plane this vertical scale height becomes very large because the vertical profile flattens, e.g.,

```
>>> qdf.estimate_hz(1.,0.125/100.)
0.85435378664432149
```

or even

```
>>> qdf.estimate_hz(1.,0.)
128674.27506772846
```

which is basically infinity.

## 1.7.2 Evaluating moments

We can evaluate various moments of the DF giving the density, mean velocities, and velocity dispersions. For example, the mean radial velocity is again everywhere zero because the potential and the DF are axisymmetric

```
>>> qdf.meanvR(1.,0.)
0.0
```

Likewise, the mean vertical velocity is everywhere zero

```
>>> qdf.meanvz(1.,0.)
0.0
```

The mean rotational velocity has a more interesting dependence on position. Near the plane, this is the same as that calculated for a similar two-dimensional disk DF (see *Evaluating moments of the DF*)

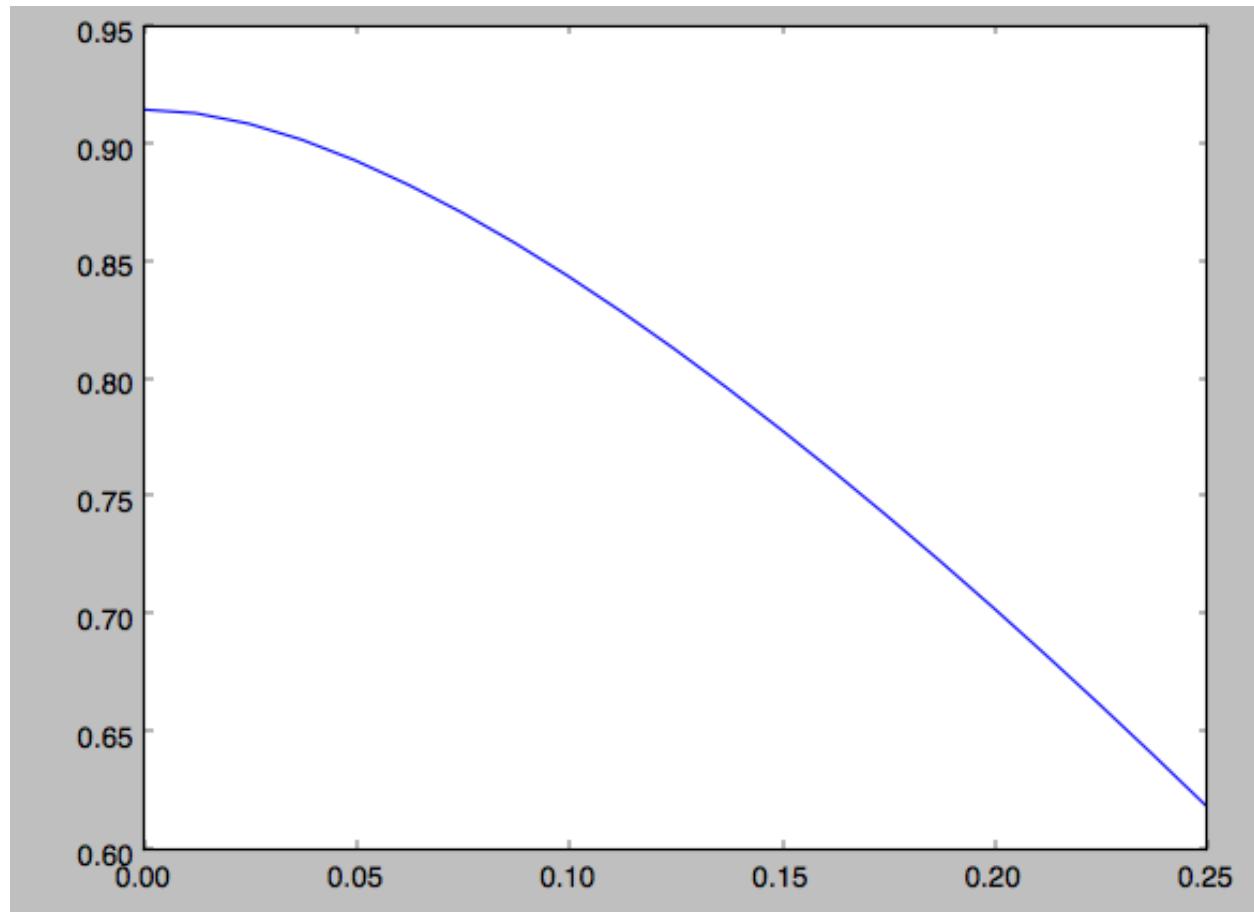
```
>>> qdf.meanvT(1.,0.)
0.9150884078276913
```

However, this value decreases as one moves further from the plane. The `quasiisothermaldf` allows us to calculate the average rotational velocity as a function of height above the plane. For example,

```
>>> zs= numpy.linspace(0.,0.25,21)
>>> mvts= numpy.array([qdf.meanvT(1.,z) for z in zs])
```

which gives

```
>>> plot(zs,mvts)
```



We can also calculate the second moments of the DF. We can check whether the radial and velocity dispersions at  $R_0$  are close to their input values

```
>>> numpy.sqrt(qdf.sigmaR2(1.,0.))
0.20918647082092351
>>> numpy.sqrt(qdf.sigmaz2(1.,0.))
0.092564222527283468
```

and they are pretty close. We can also calculate the mixed  $R$  and  $z$  moment, for example,

```
>>> qdf.sigmaRz(1.,0.125)
0.0
```

or expressed as an angle (the *tilt of the velocity ellipsoid*)

```
>>> qdf.tilt(1.,0.125)
0.0
```

This tilt is zero because we are using the adiabatic approximation. As this approximation assumes that the motions in the plane are decoupled from the vertical motions of stars, the mixed moment is zero. However, this approximation is invalid for stars that go far above the plane. By using the Staeckel approximation to calculate the actions, we can model this coupling better. Setting up a `quasiisothermaldf` instance with the Staeckel approximation

```
>>> from galpy.actionAngle import actionAngleStaeckel
>>> aAS= actionAngleStaeckel(pot=MWPotential,delta=0.55,c=True)
>>> qdfS= quasiisothermaldf(1./3.,0.2,0.1,1.,1.,pot=MWPotential,aA=aAS,cutcounter=True)
```

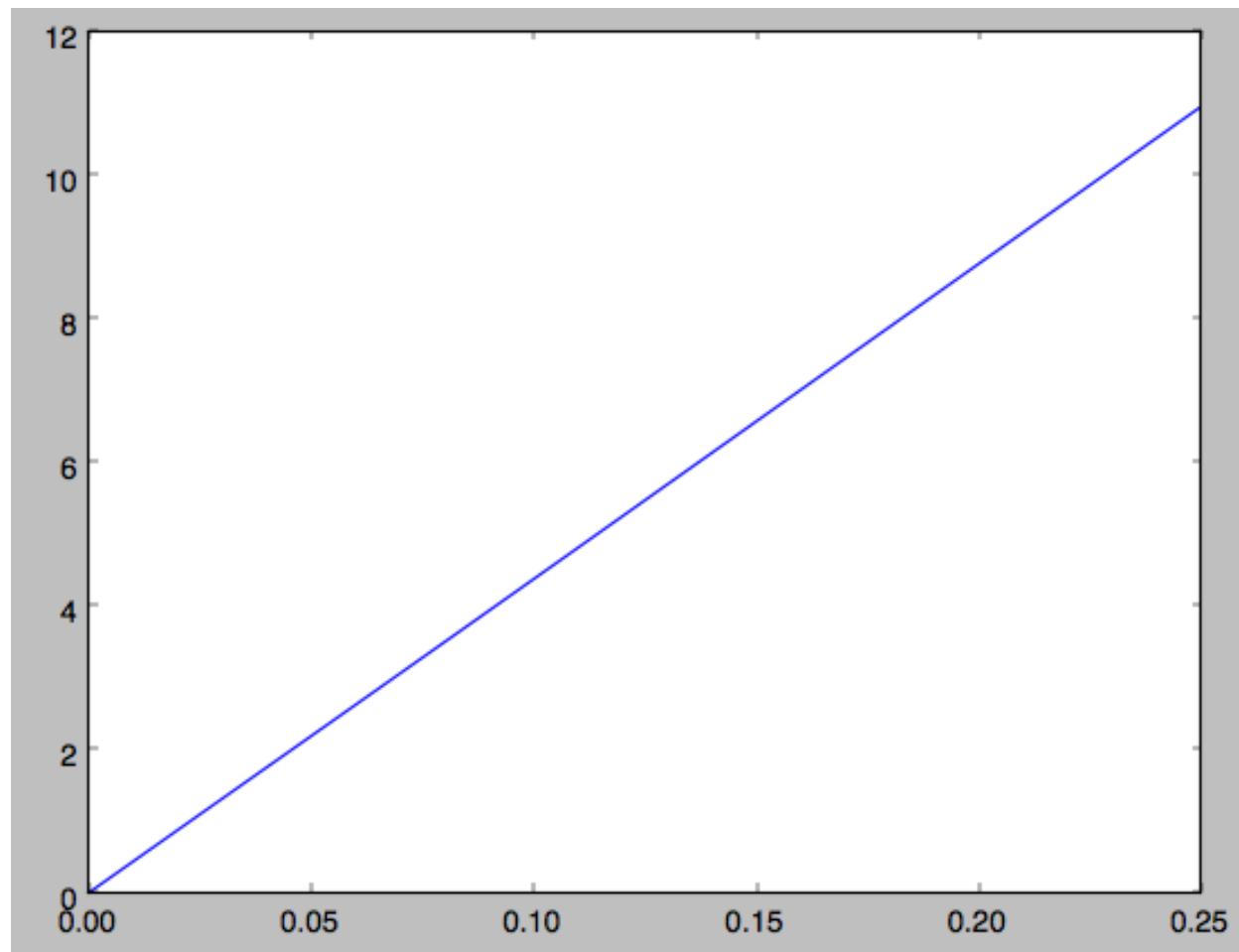
we can similarly calculate the tilt

```
>>> qdfS.tilt(1.,0.125)
5.4669442080366721
```

or about 5 degrees. As a function of height, we find

```
>>> tilts= numpy.array([qdfS.tilt(1.,z) for z in zs])
>>> plot(zs,tilts)
```

which gives



We can also calculate the density and surface density (the zero-th velocity moments). For example, the vertical density

```
>>> densz= numpy.array([qdf.density(1.,z) for z in zs])
```

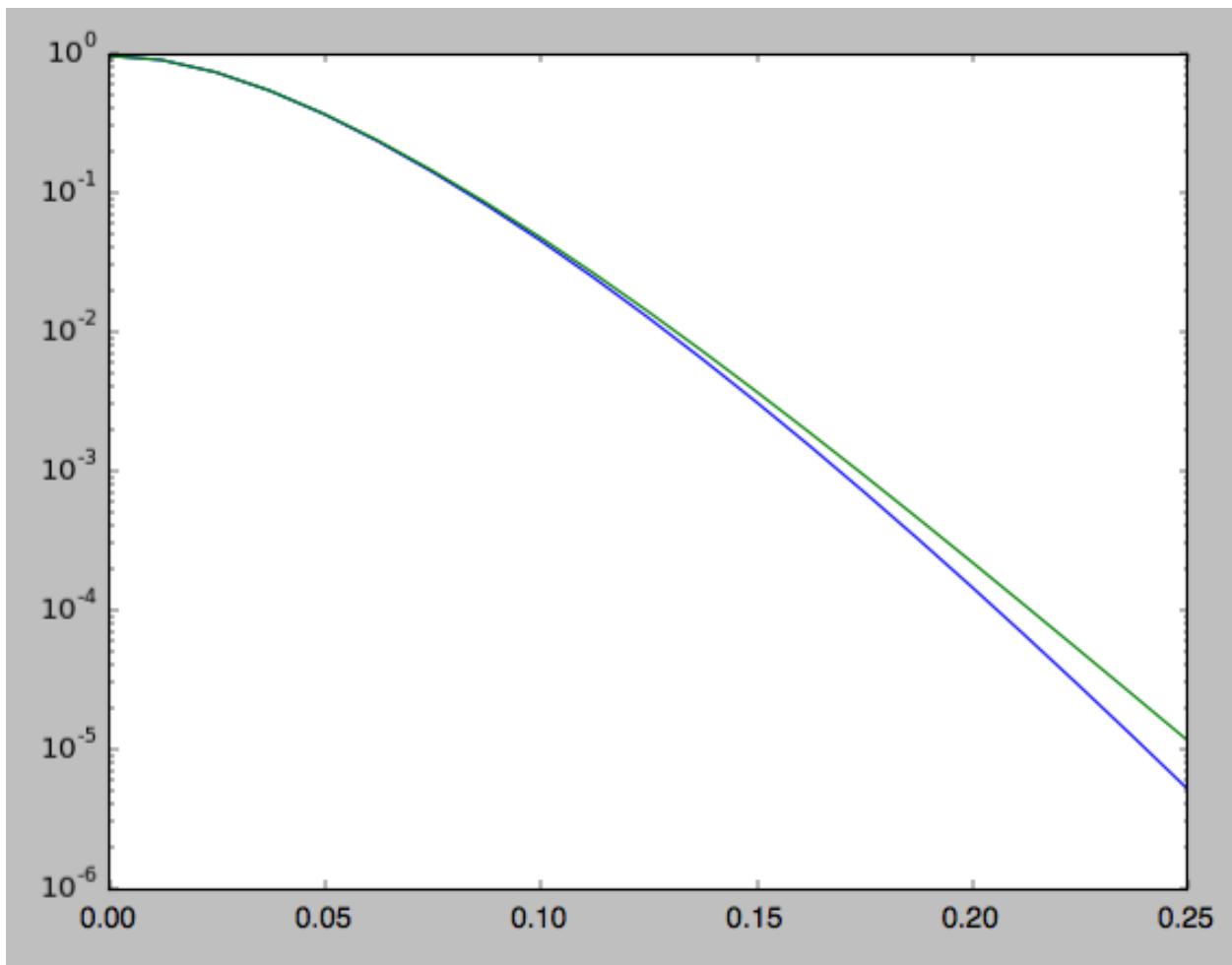
and

```
>>> denszS= numpy.array([qdfs.density(1.,z) for z in zs])
```

We can compare the vertical profiles calculated using the adiabatic and Staeckel action-angle approximations

```
>>> semilogy(zs,densz/densz[0])
>>> semilogy(zs,denszS/denszS[0])
```

which gives



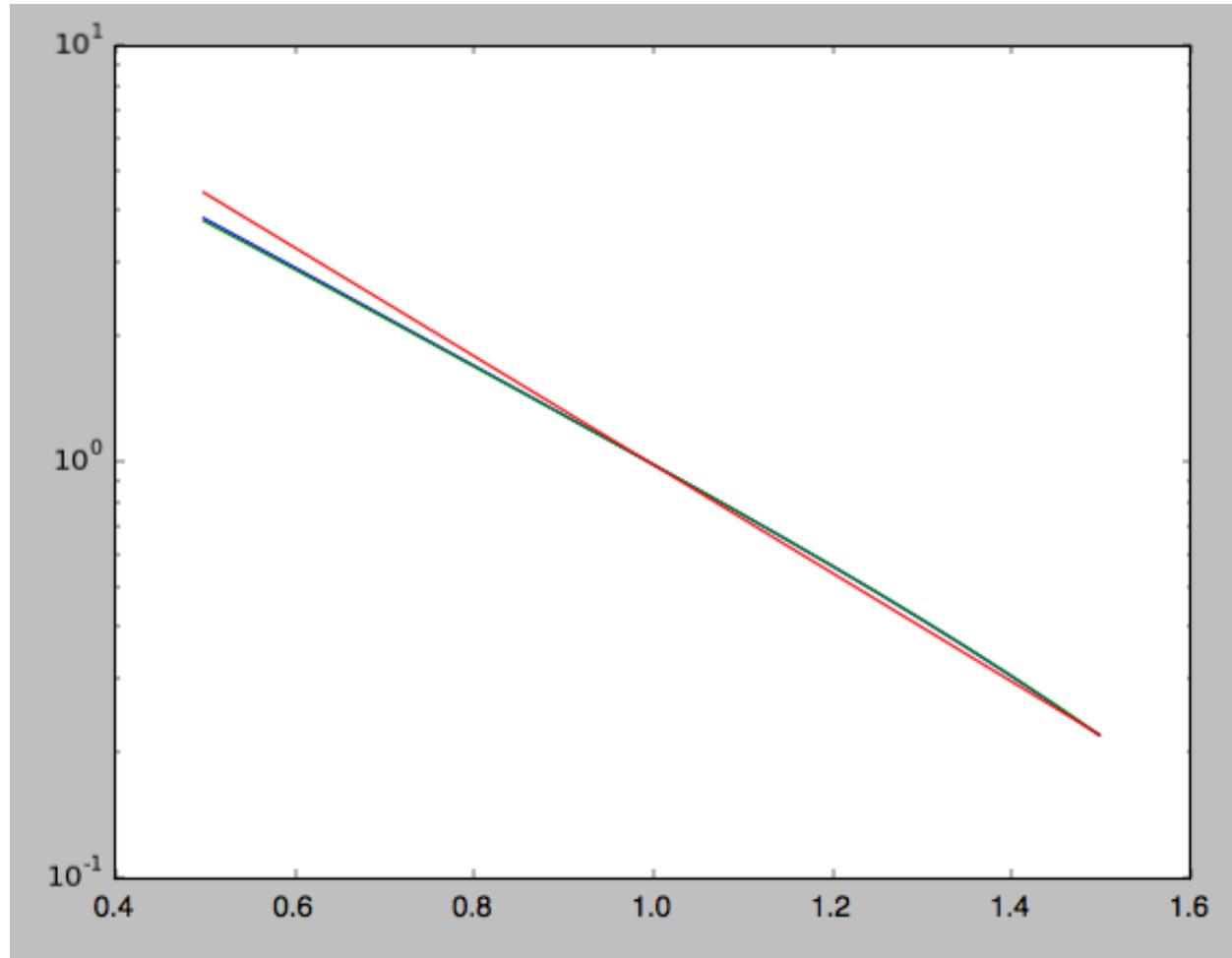
Similarly, we can calculate the radial profile of the surface density

```
>>> rs= numpy.linspace(0.5,1.5,21)
>>> surfr= numpy.array([qdf.surfacemass_z(r) for r in rs])
>>> surfrS= numpy.array([qdfS.surfacemass_z(r) for r in rs])
```

and compare them with each other and an exponential with scale length 1/3

```
>>> semilogy(rs,surfr/surfr[10])
>>> semilogy(rs,surfrS/surfrS[10])
>>> semilogy(rs,numpy.exp(-(rs-1.)/(1./3.)))
```

which gives



The two radial profiles are almost indistinguishable and are very close, if somewhat shallower, than the pure exponential profile.

General velocity moments, including all higher order moments, are implemented in `quasiisothermaldf.vmomentdensity`.

### 1.7.3 Evaluating and sampling the full probability distribution function

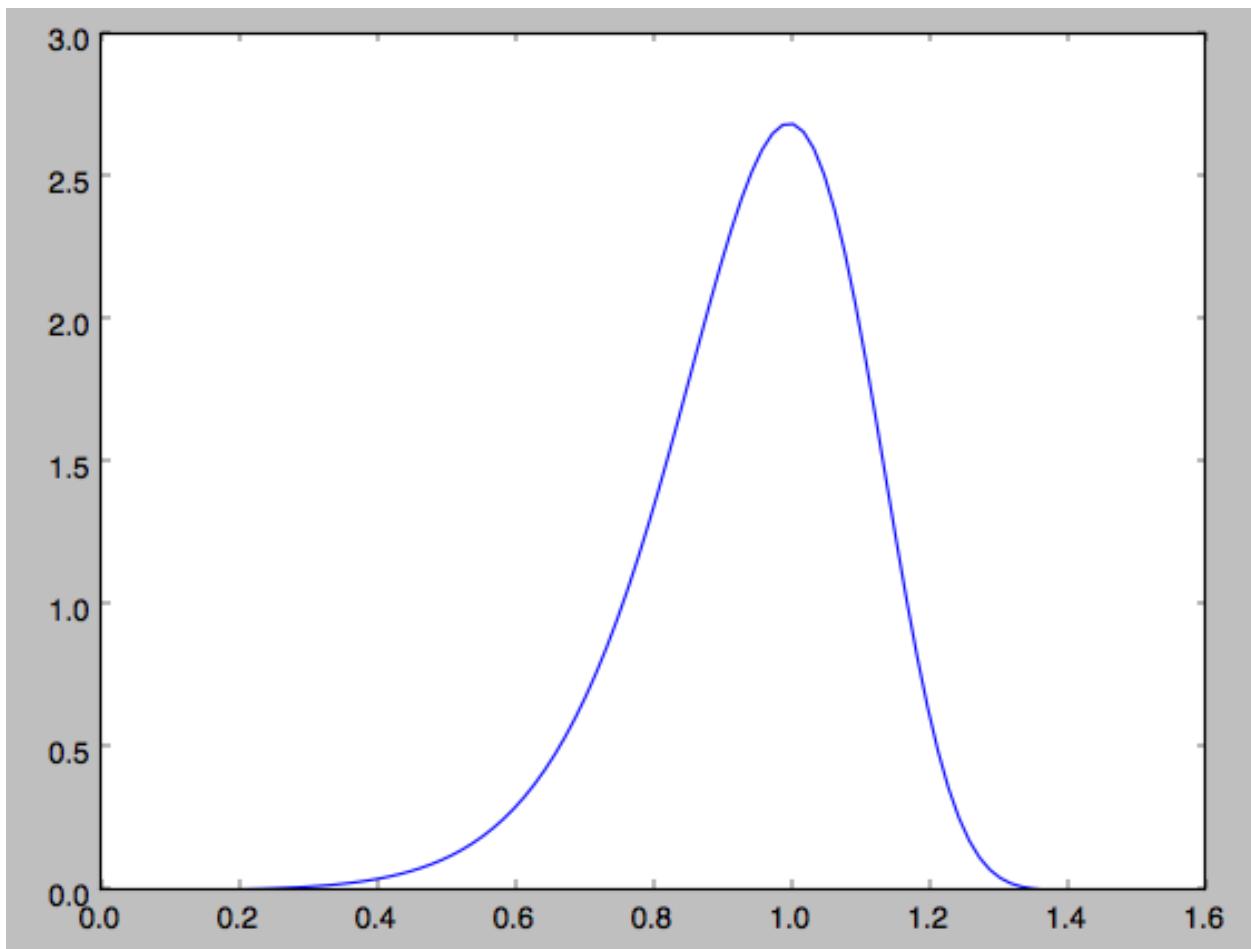
We can evaluate the distribution itself by calling the object, e.g.,

```
>>> qdf(1.,0.1,1.1,0.1,0.) #input: R,vR,vT,z,vz  
array([ 10.16445158])
```

or as a function of rotational velocity, for example in the mid-plane

```
>>> vts= numpy.linspace(0.,1.5,101)  
>>> pvt= numpy.array([qdfs(1.,0.,vt,0.,0.) for vt in vts])  
>>> plot(vts,pvt/numpy.sum(pvt)/(vts[1]-vts[0]))
```

which gives



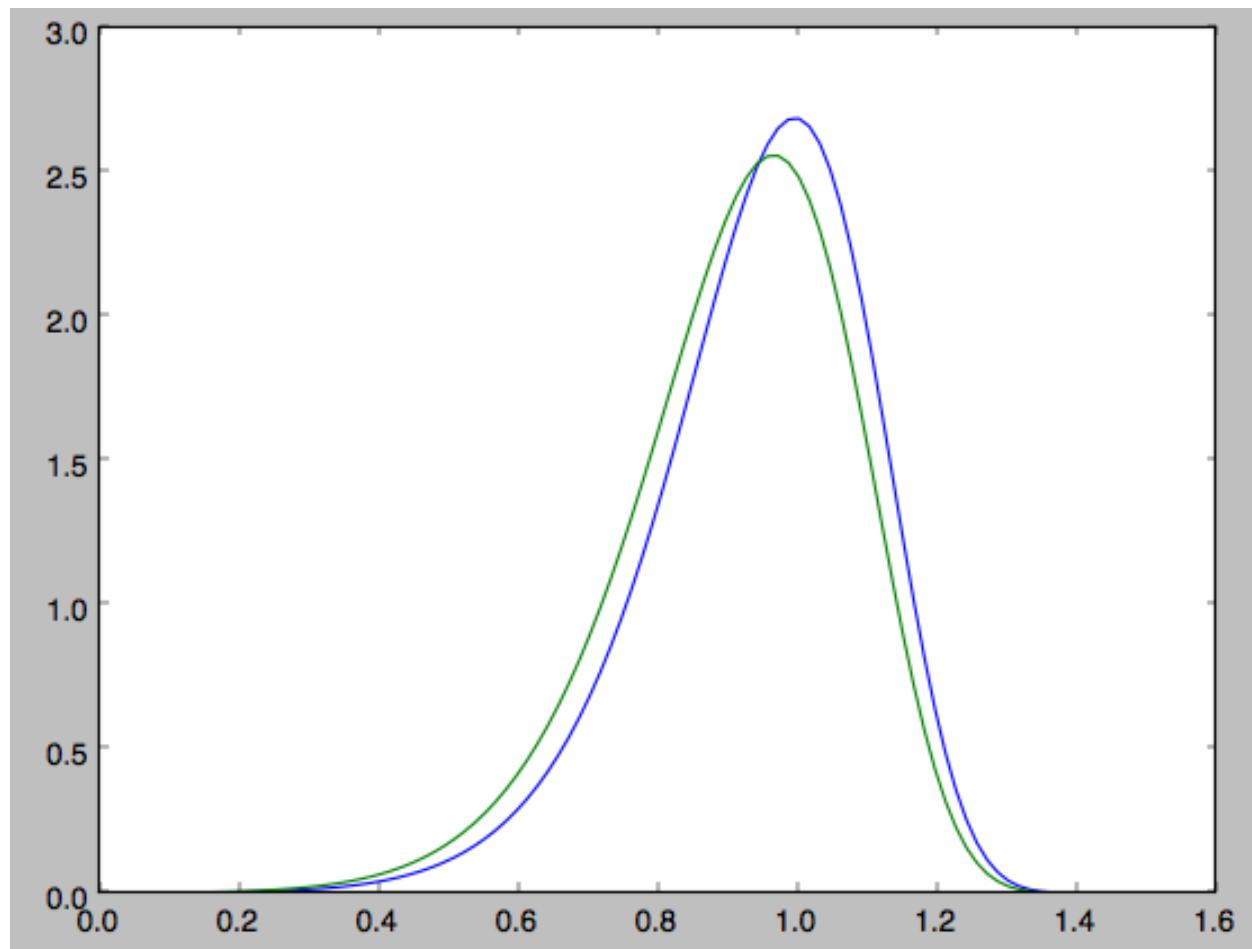
This is, however, not the true distribution of rotational velocities at  $R = 0$  and  $z = 0$ , because it is conditioned on zero radial and vertical velocities. We can calculate the distribution of rotational velocities marginalized over the radial and vertical velocities as

```
>>> qdfS.pvT(1.,1.,0.) #input vT,R,z
15.464330302557528
```

or as a function of rotational velocity

```
>>> pvt= numpy.array([qdfS.pvT(vt,1.,0.) for vt in vts])
```

overplotting this over the previous distribution gives

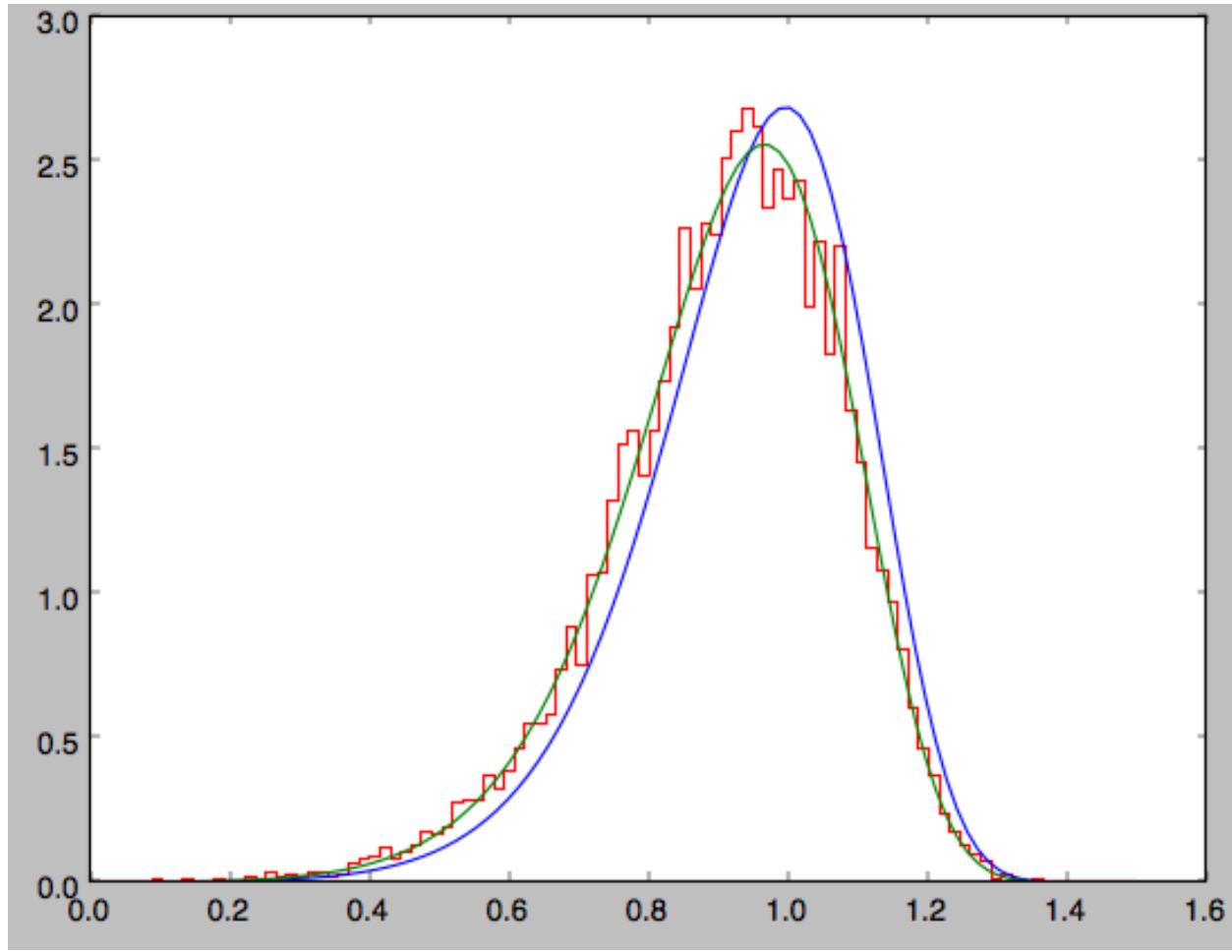


which is slightly different from the conditioned distribution. Similarly, we can calculate marginalized velocity probabilities ‘pvR, pvz, pvRvT, pvRvz, and pvTvz’. These are all multiplied with the density, such that marginalizing these over the remaining velocity component results in the density.

We can sample velocities at a given location using `quasiisothermaldf.sampleV` (there is currently no support for sampling locations from the density profile, although that is rather trivial):

```
>>> vs= qdfS.sampleV(1.,0.,n=10000)
>>> hist(vs[:,1],normed=True,histtype='step',bins=101,range=[0.,1.5])
```

gives



which shows very good agreement with the green (marginalized over  $vR$  and  $vz$ ) curve (as it should).



---

## Library reference

---

## 2.1 Orbit

### 2.1.1 Class

#### galpy.orbit.Orbit

```
class galpy.orbit.Orbit(vxvv=None, uvw=False, lb=False, radec=False, vo=235.0, ro=8.5, zo=0.025,
                        solarmotion='hogg')
```

General orbit class representing an orbit

```
__init__(vxvv=None, uvw=False, lb=False, radec=False, vo=235.0, ro=8.5, zo=0.025, solarmotion='hogg')
```

NAME:

\_\_init\_\_

PURPOSE:

Initialize an Orbit instance

INPUT:

**vxvv - initial conditions**

3D can be either

1. in Galactocentric cylindrical coordinates [R,vR,vT(z,vz,phi)]
  2. [ra,dec,d,mu\_ra, mu\_dec,vlos] in [deg,deg,kpc,mas/yr,mas/yr,km/s] (all J2000.0; mu\_ra = mu\_ra \* cos dec)
  3. [ra,dec,d,U,V,W] in [deg,deg,kpc,km/s,km/s,kms]
  4. (l,b,d,mu\_l, mu\_b, vlos) in [deg,deg,kpc,mas/yr,mas/yr,km/s] (all J2000.0; mu\_l = mu\_l \* cos b)
  5. [l,b,d,U,V,W] in [deg,deg,kpc,km/s,km/s,kms]
- 4.and 5) also work when leaving out b and mu\_b/W

OPTIONAL INPUTS:

radec - if True, input is 2) (or 3) above  
uvw - if True, velocities are UVW  
lb - if True, input is 4) or 5) above  
vo - circular velocity at ro  
ro - distance from vantage point to GC (kpc)  
zo - offset toward the NGP of the Sun wrt the plane (kpc)  
solarmotion - ‘hogg’ or ‘dehnen’, or ‘schoenrich’, or value in [-U,V,W]

OUTPUT:

instance

HISTORY:

2010-07-20 - Written - Bovy (NYU)

## 2.1.2 Methods

### galpy.orbit.Orbit.\_\_add\_\_

Orbit.\_\_add\_\_(linOrb)

NAME:

\_\_add\_\_

PURPOSE:

add a linear orbit and a planar orbit to make a 3D orbit

INPUT:

linear or plane orbit instance

OUTPUT:

3D orbit

HISTORY:

2010-07-21 - Written - Bovy (NYU)

### galpy.orbit.Orbit.\_\_call\_\_

Orbit.\_\_call\_\_(\*args, \*\*kwargs)

NAME:

\_\_call\_\_

PURPOSE:

return the orbit at time t

INPUT:

t - desired time

rect - if true, return rectangular coordinates

OUTPUT:

an Orbit instance with initial condition set to the phase-space at time t or list of Orbit instances if multiple times are given

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## galpy.orbit.Orbit.bb

Orbit.bb (\*args, \*\*kwargs)

NAME:

bb

PURPOSE:

return Galactic latitude

INPUT:

t - (optional) time at which to get bb

obs=[X,Y,Z] - (optional) position of observer (in kpc) (default=[8.5,0.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

OUTPUT:

b(t)

HISTORY:

2011-02-23 - Written - Bovy (NYU)

## galpy.orbit.Orbit.dec

Orbit.dec (\*args, \*\*kwargs)

NAME:

dec

PURPOSE:

return the declination

INPUT:

t - (optional) time at which to get dec

obs=[X,Y,Z] - (optional) position of observer (in kpc) (default=[8.5,0.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

OUTPUT:

dec(t)

HISTORY:

2011-02-23 - Written - Bovy (NYU)

## galpy.orbit.Orbit.dist

Orbit.**dist** (\*args, \*\*kwargs)

NAME:

dist

PURPOSE:

return distance from the observer

INPUT:

t - (optional) time at which to get dist

obs=[X,Y,Z] - (optional) position of observer (in kpc) (default=[8.5,0.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

OUTPUT:

dist(t) in kpc

HISTORY:

2011-02-23 - Written - Bovy (NYU)

## galpy.orbit.Orbit.E

Orbit.**E** (\*args, \*\*kwargs)

NAME:

E

PURPOSE:

calculate the energy

INPUT:

t - (optional) time at which to get the energy

pot= Potential instance or list of such instances

OUTPUT:

energy

HISTORY:

2010-09-15 - Written - Bovy (NYU)

## galpy.orbit.Orbit.e

Orbit.**e** (analytic=False, pot=None)

NAME:

e

PURPOSE:

calculate the eccentricity

INPUT:

analytic - compute this analytically

pot - potential to use for analytical calculation

OUTPUT:

eccentricity

HISTORY:

2010-09-15 - Written - Bovy (NYU)

## galpy.orbit.Orbit.ER

`Orbit.ER(*args, **kwargs)`

NAME:

ER

PURPOSE:

calculate the radial energy

INPUT:

t - (optional) time at which to get the radial energy

pot= Potential instance or list of such instances

OUTPUT:

radial energy

HISTORY:

2013-11-30 - Written - Bovy (IAS)

## galpy.orbit.Orbit.Ez

`Orbit.Ez(*args, **kwargs)`

NAME:

Ez

PURPOSE:

calculate the vertical energy

INPUT:

t - (optional) time at which to get the vertical energy

pot= Potential instance or list of such instances

OUTPUT:

vertical energy

HISTORY:

2013-11-30 - Written - Bovy (IAS)

## galpy.orbit.Orbit.integrate

Orbit.**integrate**(*t, pot, method='leapfrog\_c'*)

NAME:

integrate

PURPOSE:

integrate the orbit

INPUT:

*t* - list of times at which to output (0 has to be in this!)

*pot* - potential instance or list of instances

*method*=‘odeint’ for scipy’s odeint or ‘leapfrog’ for a simple leapfrog implementation

OUTPUT:

(none) (get the actual orbit using getOrbit())

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## galpy.orbit.Orbit.getOrbit

Orbit.**getOrbit**()

NAME:

getOrbit

PURPOSE:

return a previously calculated orbit

INPUT:

(none)

OUTPUT:

array orbit[nt,nd]

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## galpy.orbit.Orbit.helioX

Orbit.**helioX**(\*args, \*\*kwargs)

NAME:

helioX

PURPOSE:

return Heliocentric Galactic rectangular x-coordinate (aka “X”)

INPUT:

*t* - (optional) time at which to get X

**obs=[X,Y,Z] - (optional) position and velocity of observer** (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer  
ro= distance in kpc corresponding to R=1. (default: 8.5)

OUTPUT:

helioX(t)

HISTORY:

2011-02-24 - Written - Bovy (NYU)

## galpy.orbit.Orbit.helioY

Orbit.helioY(\*args, \*\*kwargs)

NAME:

helioY

PURPOSE:

return Heliocentric Galactic rectangular y-coordinate (aka “Y”)

INPUT:

t - (optional) time at which to get Y

**obs=[X,Y,Z] - (optional) position and velocity of observer** (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

OUTPUT:

helioY(t)

HISTORY:

2011-02-24 - Written - Bovy (NYU)

## galpy.orbit.Orbit.helioZ

Orbit.helioZ(\*args, \*\*kwargs)

NAME:

helioZ

PURPOSE:

return Heliocentric Galactic rectangular z-coordinate (aka “Z”)

INPUT:

t - (optional) time at which to get Z

**obs=[X,Y,Z] - (optional) position and velocity of observer** (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

OUTPUT:

helioZ(t)

HISTORY:

2011-02-24 - Written - Bovy (NYU)

### galpy.orbit.Orbit.Jacobi

Orbit.**Jacobi**(\*args, \*\*kwargs)

NAME:

Jacobi

PURPOSE:

calculate the Jacobi integral E - Omega L

INPUT:

t - (optional) time at which to get the Jacobi integral

OmegaP= pattern speed

pot= potential instance or list of such instances

OUTPUT:

Jacobi integral

HISTORY:

2011-04-18 - Written - Bovy (NYU)

### galpy.orbit.Orbit.jp

Orbit.**jp**(pot=None, \*\*kwargs)

NAME:

jp

PURPOSE:

calculate the azimuthal action

INPUT:

pot - potential

type= ('adiabatic') type of actionAngle module to use

1.'adiabatic'

2.'staeckel'

3.'isochroneApprox'

4.'spherical'

+actionAngle module setup kwargs

OUTPUT:

jp

HISTORY:

2010-11-30 - Written - Bovy (NYU)

2013-11-27 - Re-written using new actionAngle modules - Bovy (IAS)

## galpy.orbit.Orbit.jr

Orbit.**jr** (*pot=None, \*\*kwargs*)

NAME:

jr

PURPOSE:

calculate the radial action

INPUT:

pot - potential

type= ('adiabatic') type of actionAngle module to use

1.'adiabatic'

2.'staeckel'

3.'isochroneApprox'

4.'spherical'

+actionAngle module setup kwargs

OUTPUT:

jr

HISTORY:

2010-11-30 - Written - Bovy (NYU)

2013-11-27 - Re-written using new actionAngle modules - Bovy (IAS)

## galpy.orbit.Orbit.jz

Orbit.**jz** (*pot=None, \*\*kwargs*)

NAME:

jz

PURPOSE:

calculate the vertical action

INPUT:

pot - potential

type= ('adiabatic') type of actionAngle module to use

1.'adiabatic'

2.'staeckel'

3.'isochroneApprox'

4.'spherical'

+actionAngle module setup kwargs

OUTPUT:

jz

HISTORY:

2012-06-01 - Written - Bovy (IAS)  
2013-11-27 - Re-written using new actionAngle modules - Bovy (IAS)

## galpy.orbit.Orbit.ll

`Orbit.ll(*args, **kwargs)`

NAME:

ll

PURPOSE:

return Galactic longitude

INPUT:

t - (optional) time at which to get ll

obs=[X,Y,Z] - (optional) position of observer (in kpc) (default=[8.5,0.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

OUTPUT:

l(t)

HISTORY:

2011-02-23 - Written - Bovy (NYU)

## galpy.orbit.Orbit.L

`Orbit.L(*args, **kwargs)`

NAME:

L

PURPOSE:

calculate the angular momentum at time t

INPUT:

t - (optional) time at which to get the angular momentum

OUTPUT:

angular momentum

HISTORY:

2010-09-15 - Written - Bovy (NYU)

## galpy.orbit.Orbit.Op

`Orbit.Op(pot=None, **kwargs)`

NAME:

Op

**PURPOSE:**

calculate the azimuthal frequency

**INPUT:**

pot - potential

type= ('adiabatic') type of actionAngle module to use

1. 'adiabatic'
2. 'staeckel'
3. 'isochroneApprox'
4. 'spherical'

+actionAngle module setup kwargs

**OUTPUT:**

Op

**HISTORY:**

2013-11-27 - Written - Bovy (IAS)

**`galpy.orbit.Orbit.Or`**

`Orbit.Or(pot=None, **kwargs)`

**NAME:**

Or

**PURPOSE:**

calculate the radial frequency

**INPUT:**

pot - potential

type= ('adiabatic') type of actionAngle module to use

1. 'adiabatic'
2. 'staeckel'
3. 'isochroneApprox'
4. 'spherical'

+actionAngle module setup kwargs

**OUTPUT:**

Or

**HISTORY:**

2013-11-27 - Written - Bovy (IAS)

## galpy.orbit.Orbit.Oz

Orbit.**Oz** (*pot=None*, *\*\*kwargs*)

NAME:

Oz

PURPOSE:

calculate the vertical frequency

INPUT:

pot - potential

type= ('adiabatic') type of actionAngle module to use

1.'adiabatic'

2.'staeckel'

3.'isochroneApprox'

4.'spherical'

+actionAngle module setup kwargs

OUTPUT:

Oz

HISTORY:

2013-11-27 - Written - Bovy (IAS)

## galpy.orbit.Orbit.phi

Orbit.**phi** (\*args, \*\*kwargs)

NAME:

phi

PURPOSE:

return azimuth

INPUT:

t - (optional) time at which to get the azimuth

OUTPUT:

phi(t)

HISTORY:

2010-09-21 - Written - Bovy (NYU)

## galpy.orbit.Orbit.plot

Orbit.**plot** (\*args, \*\*kwargs)

NAME:

plot

**PURPOSE:**

plot a previously calculated orbit (with reasonable defaults)

**INPUT:**

d1= first dimension to plot ('x', 'y', 'R', 'vR', 'vT', 'z', 'vz', ...)

d2= second dimension to plot

matplotlib.plot inputs+bovy\_plot.plot inputs

**OUTPUT:**

sends plot to output device

**HISTORY:**

2010-07-10 - Written - Bovy (NYU)

**galpy.orbit.Orbit.plot3d**

Orbit.**plot3d**(\*args, \*\*kwargs)

**NAME:**

plot3d

**PURPOSE:**

plot 3D aspects of an Orbit

**INPUT:**

bovy\_plot3d args and kwargs

**OUTPUT:**

plot

**HISTORY:**

2010-07-26 - Written - Bovy (NYU)

2010-09-22 - Adapted to more general framework - Bovy (NYU)

2010-01-08 - Adapted to 3D - Bovy (NYU)

**galpy.orbit.Orbit.plotE**

Orbit.**plotE**(\*args, \*\*kwargs)

**NAME:**

plotE

**PURPOSE:**

plot E(.) along the orbit

**INPUT:**

pot= Potential instance or list of instances in which the orbit was integrated

d1= plot Ez vs d1: e.g., 't', 'z', 'R', 'vR', 'vT', 'vz'

+bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## galpy.orbit.Orbit.plotEz

Orbit.**plotEz** (\*args, \*\*kwargs)

NAME:

plotEz

PURPOSE:

plot E\_z(.) along the orbit

INPUT:

pot= Potential instance or list of instances in which the orbit was integrated

d1= plot Ez vs d1: e.g., 't', 'z', 'R'

+bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## galpy.orbit.Orbit.plotEzJz

Orbit.**plotEzJz** (\*args, \*\*kwargs)

NAME:

plotEzJzt

PURPOSE:

plot E\_z(t)/sqrt(dens(R)) along the orbit (an approximation to the vertical action)

INPUT:

pot - Potential instance or list of instances in which the orbit was integrated

d1= plot Ez vs d1: e.g., 't', 'z', 'R'

+bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-08-08 - Written - Bovy (NYU)

## galpy.orbit.Orbit.plotphi

Orbit.**plotphi**(\*args, \*\*kwargs)

NAME:

plotphi

PURPOSE:

plot phi(.) along the orbit

INPUT:

d1= plot vs d1: e.g., ‘t’, ‘z’, ‘R’

bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## galpy.orbit.Orbit.plotR

Orbit.**plotR**(\*args, \*\*kwargs)

NAME:

plotR

PURPOSE:

plot R(.) along the orbit

INPUT:

d1= plot vs d1: e.g., ‘t’, ‘z’, ‘R’

bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## galpy.orbit.Orbit.plotvR

Orbit.**plotvR**(\*args, \*\*kwargs)

NAME:

plotvR

PURPOSE:

plot vR(.) along the orbit

INPUT:

d1= plot vs d1: e.g., ‘t’, ‘z’, ‘R’  
bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-10 - Written - Bovy (NYU)

### galpy.orbit.Orbit.plotvT

Orbit.**plotvT**(\*args, \*\*kwargs)

NAME:

plotvT

PURPOSE:

plot vT(.) along the orbit

INPUT:

d1= plot vs d1: e.g., ‘t’, ‘z’, ‘R’  
bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-10 - Written - Bovy (NYU)

### galpy.orbit.Orbit.plotvx

Orbit.**plotvx**(\*args, \*\*kwargs)

NAME:

plotvx

PURPOSE:

plot vx(.) along the orbit

INPUT:

d1= plot vs d1: e.g., ‘t’, ‘z’, ‘R’  
bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-21 - Written - Bovy (NYU)

## galpy.orbit.Orbit.plotvy

Orbit.**plotvy**(\*args, \*\*kwargs)

NAME:

plotvy

PURPOSE:

plot vy(.) along the orbit

INPUT:

d1= plot vs d1: e.g., ‘t’, ‘z’, ‘R’

bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-21 - Written - Bovy (NYU)

## galpy.orbit.Orbit.plotvz

Orbit.**plotvz**(\*args, \*\*kwargs)

NAME:

plotvz

PURPOSE:

plot vz(.) along the orbit

INPUT: d1= plot vs d1: e.g., ‘t’, ‘z’, ‘R’

bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## galpy.orbit.Orbit.plotx

Orbit.**plotx**(\*args, \*\*kwargs)

NAME:

plotx

PURPOSE:

plot x(.) along the orbit

INPUT:

d1= plot vs d1: e.g., ‘t’, ‘z’, ‘R’

bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-21 - Written - Bovy (NYU)

## galpy.orbit.Orbit.ploty

Orbit.**ploty**(\*args, \*\*kwargs)

NAME:

ploty

PURPOSE:

plot y(.) along the orbit

INPUT:

d1= plot vs d1: e.g., ‘t’, ‘z’, ‘R’

bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-21 - Written - Bovy (NYU)

## galpy.orbit.Orbit.plotz

Orbit.**plotz**(\*args, \*\*kwargs)

NAME:

plotz

PURPOSE:

plot z(.) along the orbit

INPUT:

d1= plot vs d1: e.g., ‘t’, ‘z’, ‘R’

bovy\_plot.bovy\_plot inputs

OUTPUT:

figure to output device

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## galpy.orbit.Orbit.pmbb

Orbit.**pmbb**(\*args, \*\*kwargs)

NAME:

pmbb

**PURPOSE:**

return proper motion in Galactic latitude (in mas/yr)

**INPUT:**

t - (optional) time at which to get pmhb

**obs=[X,Y,Z,vx,vy,vz] - (optional) position and velocity of observer** (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

**OUTPUT:**

pm\_b(t)

**HISTORY:**

2011-02-24 - Written - Bovy (NYU)

**galpy.orbit.Orbit.pmdc**

Orbit.pmdc (\*args, \*\*kwargs)

**NAME:**

pmdc

**PURPOSE:**

return proper motion in declination (in mas/yr)

**INPUT:**

t - (optional) time at which to get pmdc

**obs=[X,Y,Z,vx,vy,vz] - (optional) position and velocity of observer** (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

**OUTPUT:**

pm\_dec(t)

**HISTORY:**

2011-02-24 - Written - Bovy (NYU)

**galpy.orbit.Orbit.pmll**

Orbit.pmll (\*args, \*\*kwargs)

**NAME:**

pmll

**PURPOSE:**

return proper motion in Galactic longitude (in mas/yr)

**INPUT:**

t - (optional) time at which to get pmll

**obs=[X,Y,Z,vx,vy,vz]** - (optional) position and velocity of observer (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

OUTPUT:

pm\_ll(t)

HISTORY:

2011-02-24 - Written - Bovy (NYU)

### galpy.orbit.Orbit.pmra

Orbit.pmra (\*args, \*\*kwargs)

NAME:

pmra

PURPOSE:

return proper motion in right ascension (in mas/yr)

INPUT:

t - (optional) time at which to get pmra

**obs=[X,Y,Z,vx,vy,vz]** - (optional) position and velocity of observer (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

OUTPUT:

pm\_ra(t)

HISTORY:

2011-02-24 - Written - Bovy (NYU)

### galpy.orbit.Orbit.R

Orbit.R (\*args, \*\*kwargs)

NAME:

R

PURPOSE:

return cylindrical radius at time t

INPUT:

t - (optional) time at which to get the radius

OUTPUT:

R(t)

**HISTORY:**

2010-09-21 - Written - Bovy (NYU)

**galpy.orbit.Orbit.ra**

`Orbit.ra (*args, **kwargs)`

**NAME:**

ra

**PURPOSE:**

return the right ascension

**INPUT:**

t - (optional) time at which to get ra

obs=[X,Y,Z] - (optional) position of observer (in kpc) (default=[8.5,0.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

**OUTPUT:**

ra(t)

**HISTORY:**

2011-02-23 - Written - Bovy (NYU)

**galpy.orbit.Orbit.rap**

`Orbit.rap (analytic=False, pot=None)`

**NAME:**

rap

**PURPOSE:**

calculate the apocenter radius

**INPUT:**

analytic - compute this analytically

pot - potential to use for analytical calculation

**OUTPUT:**

R\_ap

**HISTORY:**

2010-09-20 - Written - Bovy (NYU)

**galpy.orbit.Orbit.resetA**

`Orbit.resetA (pot=None, type=None)`

**NAME:**

resetA

PURPOSE:

re-set up an actionAngle module for this Orbit

INPUT:

(none)

OUTPUT:

True if reset happened, False otherwise

HISTORY:

2014-01-06 - Written - Bovy (IAS)

## galpy.orbit.Orbit.rperi

Orbit.**rperi** (*analytic=False, pot=None*)

NAME:

rperi

PURPOSE:

calculate the pericenter radius

INPUT:

analytic - compute this analytically

pot - potential to use for analytical calculation

OUTPUT:

R\_peri

HISTORY:

2010-09-20 - Written - Bovy (NYU)

## galpy.orbit.Orbit.setphi

Orbit.**setphi** (*phi*)

NAME:

setphi

PURPOSE:

set initial azimuth

INPUT:

phi - desired azimuth

OUTPUT:

(none)

HISTORY:

2010-08-01 - Written - Bovy (NYU)

BUGS:

Should perform check that this orbit has phi

### galpy.orbit.Orbit.toLinear

Orbit.**toLinear**()

NAME:

toLinear

PURPOSE:

convert a 3D orbit into a 1D orbit (z)

INPUT:

(none)

OUTPUT:

linear Orbit

HISTORY:

2010-11-30 - Written - Bovy (NYU)

### galpy.orbit.Orbit.toPlanar

Orbit.**toPlanar**()

NAME:

toPlanar

PURPOSE:

convert a 3D orbit into a 2D orbit

INPUT:

(none)

OUTPUT:

planar Orbit

HISTORY:

2010-11-30 - Written - Bovy (NYU)

### galpy.orbit.Orbit.Tp

Orbit.**Tp**(pot=None, \*\*kwargs)

NAME:

Tp

PURPOSE:

calculate the azimuthal period

INPUT:

pot - potential

type= ('adiabatic') type of actionAngle module to use

1.‘adiabatic’  
2.‘staeckel’  
3.‘isochroneApprox’  
4.‘spherical’  
+actionAngle module setup kwargs

OUTPUT:

Tp

HISTORY:

2010-11-30 - Written - Bovy (NYU)  
2013-11-27 - Re-written using new actionAngle modules - Bovy (IAS)

## galpy.orbit.Orbit.Tr

Orbit.Tr(*pot=None, \*\*kwargs*)

NAME:

Tr

PURPOSE:

calculate the radial period

INPUT:

pot - potential  
type= (‘adiabatic’) type of actionAngle module to use  
1.‘adiabatic’  
2.‘staeckel’  
3.‘isochroneApprox’  
4.‘spherical’  
+actionAngle module setup kwargs

OUTPUT:

Tr

HISTORY:

2010-11-30 - Written - Bovy (NYU)  
2013-11-27 - Re-written using new actionAngle modules - Bovy (IAS)

## galpy.orbit.Orbit.TrTp

Orbit.TrTp(*pot=None, \*\*kwargs*)

NAME:

TrTp

PURPOSE:

the ‘ratio’ between the radial and azimuthal period  $T_r/T_\phi \cdot \pi$

INPUT:

pot - potential

type= (‘adiabatic’) type of actionAngle module to use

1.‘adiabatic’

2.‘staeckel’

3.‘isochroneApprox’

4.‘spherical’

+actionAngle module setup kwargs

OUTPUT:

$T_r/T_\phi \cdot \pi$

HISTORY:

2010-11-30 - Written - Bovy (NYU)

2013-11-27 - Re-written using new actionAngle modules - Bovy (IAS)

## galpy.orbit.Orbit.Tz

Orbit.Tz (*pot=None, \*\*kwargs*)

NAME:

Tz

PURPOSE:

calculate the vertical period

INPUT:

pot - potential

type= (‘adiabatic’) type of actionAngle module to use

1.‘adiabatic’

2.‘staeckel’

3.‘isochroneApprox’

4.‘spherical’

+actionAngle module setup kwargs

OUTPUT:

Tz

HISTORY:

2012-06-01 - Written - Bovy (IAS)

2013-11-27 - Re-written using new actionAngle modules - Bovy (IAS)

## galpy.orbit.Orbit.U

Orbit.**U**(\*args, \*\*kwargs)

NAME:

U

PURPOSE:

return Heliocentric Galactic rectangular x-velocity (aka “U”)

INPUT:

t - (optional) time at which to get U

**obs=[X,Y,Z,vx,vy,vz]** - (optional) position and velocity of observer (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

OUTPUT:

U(t)

HISTORY:

2011-02-24 - Written - Bovy (NYU)

## galpy.orbit.Orbit.V

Orbit.**V**(\*args, \*\*kwargs)

NAME:

V

PURPOSE:

return Heliocentric Galactic rectangular y-velocity (aka “V”)

INPUT:

t - (optional) time at which to get U

**obs=[X,Y,Z,vx,vy,vz]** - (optional) position and velocity of observer (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

OUTPUT:

V(t)

HISTORY:

2011-02-24 - Written - Bovy (NYU)

## galpy.orbit.Orbit.vbb

Orbit.**vbb** (\*args, \*\*kwargs)

NAME:

vbb

PURPOSE:

return velocity in Galactic latitude (km/s)

INPUT:

t - (optional) time at which to get vbb

**obs=[X,Y,Z,vx,vy,vz]** - (optional) position and velocity of observer (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

OUTPUT:

v\_b(t) in km/s

HISTORY:

2011-02-24 - Written - Bovy (NYU)

## galpy.orbit.Orbit.vdec

Orbit.**vdec** (\*args, \*\*kwargs)

NAME:

vdec

PURPOSE:

return velocity in declination (km/s)

INPUT:

t - (optional) time at which to get vdec

**obs=[X,Y,Z,vx,vy,vz]** - (optional) position and velocity of observer (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

OUTPUT:

v\_dec(t) in km/s

HISTORY:

2011-03-27 - Written - Bovy (NYU)

## galpy.orbit.Orbit.vll

Orbit.**vll**(\*args, \*\*kwargs)

NAME:

vll

PURPOSE:

return the velocity in Galactic longitude (km/s)

INPUT:

t - (optional) time at which to get vll

**obs=[X,Y,Z,vx,vy,vz]** - (optional) position and velocity of observer (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

OUTPUT:

v\_l(t) in km/s

HISTORY:

2011-03-27 - Written - Bovy (NYU)

## galpy.orbit.Orbit.vlos

Orbit.**vlos**(\*args, \*\*kwargs)

NAME:

vlos

PURPOSE:

return the line-of-sight velocity (in km/s)

INPUT:

t - (optional) time at which to get vlos

**obs=[X,Y,Z,vx,vy,vz]** - (optional) position and velocity of observer (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

OUTPUT:

vlos(t)

HISTORY:

2011-02-24 - Written - Bovy (NYU)

## galpy.orbit.Orbit.vphi

Orbit.**vphi**(\*args, \*\*kwargs)

NAME:

vphi

PURPOSE:

return angular velocity

INPUT:

t - (optional) time at which to get the angular velocity

OUTPUT:

vphi(t)

HISTORY:

2010-09-21 - Written - Bovy (NYU)

## galpy.orbit.Orbit.vR

Orbit.**vR**(\*args, \*\*kwargs)

NAME:

vR

PURPOSE:

return radial velocity at time t

INPUT:

t - (optional) time at which to get the radial velocity

OUTPUT:

vR(t)

HISTORY:

2010-09-21 - Written - Bovy (NYU)

## galpy.orbit.Orbit.vra

Orbit.**vra**(\*args, \*\*kwargs)

NAME:

vra

PURPOSE:

return velocity in right ascension (km/s)

INPUT:

t - (optional) time at which to get vra

**obs=[X,Y,Z,vx,vy,vz]** - (optional) position and velocity of observer (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

ro= distance in kpc corresponding to R=1. (default: 8.5)

vo= velocity in km/s corresponding to v=1. (default: 235.)

OUTPUT:

v\_ra(t) in km/s

HISTORY:

2011-03-27 - Written - Bovy (NYU)

## galpy.orbit.Orbit.vT

Orbit.vT(\*args, \*\*kwargs)

NAME:

vT

PURPOSE:

return tangential velocity at time t

INPUT:

t - (optional) time at which to get the tangential velocity

OUTPUT:

vT(t)

HISTORY:

2010-09-21 - Written - Bovy (NYU)

## galpy.orbit.Orbit.vx

Orbit.vx(\*args, \*\*kwargs)

NAME:

vx

PURPOSE:

return x velocity at time t

INPUT:

t - (optional) time at which to get the velocity

OUTPUT:

vx(t)

HISTORY:

2010-11-30 - Written - Bovy (NYU)

## galpy.orbit.Orbit.vy

Orbit.vy(\*args, \*\*kwargs)

NAME:

vy

**PURPOSE:**

return y velocity at time t

**INPUT:**

t - (optional) time at which to get the velocity

**OUTPUT:**

$v_y(t)$

**HISTORY:**

2010-11-30 - Written - Bovy (NYU)

**galpy.orbit.Orbit.vz**

`Orbit.vz(*args, **kwargs)`

**NAME:**

`vz`

**PURPOSE:**

return vertical velocity

**INPUT:**

t - (optional) time at which to get the vertical velocity

**OUTPUT:**

$v_z(t)$

**HISTORY:**

2010-09-21 - Written - Bovy (NYU)

**galpy.orbit.Orbit.W**

`Orbit.W(*args, **kwargs)`

**NAME:**

`W`

**PURPOSE:**

return Heliocentric Galactic rectangular z-velocity (aka “W”)

**INPUT:**

t - (optional) time at which to get W

**obs=[X,Y,Z,vx,vy,vz]** - (optional) position and velocity of observer (in kpc and km/s) (default=[8.5,0.,0.,0.,235.,0.]) OR Orbit object that corresponds to the orbit of the observer

$r_o$ = distance in kpc corresponding to R=1. (default: 8.5)

$v_o$ = velocity in km/s corresponding to v=1. (default: 235.)

**OUTPUT:**

$W(t)$

**HISTORY:**

2011-02-24 - Written - Bovy (NYU)

## galpy.orbit.Orbit.wp

`Orbit.wp (pot=None, **kwargs)`

NAME:

wp

PURPOSE:

calculate the azimuthal angle

INPUT:

pot - potential

type= ('adiabatic') type of actionAngle module to use

1.'adiabatic'

2.'staeckel'

3.'isochroneApprox'

4.'spherical'

+actionAngle module setup kwargs

OUTPUT:

wp

HISTORY:

2010-11-30 - Written - Bovy (NYU)

2013-11-27 - Re-written using new actionAngle modules - Bovy (IAS)

## galpy.orbit.Orbit.wr

`Orbit.wr (pot=None, **kwargs)`

NAME:

wr

PURPOSE:

calculate the radial angle

INPUT:

pot - potential

type= ('adiabatic') type of actionAngle module to use

1.'adiabatic'

2.'staeckel'

3.'isochroneApprox'

4.'spherical'

+actionAngle module setup kwargs

OUTPUT:

wr

HISTORY:

2010-11-30 - Written - Bovy (NYU)

2013-11-27 - Re-written using new actionAngle modules - Bovy (IAS)

## galpy.orbit.Orbit.wz

Orbit.wz (*pot=None*, *\*\*kwargs*)

NAME:

wz

PURPOSE:

calculate the vertical angle

INPUT:

pot - potential

type= ('adiabatic') type of actionAngle module to use

1. 'adiabatic'
2. 'staeckel'
3. 'isochroneApprox'
4. 'spherical'

+actionAngle module setup kwargs

OUTPUT:

wz

HISTORY:

2012-06-01 - Written - Bovy (IAS)

2013-11-27 - Re-written using new actionAngle modules - Bovy (IAS)

## galpy.orbit.Orbit.x

Orbit.x (\*args, \*\*kwargs)

NAME:

x

PURPOSE:

return x

INPUT:

t - (optional) time at which to get x

OUTPUT:

x(t)

HISTORY:

2010-09-21 - Written - Bovy (NYU)

### galpy.orbit.Orbit.y

Orbit.y (\*args, \*\*kwargs)

NAME:

y

PURPOSE:

return y

INPUT:

t - (optional) time at which to get y

OUTPUT:

y(t)

HISTORY:

2010-09-21 - Written - Bovy (NYU)

### galpy.orbit.Orbit.z

Orbit.z (\*args, \*\*kwargs)

NAME:

z

PURPOSE:

return vertical height

INPUT:

t - (optional) time at which to get the vertical height

OUTPUT:

z(t)

HISTORY:

2010-09-21 - Written - Bovy (NYU)

### galpy.orbit.Orbit.zmax

Orbit.zmax (analytic=False, pot=None)

NAME:

zmax

PURPOSE:

calculate the maximum vertical height

INPUT:

analytic - compute this analytically  
pot - potential to use for analytical calculation

OUTPUT:

Z\_max

HISTORY:

2010-09-20 - Written - Bovy (NYU)

## 2.2 Potential

### 2.2.1 3D potentials

#### General instance routines

Use as Potential-instance.method(...)

##### galpy.potential.Potential.\_\_call\_\_

Potential.\_\_call\_\_(R, z, phi=0.0, t=0.0, dR=0, dphi=0)

**NAME:** \_\_call\_\_

**PURPOSE:** evaluate the potential at (R,z,phi,t)

**INPUT:** R - Cylindrical Galactocentric radius

z - vertical height

phi - azimuth (optional)

t - time (optional)

dR=dphi=, if set to non-zero integers, return the dR, dphi't derivative instead

**OUTPUT:** Phi(R,z,t)

**HISTORY:** 2010-04-16 - Written - Bovy (NYU)

##### galpy.potential.Potential.dens

Potential.dens(R, z, phi=0.0, t=0.0, forcepoisson=False)

**NAME:**

dens

**PURPOSE:**

evaluate the density rho(R,z,t)

**INPUT:**

R - Cylindrical Galactocentric radius

z - vertical height

phi - azimuth (optional)

t - time (optional)

KEYWORDS:

forcepoisson= if True, calculate the density through the Poisson equation, even if an explicit expression for the density exists

OUTPUT:

rho (R,z,phi,t)

HISTORY:

2010-08-08 - Written - Bovy (NYU)

## galpy.potential.Potential.dvcircdR

Potential.**dvcircdR**(*R*)

NAME:

dvcircdR

PURPOSE:

calculate the derivative of the circular velocity at R wrt R in this potential

INPUT:

R - Galactocentric radius

OUTPUT:

derivative of the circular rotation velocity wrt R

HISTORY:

2013-01-08 - Written - Bovy (IAS)

## galpy.potential.Potential.epifreq

Potential.**epifreq**(*R*)

NAME:

epifreq

PURPOSE:

calculate the epicycle frequency at R in this potential

INPUT:

R - Galactocentric radius

OUTPUT:

epicycle frequency

HISTORY:

2011-10-09 - Written - Bovy (IAS)

## galpy.potential.Potential.flattening

Potential.**flattening**(*R*, *z*)

NAME:

flattening

PURPOSE:

calculate the potential flattening, defined as  $\sqrt{|\mathbf{z}/\mathbf{R} \cdot \mathbf{F}_R / \mathbf{F}_z|}$

INPUT:

*R* - Galactocentric radius

*z* - height

OUTPUT:

flattening

HISTORY:

2012-09-13 - Written - Bovy (IAS)

## galpy.potential.Potential.lindbladR

Potential.**lindbladR**(*OmegaP*, *m*=2, \*\**kwargs*)

NAME:

lindbladR

PURPOSE:

calculate the radius of a Lindblad resonance

INPUT:

*OmegaP* - pattern speed

**m= order of the resonance (as in m(O-Op)=kappa (negative m for outer) use m='corotation'**  
for corotation +scipy.optimize.brentq xtol,rtol,maxiter kwargs

OUTPUT:

radius of Linblad resonance, None if there is no resonance

HISTORY:

2011-10-09 - Written - Bovy (IAS)

## galpy.potential.Potential.omegac

Potential.**omegac**(*R*)

NAME:

omegac

PURPOSE:

calculate the circular angular speed at *R* in this potential

INPUT:

R - Galactocentric radius

OUTPUT:

circular angular speed

HISTORY:

2011-10-09 - Written - Bovy (IAS)

### **galpy.potential.Potential.phiforce**

Potential.**phiforce** ( $R, z, phi=0.0, t=0.0$ )

NAME:

phiforce

PURPOSE:

evaluate the azimuthal force  $F_{\phi}$  ( $R, z, \phi, t$ )

INPUT:

R - Cylindrical Galactocentric radius

z - vertical height

phi - azimuth (rad)

t - time (optional)

OUTPUT:

$F_{\phi}$  ( $R, z, \phi, t$ )

HISTORY:

2010-07-10 - Written - Bovy (NYU)

### **galpy.potential.Potential.phi2deriv**

Potential.**phi2deriv** ( $R, Z, phi=0.0, t=0.0$ )

NAME:

phi2deriv

PURPOSE:

evaluate the second azimuthal derivative

INPUT:

R - Galactocentric radius

Z - vertical height

phi - Galactocentric azimuth

t - time

OUTPUT:

$d^2\phi/d\phi^2$

HISTORY:

2013-09-24 - Written - Bovy (IAS)

### galpy.potential.Potential.plot

Potential.**plot** (*t=0.0, rmin=0.0, rmax=1.5, nrs=21, zmin=-0.5, zmax=0.5, nzs=21, ncontours=21, savefilename=None*)

**NAME:**

plot

**PURPOSE:**

plot the potential

**INPUT:**

*t* - time tp plot potential at

*rmin* - minimum R

*rmax* - maximum R

*nrs* - grid in R

*zmin* - minimum z

*zmax* - maximum z

*nzs* - grid in z

*ncontours* - number of contours

*savefilename* - save to or restore from this savefile (pickle)

**OUTPUT:**

plot to output device

**HISTORY:**

2010-07-09 - Written - Bovy (NYU)

### galpy.potential.Potential.plotDensity

Potential.**plotDensity** (*rmin=0.0, rmax=1.5, nrs=21, zmin=-0.5, zmax=0.5, nzs=21, ncontours=21, savefilename=None, aspect=None, log=False*)

**NAME:** plotDensity

**PURPOSE:** plot the density of this potential

**INPUT:**

*rmin* - minimum R

*rmax* - maximum R

*nrs* - grid in R

*zmin* - minimum z

*zmax* - maximum z

*nzs* - grid in z

*ncontours* - number of contours

savefilename - save to or restore from this savefile (pickle)  
log= if True, plot the log density

**OUTPUT:** plot to output device

**HISTORY:** 2014-01-05 - Written - Bovy (IAS)

### galpy.potential.Potential.plotEscapecurve

Potential.**plotEscapecurve**(\*args, \*\*kwargs)

NAME:

plotEscapecurve

PURPOSE:

plot the escape velocity curve for this potential (in the z=0 plane for non-spherical potentials)

INPUT:

Rrange - range

grid - number of points to plot

savefilename - save to or restore from this savefile (pickle)

+bovy\_plot(\*args, \*\*kwargs)

OUTPUT:

plot to output device

HISTORY:

2010-08-08 - Written - Bovy (NYU)

### galpy.potential.Potential.plotRotcurve

Potential.**plotRotcurve**(\*args, \*\*kwargs)

NAME:

plotRotcurve

PURPOSE:

plot the rotation curve for this potential (in the z=0 plane for non-spherical potentials)

INPUT:

Rrange - range

grid - number of points to plot

savefilename - save to or restore from this savefile (pickle)

+bovy\_plot(\*args, \*\*kwargs)

OUTPUT:

plot to output device

HISTORY:

2010-07-10 - Written - Bovy (NYU)

**galpy.potential.Potential.R2deriv**

Potential.R2deriv ( $R, Z, phi=0.0, t=0.0$ )

NAME:

R2deriv

PURPOSE:

evaluate the second radial derivative

INPUT:

$R$  - Galactocentric radius

$Z$  - vertical height

$phi$  - Galactocentric azimuth

$t$  - time

OUTPUT:

$d2phi/dR2$

HISTORY:

2011-10-09 - Written - Bovy (IAS)

**galpy.potential.Potential.R2deriv**

Potential.R2deriv ( $R, Z, phi=0.0, t=0.0$ )

NAME:

R2deriv

PURPOSE:

evaluate the second radial derivative

INPUT:

$R$  - Galactocentric radius

$Z$  - vertical height

$phi$  - Galactocentric azimuth

$t$  - time

OUTPUT:

$d2phi/dR2$

HISTORY:

2011-10-09 - Written - Bovy (IAS)

**galpy.potential.Potential.Rforce**

Potential.Rforce ( $R, z, phi=0.0, t=0.0$ )

NAME:

Rforce

PURPOSE:

evaluate radial force F\_R (R,z)

INPUT:

R - Cylindrical Galactocentric radius

z - vertical height

phi - azimuth (optional)

t - time (optional)

OUTPUT:

F\_R (R,z,phi,t)

HISTORY:

2010-04-16 - Written - Bovy (NYU)

**galpy.potential.Potential.rl**

Potential.rl(lz)

NAME:

rl

PURPOSE:

calculate the radius of a circular orbit of Lz

INPUT:

lz - Angular momentum

OUTPUT:

radius

HISTORY:

2012-07-30 - Written - Bovy ([IAS@MPIA](#))

NOTE:

seems to take about ~0.5 ms for a Miyamoto-Nagai potential; ~0.75 ms for a MWPotential

**galpy.planar.Potential.toPlanar**

Potential.toPlanar()

NAME: toPlanar

PURPOSE: convert a 3D potential into a planar potential in the mid-plane

INPUT: (none)

OUTPUT: planarPotential

HISTORY

**galpy.potential.Potential.toVertical**

Potential.**toVertical**(*R*)

**NAME:** toVertical

**PURPOSE:** convert a 3D potential into a linear (vertical) potential at R

**INPUT:** R - Galactocentric radius at which to create the vertical potential

**OUTPUT:** linear (vertical) potential

**HISTORY**

**galpy.potential.Potential.vcirc**

Potential.**vcirc**(*R*)

**NAME:**

vcirc

**PURPOSE:**

calculate the circular velocity at R in this potential

**INPUT:**

R - Galactocentric radius

**OUTPUT:**

circular rotation velocity

**HISTORY:**

2011-10-09 - Written - Bovy (IAS)

**galpy.potential.Potential.verticalfreq**

Potential.**verticalfreq**(*R*)

**NAME:**

verticalfreq

**PURPOSE:**

calculate the vertical frequency at R in this potential

**INPUT:**

R - Galactocentric radius

**OUTPUT:**

vertical frequency

**HISTORY:**

2012-07-25 - Written - Bovy ([IAS@MPIA](#))

## galpy.potential.Potential.vesc

Potential.vesc( $R$ )

NAME:

vesc

PURPOSE:

calculate the escape velocity at  $R$  for this potential

INPUT:

$R$  - Galactocentric radius

OUTPUT:

escape velocity

HISTORY:

2011-10-09 - Written - Bovy (IAS)

## galpy.potential.Potential.vterm

Potential.vterm( $l$ , deg=True)

NAME:

vterm

PURPOSE:

calculate the terminal velocity at  $l$  in this potential

INPUT:

$l$  - Galactic longitude [deg/rad]

deg= if True (default),  $l$  in deg

OUTPUT:

terminal velocity

HISTORY:

2013-05-31 - Written - Bovy (IAS)

## galpy.potential.Potential.z2deriv

Potential.z2deriv( $R, Z, phi=0.0, t=0.0$ )

NAME:

z2deriv

PURPOSE:

evaluate the second vertical derivative

INPUT:

R - Galactocentric radius

Z - vertical height

phi - Galactocentric azimuth

t - time

OUTPUT:

$d^2\phi/dz^2$

HISTORY:

2012-07-25 - Written - Bovy ([IAS@MPIA](#))

### galpy.potential.Potential.zforce

Potential.**zforce** ( $R, z, \phi=0.0, t=0.0$ )

NAME:

zforce

PURPOSE:

evaluate the vertical force  $F_z(R, z, t)$

INPUT:

R - Cylindrical Galactocentric radius

z - vertical height

phi - azimuth (optional)

t - time (optional)

OUTPUT:

$F_z(R, z, \phi, t)$

HISTORY:

2010-04-16 - Written - Bovy (NYU)

### General 3D potential routines

Use as method(...)

#### galpy.potential.dvcircdR

galpy.potential.**dvcircdR** ( $Pot, R$ )

NAME:

dvcircdR

PURPOSE:

calculate the derivative of the circular velocity wrt R at R in potential Pot

INPUT:

Pot - Potential instance or list of such instances

R - Galactocentric radius

OUTPUT:

derivative of the circular rotation velocity wrt R

HISTORY:

2013-01-08 - Written - Bovy (IAS)

## galpy.potential.epifreq

galpy.potential.**epifreq**(Pot, R)

NAME:

epifreq

PURPOSE:

calculate the epicycle frequency at R in the potential Pot

INPUT:

Pot - Potential instance or list thereof

R - Galactocentric radius

OUTPUT:

epicycle frequency

HISTORY:

2012-07-25 - Written - Bovy (IAS)

## galpy.potential.evaluateDensities

galpy.potential.**evaluateDensities**(R, z, Pot, phi=0.0, t=0.0, forcepoisson=False)

NAME:

evaluateDensities

PURPOSE:

convenience function to evaluate a possible sum of densities

INPUT:

R - cylindrical Galactocentric distance

z - distance above the plane

Pot - potential or list of potentials

phi - azimuth

t - time

forcepoisson= if True, calculate the density through the Poisson equation, even if an explicit expression for the density exists

OUTPUT:

rho(R,z)

**HISTORY:**

2010-08-08 - Written - Bovy (NYU)  
2013-12-28 - Added forcepoisson - Bovy (IAS)

**galpy.potential.evaluatephiforces**

galpy.potential.**evaluatephiforces** ( $R, z, Pot, phi=0.0, t=0.0$ )

**NAME:**

evaluatephiforces

**PURPOSE:**

convenience function to evaluate a possible sum of potentials

**INPUT:** R - cylindrical Galactocentric distance

z - distance above the plane

Pot - a potential or list of potentials

phi - azimuth (optional)

t - time (optional)

**OUTPUT:**

$F_{\phi}(R, z, \phi, t)$

**HISTORY:**

2010-04-16 - Written - Bovy (NYU)

**galpy.potential.evaluatePotentials**

galpy.potential.**evaluatePotentials** ( $R, z, Pot, phi=0.0, t=0.0$ )

**NAME:** evaluatePotentials**PURPOSE:** convenience function to evaluate a possible sum of potentials**INPUT:** R - cylindrical Galactocentric distance

z - distance above the plane

Pot - potential or list of potentials

phi - azimuth

t - time

**OUTPUT:**  $\Phi(R, z)$ **HISTORY:** 2010-04-16 - Written - Bovy (NYU)

### galpy.potential.evaluateR2derivs

galpy.potential.**evaluateR2derivs**(*R, z, Pot, phi=0.0, t=0.0*)

**NAME:** evaluateR2derivs

**PURPOSE:** convenience function to evaluate a possible sum of potentials

**INPUT:** *R* - cylindrical Galactocentric distance

*z* - distance above the plane

*Pot* - a potential or list of potentials

*phi* - azimuth (optional)

*t* - time (optional)

**OUTPUT:** d2Phi/d2R(*R,z,phi,t*)

**HISTORY:** 2012-07-25 - Written - Bovy (IAS)

### galpy.potential.evaluateRzderivs

galpy.potential.**evaluateRzderivs**(*R, z, Pot, phi=0.0, t=0.0*)

**NAME:** evaluateRzderivs

**PURPOSE:** convenience function to evaluate a possible sum of potentials

**INPUT:** *R* - cylindrical Galactocentric distance

*z* - distance above the plane

*Pot* - a potential or list of potentials

*phi* - azimuth (optional)

*t* - time (optional)

**OUTPUT:** d2Phi/dz/dR(*R,z,phi,t*)

**HISTORY:** 2013-08-28 - Written - Bovy (IAS)

### galpy.potential.evaluateRforces

galpy.potential.**evaluateRforces**(*R, z, Pot, phi=0.0, t=0.0*)

**NAME:** evaluateRforce

**PURPOSE:** convenience function to evaluate a possible sum of potentials

**INPUT:** *R* - cylindrical Galactocentric distance

*z* - distance above the plane

*Pot* - a potential or list of potentials

*phi* - azimuth (optional)

*t* - time (optional)

**OUTPUT:** F\_R(*R,z,phi,t*)

**HISTORY:** 2010-04-16 - Written - Bovy (NYU)

**galpy.potential.evaluatez2derivs**

`galpy.potential.evaluatez2derivs(R, z, Pot, phi=0.0, t=0.0)`

**NAME:** evaluatez2derivs

**PURPOSE:** convenience function to evaluate a possible sum of potentials

**INPUT:** R - cylindrical Galactocentric distance

z - distance above the plane

Pot - a potential or list of potentials

phi - azimuth (optional)

t - time (optional)

**OUTPUT:** d2Phi/d2z(R,z,phi,t)

**HISTORY:** 2012-07-25 - Written - Bovy (IAS)

**galpy.potential.evaluatezforces**

`galpy.potential.evaluatezforces(R, z, Pot, phi=0.0, t=0.0)`

**NAME:**

evaluatezforces

**PURPOSE:**

convenience function to evaluate a possible sum of potentials

**INPUT:**

R - cylindrical Galactocentric distance

z - distance above the plane

Pot - a potential or list of potentials

phi - azimuth (optional)

t - time (optional)

**OUTPUT:**

F\_z(R,z,phi,t)

**HISTORY:**

2010-04-16 - Written - Bovy (NYU)

**galpy.potential.flattening**

`galpy.potential.flattening(Pot, R, z)`

**NAME:**

flattening

**PURPOSE:**

calculate the potential flattening, defined as  $\sqrt{|\mathbf{z}/\mathbf{R} \cdot \mathbf{F}_R/\mathbf{F}_z|}$

**INPUT:**

Pot - Potential instance or list thereof

R - Galactocentric radius

z - height

OUTPUT:

flattening

HISTORY:

2012-09-13 - Written - Bovy (IAS)

### galpy.potential.lindbladR

galpy.potential.**lindbladR**(*Pot, OmegaP, m=2, \*\*kwargs*)

NAME:

lindbladR

PURPOSE:

calculate the radius of a Lindblad resonance

INPUT:

Pot - Potential instance or list of such instances

*OmegaP* - pattern speed

**m= order of the resonance (as in m(O-Op)=kappa (negative m for outer) use m='corotation'**  
for corotation

+scipy.optimize.brentq xtol,rtol,maxiter kwargs

OUTPUT:

radius of Linblad resonance, None if there is no resonance

HISTORY:

2011-10-09 - Written - Bovy (IAS)

### galpy.potential.omegac

galpy.potential.**omegac**(*Pot, R*)

NAME:

omegac

PURPOSE:

calculate the circular angular speed velocity at R in potential Pot

INPUT:

Pot - Potential instance or list of such instances

R - Galactocentric radius

OUTPUT:

circular angular speed

HISTORY:

2011-10-09 - Written - Bovy (IAS)

### galpy.potential.plotDensities

```
galpy.potential.plotDensities(Pot, rmin=0.0, rmax=1.5, nrs=21, zmin=-0.5, zmax=0.5, nzs=21, ncontours=21, savefilename=None, aspect=None, log=False)
```

**NAME:** plotDensities

**PURPOSE:** plot the density a set of potentials

**INPUT:** Pot - Potential or list of Potential instances

rmin - minimum R

rmax - maximum R

nrs - grid in R

zmin - minimum z

zmax - maximum z

nzs - grid in z

ncontours - number of contours

savefilename - save to or restore from this savefile (pickle)

log= if True, plot the log density

**OUTPUT:** plot to output device

**HISTORY:** 2013-07-05 - Written - Bovy (IAS)

### galpy.potential.plotEscapecurve

```
galpy.potential.plotEscapecurve(Pot, *args, **kwargs)
```

**NAME:**

plotEscapecurve

**PURPOSE:**

plot the escape velocity curve for this potential (in the z=0 plane for non-spherical potentials)

**INPUT:**

Pot - Potential or list of Potential instances

Range - Range in R to consider

grid - grid in R

savefilename - save to or restore from this savefile (pickle)

+bovy\_plot.bovy\_plot args and kwargs

**OUTPUT:**

plot to output device

**HISTORY:**

2010-08-08 - Written - Bovy (NYU)

## galpy.potential.plotPotentials

```
galpy.potential.plotPotentials(Pot, rmin=0.0, rmax=1.5, nrs=21, zmin=-0.5, zmax=0.5, nzs=21, ncontours=21, savefilename=None, aspect=None)
```

**NAME:** plotPotentials

**PURPOSE:** plot a set of potentials

**INPUT:** Pot - Potential or list of Potential instances

rmin - minimum R

rmax - maximum R

nrs - grid in R

zmin - minimum z

zmax - maximum z

nzs - grid in z

ncontours - number of contours

savefilename - save to or restore from this savefile (pickle)

**OUTPUT:** plot to output device

**HISTORY:** 2010-07-09 - Written - Bovy (NYU)

## galpy.potential.plotRotcurve

```
galpy.potential.plotRotcurve(Pot, *args, **kwargs)
```

**NAME:**

plotRotcurve

**PURPOSE:**

plot the rotation curve for this potential (in the z=0 plane for non-spherical potentials)

**INPUT:**

Pot - Potential or list of Potential instances

Rrange - Range in R to consider

grid - grid in R

savefilename - save to or restore from this savefile (pickle)

+bovy\_plot.bovy\_plot args and kwargs

**OUTPUT:**

plot to output device

**HISTORY:**

2010-07-10 - Written - Bovy (NYU)

**galpy.potential.rl**

`galpy.potential.rl (Pot, lz)`

NAME:

rl

PURPOSE:

calculate the radius of a circular orbit of Lz

INPUT:

Pot - Potential instance or list thereof

lz - Angular momentum

OUTPUT:

radius

HISTORY:

2012-07-30 - Written - Bovy ([IAS@MPIA](#))

NOTE:

seems to take about ~0.5 ms for a Miyamoto-Nagai potential; ~0.75 ms for a MWPotential

**galpy.potential.vcirc**

`galpy.potential.vcirc (Pot, R)`

NAME:

vcirc

PURPOSE:

calculate the circular velocity at R in potential Pot

INPUT:

Pot - Potential instance or list of such instances

R - Galactocentric radius

OUTPUT:

circular rotation velocity

HISTORY:

2011-10-09 - Written - Bovy (IAS)

**galpy.potential.verticalfreq**

`galpy.potential.verticalfreq (Pot, R)`

NAME:

verticalfreq

PURPOSE:

calculate the vertical frequency at R in the potential Pot

INPUT:

Pot - Potential instance or list thereof

R - Galactocentric radius

OUTPUT:

vertical frequency

HISTORY:

2012-07-25 - Written - Bovy ([IAS@MPIA](#))

## galpy.potential.vesc

galpy.potential.**vesc**(Pot, R)

NAME:

vesc

PURPOSE:

calculate the escape velocity at R for potential Pot

INPUT:

Pot - Potential instances or list thereof

R - Galactocentric radius

OUTPUT:

escape velocity

HISTORY:

2011-10-09 - Written - Bovy (IAS)

## galpy.potential.vterm

galpy.potential.**vterm**(Pot, l, deg=True)

NAME:

vterm

PURPOSE:

calculate the terminal velocity at l in this potential

INPUT:

Pot - Potential instance

l - Galactic longitude [deg/rad]

deg= if True (default), l in deg

OUTPUT:

terminal velocity

HISTORY:

2013-05-31 - Written - Bovy (IAS)

## Specific potentials

### Double exponential disk potential

```
class galpy.potential.DoubleExponentialDiskPotential(amp=1.0,
                                                    ro=1.0,
                                                    hr=0.3333333333333333,
                                                    hz=0.0625,
                                                    maxiter=20,
                                                    tol=0.001,
                                                    normalize=False,
                                                    new=True,
                                                    kmaxFac=2.0,
                                                    glorder=10)
```

Class that implements the double exponential disk potential  $\rho(R,z) = \rho_0 e^{-R/h_R} e^{-|z|/h_z}$

```
__init__(amp=1.0, ro=1.0, hr=0.3333333333333333, hz=0.0625, maxiter=20, tol=0.001, normalize=False, new=True, kmaxFac=2.0, glorder=10)
```

NAME:

`__init__`

PURPOSE:

initialize a double-exponential disk potential

INPUT:

amp - amplitude to be applied to the potential (default: 1)

hr - disk scale-length in terms of ro

hz - scale-height

tol - relative accuracy of potential-evaluations

maxiter - scipy.integrate keyword

normalize - if True, normalize such that  $\nabla\phi(1,0)=1$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $\nabla\phi(1,0)=1$ .

OUTPUT:

DoubleExponentialDiskPotential object

HISTORY:

2010-04-16 - Written - Bovy (NYU)

2013-01-01 - Re-implemented using faster integration techniques - Bovy (IAS)

### Double power-law density spherical potential

```
class galpy.potential.TwoPowerSphericalPotential(amp=1.0, a=1.0, alpha=1.0, beta=3.0,
                                                 normalize=False)
```

Class that implements spherical potentials that are derived from two-power density models

A

$\rho(r) = \frac{A}{r^a} (1+r/a)^{\alpha-\beta}$

```
__init__(amp=1.0, a=1.0, alpha=1.0, beta=3.0, normalize=False)
```

NAME:

`__init__`

PURPOSE:

initialize a two-power-density potential

INPUT:

amp - amplitude to be applied to the potential (default: 1)

a - “scale” (in terms of Ro)

alpha - inner power

beta - outer power

normalize - if True, normalize such that  $vc(1.,0.)=1.$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $vc(1.,0.)=1.$

OUTPUT:

(none)

HISTORY:

2010-07-09 - Started - Bovy (NYU)

### Jaffe potential

```
class galpy.potential.JaffePotential(amp=1.0, a=1.0, normalize=False)
```

Class that implements the Jaffe potential

```
__init__(amp=1.0, a=1.0, normalize=False)
```

NAME:

\_\_init\_\_

PURPOSE:

Initialize a Jaffe potential

INPUT:

amp - amplitude to be applied to the potential

a - “scale” (in terms of Ro)

normalize - if True, normalize such that  $vc(1.,0.)=1.$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $vc(1.,0.)=1.$

OUTPUT:

(none)

HISTORY:

2010-07-09 - Written - Bovy (NYU)

### Flattened Power-law potential

Flattening is in the potential as in [Evans \(1994\)](#) rather than in the density

```
class galpy.potential.FlattenedPowerPotential(amp=1.0, alpha=1.0, q=1.0, core=1e-08, normalize=False)
```

Class that implements a power-law potential that is flattened in the potential (NOT the density) amp

$\phi(R,z) = \frac{amp}{R^{\alpha}} ; m^2 = R^2 + z^2/q^2$  alpha m^alpha

```
__init__(amp=1.0, alpha=1.0, q=1.0, core=1e-08, normalize=False)
NAME:
```

\_\_init\_\_

PURPOSE:

initialize a flattened power-law potential

INPUT:

amp - amplitude to be applied to the potential (default: 1)

alpha - power

q - flattening

core - core radius

normalize - if True, normalize such that  $vc(1.,0.)=1.$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $vc(1.,0.)=1.$

OUTPUT:

(none)

HISTORY:

2013-01-09 - Written - Bovy (IAS)

## Hernquist potential

```
class galpy.potential.HernquistPotential(amp=1.0, a=1.0, normalize=False)
```

Class that implements the Hernquist potential

```
__init__(amp=1.0, a=1.0, normalize=False)
```

NAME:

\_\_init\_\_

PURPOSE:

Initialize a Hernquist potential

INPUT:

amp - amplitude to be applied to the potential

a - “scale” (in terms of  $R_\odot$ )

normalize - if True, normalize such that  $vc(1.,0.)=1.$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $vc(1.,0.)=1.$

OUTPUT:

(none)

HISTORY:

2010-07-09 - Written - Bovy (NYU)

## Kepler potential

**class** galpy.potential.**KeplerPotential** (*amp=1.0, normalize=False*)

Class that implements the Kepler potential

amp

**Phi(r)=**  $\frac{-\mathrm{amp}}{r}$

**\_\_init\_\_** (*amp=1.0, normalize=False*)

NAME:

**\_\_init\_\_**

PURPOSE:

initialize a Kepler potential

INPUT:

amp - amplitude to be applied to the potential (default: 1)

alpha - inner power

normalize - if True, normalize such that  $vc(1.,0.)=1.$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $vc(1.,0.)=1.$

OUTPUT:

(none)

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## Logarithmic halo potential

**class** galpy.potential.**LogarithmicHaloPotential** (*amp=1.0, core=1e-08, q=1.0, normalize=False*)

Class that implements the logarithmic halo potential  $\Phi(r)$

**\_\_init\_\_** (*amp=1.0, core=1e-08, q=1.0, normalize=False*)

NAME:

**\_\_init\_\_**

PURPOSE:

initialize a Logarithmic Halo potential

INPUT:

amp - amplitude to be applied to the potential (default: 1)

core - core radius at which the logarithm is cut

q - potential flattening  $(z/q)^{**2}$ .

normalize - if True, normalize such that  $vc(1.,0.)=1.$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $vc(1.,0.)=1.$

OUTPUT:

(none)

**HISTORY:**

2010-04-02 - Started - Bovy (NYU)

**Miyamoto-Nagai potential**

```
class galpy.potential.MiyamotoNagaiPotential(amp=1.0, a=0.0, b=0.0, normalize=False)
```

**Class that implements the Miyamoto-Nagai potential** amp

**phi(R,z) = -**  $\frac{\text{sqrt}(R^2 + (a + \text{sqrt}(z^2 + b^2))^2)}{2}$

**\_\_init\_\_(amp=1.0, a=0.0, b=0.0, normalize=False)**

NAME:

**\_\_init\_\_**

**PURPOSE:**

initialize a Miyamoto-Nagai potential

**INPUT:**

amp - amplitude to be applied to the potential (default: 1)

a - “disk scale” (in terms of Ro)

b - “disk height” (in terms of Ro)

normalize - if True, normalize such that  $vc(1.,0.)=1.$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $vc(1.,0.)=1.$

**OUTPUT:**

(none)

**HISTORY:**

2010-07-09 - Started - Bovy (NYU)

**NFW potential**

```
class galpy.potential.NFWPotential(amp=1.0, a=1.0, normalize=False)
```

**Class that implements the NFW potential**

**\_\_init\_\_(amp=1.0, a=1.0, normalize=False)**

NAME:

**\_\_init\_\_**

**PURPOSE:**

Initialize a NFW potential

**INPUT:**

amp - amplitude to be applied to the potential

a - “scale” (in terms of Ro)

normalize - if True, normalize such that  $vc(1.,0.)=1.$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $vc(1.,0.)=1.$

**OUTPUT:**

(none)

HISTORY:

2010-07-09 - Written - Bovy (NYU)

### Power-law density spherical potential

**class** galpy.potential.**PowerSphericalPotential** (*amp=1.0, alpha=1.0, normalize=False*)

Class that implements spherical potentials that are derived from power-law density models

amp

**rho(r)=** \_\_\_\_\_  $r^{\alpha}$

**\_\_init\_\_** (*amp=1.0, alpha=1.0, normalize=False*)

NAME:

**\_init\_**

PURPOSE:

initialize a power-law-density potential

INPUT:

amp - amplitude to be applied to the potential (default: 1)

alpha - inner power

normalize - if True, normalize such that  $\text{vc}(1.,0.)=1.$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $\text{vc}(1.,0.)=1.$

OUTPUT:

(none)

HISTORY:

2010-07-10 - Written - Bovy (NYU)

### Razor-thin exponential disk potential

**class** galpy.potential.**RazorThinExponentialDiskPotential** (*amp=1.0, ro=1.0, hr=0.3333333333333333, maxiter=20, tol=0.001, normalize=False, new=True, glorder=100*)

Class that implements the razor-thin exponential disk potential  $\rho(R,z) = \rho_0 e^{-R/h_R} \delta(z)$

**\_\_init\_\_** (*amp=1.0, ro=1.0, hr=0.3333333333333333, maxiter=20, tol=0.001, normalize=False, new=True, glorder=100*)

NAME:

**\_init\_**

PURPOSE:

initialize a razor-thin-exponential disk potential

INPUT:

amp - amplitude to be applied to the potential (default: 1)  
hr - disk scale-length in terms of ro  
tol - relative accuracy of potential-evaluations  
maxiter - scipy.integrate keyword  
normalize - if True, normalize such that  $vc(1.,0.)=1.$ , or, if given as a number, such that the force is this fraction of the force necessary to make  $vc(1.,0.)=1.$

OUTPUT:

RazorThinExponentialDiskPotential object

HISTORY:

2012-12-27 - Written - Bovy (IAS)

In addition to these classes, a Milky-Way-like potential is defined as `galpy.potential.MWPotential`. This potential is defined as

```
>>> mp= MiyamotoNagaiPotential(a=0.5,b=0.0375,normalize=.6)
>>> np= NFWPotential(a=4.5,normalize=.35)
>>> hp= HernquistPotential(a=0.6/8,normalize=0.05)
>>> MWPotential= [mp,np,hp]
```

and can thus be used like any list of Potentials.

## 2.2.2 2D potentials

### General instance routines

Use as `Potential-instance.method(...)`

#### `galpy.potential.planarPotential.__call__`

`planarPotential.__call__(R, phi=0.0, t=0.0, dR=0, dphi=0)`  
NAME:

`__call__`

PURPOSE:

evaluate the potential

INPUT:

R - Cylindrical radius

phi= azimuth (optional)

t= time (optional)

dR=, dphi= if set to non-zero integers, return the dR,dphi't derivative

OUTPUT:

`Phi(R,phi,t))`

HISTORY:

2010-07-13 - Written - Bovy (NYU)

**galpy.potential.planarPotential.phiforce**

planarPotential.**phiforce** ( $R, phi=0.0, t=0.0$ )

NAME:

phiforce

PURPOSE:

evaluate the phi force

INPUT:

$R$  - Cylindrical radius

$phi$ = azimuth (optional)

$t$ = time (optional)

OUTPUT:

$\mathbf{F}_\phi(R,(\phi,t))$

HISTORY:

2010-07-13 - Written - Bovy (NYU)

**galpy.potential.planarPotential.Rforce**

planarPotential.**Rforce** ( $R, phi=0.0, t=0.0$ )

NAME:

Rforce

PURPOSE:

evaluate the radial force

INPUT:

$R$  - Cylindrical radius

$phi$ = azimuth (optional)

$t$ = time (optional)

OUTPUT:

$\mathbf{F}_R(R,(\phi,t))$

HISTORY:

2010-07-13 - Written - Bovy (NYU)

**General axisymmetric potential instance routines**

Use as `Potential-instance.method(...)`

**galpy.potential.planarAxiPotential.epifreq**

Potential.**epifreq**(*R*)

NAME:

epifreq

PURPOSE:

calculate the epicycle frequency at R in this potential

INPUT:

R - Galactocentric radius

OUTPUT:

epicycle frequency

HISTORY:

2011-10-09 - Written - Bovy (IAS)

**galpy.potential.planarAxiPotential.lindbladR**

Potential.**lindbladR**(*OmegaP*, *m*=2, \*\**kwargs*)

NAME:

lindbladR

PURPOSE:

calculate the radius of a Lindblad resonance

INPUT:

*OmegaP* - pattern speed

**m= order of the resonance (as in m(O-Op)=kappa (negative m for outer) use m='corotation'**  
for corotation +scipy.optimize.brentq xtol,rtol,maxiter kwargs

OUTPUT:

radius of Linblad resonance, None if there is no resonance

HISTORY:

2011-10-09 - Written - Bovy (IAS)

**galpy.potential.planarAxiPotential.omegac**

Potential.**omegac**(*R*)

NAME:

omegac

PURPOSE:

calculate the circular angular speed at R in this potential

INPUT:

R - Galactocentric radius

**OUTPUT:**

circular angular speed

**HISTORY:**

2011-10-09 - Written - Bovy (IAS)

### galpy.potential.planarAxiPotential.plot

planarAxiPotential.**plot**(\*args, \*\*kwargs)

**NAME:** plot

**PURPOSE:** plot the potential

**INPUT:** Rrange - range grid - number of points to plot savefilename - save to or restore from this savefile (pickle) +bovy\_plot(\*args, \*\*kwargs)

**OUTPUT:** plot to output device

**HISTORY:** 2010-07-13 - Written - Bovy (NYU)

### galpy.potential.planarAxiPotential.plotEscapecurve

planarAxiPotential.**plotEscapecurve**(\*args, \*\*kwargs)

**NAME:**

plotEscapecurve

**PURPOSE:**

plot the escape velocity curve for this potential

**INPUT:**

Rrange - range

grid - number of points to plot

savefilename - save to or restore from this savefile (pickle)

+bovy\_plot(\*args, \*\*kwargs)

**OUTPUT:**

plot to output device

**HISTORY:**

2010-07-13 - Written - Bovy (NYU)

### galpy.potential.planarAxiPotential.plotRotcurve

planarAxiPotential.**plotRotcurve**(\*args, \*\*kwargs)

**NAME:**

plotRotcurve

**PURPOSE:**

plot the rotation curve for this potential

**INPUT:**

Rrange - range  
grid - number of points to plot  
savefilename - save to or restore from this savefile (pickle)  
+bovy\_plot(\*args, \*\*kwargs)

**OUTPUT:**

plot to output device

**HISTORY:**

2010-07-13 - Written - Bovy (NYU)

**galpy.potential.planarAxiPotential.vcirc**

Potential.vcirc( $R$ )

**NAME:**

vcirc

**PURPOSE:**

calculate the circular velocity at  $R$  in this potential

**INPUT:**

$R$  - Galactocentric radius

**OUTPUT:**

circular rotation velocity

**HISTORY:**

2011-10-09 - Written - Bovy (IAS)

**galpy.potential.planarAxiPotential.vesc**

Potential.vesc( $R$ )

**NAME:**

vesc

**PURPOSE:**

calculate the escape velocity at  $R$  for this potential

**INPUT:**

$R$  - Galactocentric radius

**OUTPUT:**

escape velocity

**HISTORY:**

2011-10-09 - Written - Bovy (IAS)

## General 2D potential routines

Use as method ( . . . )

### `galpy.potential.evaluateplanarphiforces`

`galpy.potential.evaluateplanarphiforces (R, Pot, phi=None, t=0.0)`

NAME:

evaluateplanarphiforces

PURPOSE:

evaluate the phiforce of a (list of) planarPotential instance(s)

INPUT:

R - Cylindrical radius

Pot - (list of) planarPotential instance(s)

phi= azimuth (optional)

t= time (optional)

OUTPUT:

F\_phi(R,phi,t))

HISTORY:

2010-07-13 - Written - Bovy (NYU)

### `galpy.potential.evaluateplanarPotentials`

`galpy.potential.evaluateplanarPotentials (R, Pot, phi=None, t=0.0, dR=0, dphi=0)`

NAME:

evaluateplanarPotentials

PURPOSE:

evaluate a (list of) planarPotential instance(s)

INPUT:

R - Cylindrical radius

Pot - (list of) planarPotential instance(s)

phi= azimuth (optional)

t= time (optional)

dR=, dphi= if set to non-zero integers, return the dR,dphi't derivative instead

OUTPUT:

Phi(R,phi,t))

HISTORY:

2010-07-13 - Written - Bovy (NYU)

**galpy.potential.evaluateplanarRforces**

galpy.potential.**evaluateplanarRforces** (*R*, *Pot*, *phi=None*, *t=0.0*)

NAME:

evaluateplanarRforces

PURPOSE:

evaluate the Rforce of a (list of) planarPotential instance(s)

INPUT:

*R* - Cylindrical radius

*Pot* - (list of) planarPotential instance(s)

*phi*= azimuth (optional)

*t*= time (optional)

OUTPUT:

*F\_R(R,phi,t)*

HISTORY:

2010-07-13 - Written - Bovy (NYU)

**galpy.potential.plotEscapecurve**

galpy.potential.**plotEscapecurve** (*Pot*, \**args*, \*\**kwargs*)

NAME:

plotEscapecurve

PURPOSE:

plot the escape velocity curve for this potential (in the *z=0* plane for non-spherical potentials)

INPUT:

*Pot* - Potential or list of Potential instances

*Rrange* - Range in *R* to consider

*grid* - grid in *R*

*savefilename* - save to or restore from this savefile (pickle)

+bovy\_plot.bovy\_plot args and kwargs

OUTPUT:

plot to output device

HISTORY:

2010-08-08 - Written - Bovy (NYU)

## galpy.potential.plotplanarPotentials

galpy.potential.**plotplanarPotentials**(*Pot*, \**args*, \*\**kwargs*)

NAME:

plotplanarPotentials

PURPOSE:

plot a planar potential

INPUT:

Rrange - range

xrange, yrange - if relevant

grid, gridx, gridy - number of points to plot

savefilename - save to or restore from this savefile (pickle)

ncontours - number of contours to plot (if applicable)

+bovy\_plot(\**args*, \*\**kwargs*) or bovy\_dens2d(\*\**kwargs*)

OUTPUT:

plot to output device

HISTORY:

2010-07-13 - Written - Bovy (NYU)

## galpy.potential.plotRotcurve

galpy.potential.**plotRotcurve**(*Pot*, \**args*, \*\**kwargs*)

NAME:

plotRotcurve

PURPOSE:

plot the rotation curve for this potential (in the z=0 plane for non-spherical potentials)

INPUT:

Pot - Potential or list of Potential instances

Rrange - Range in R to consider

grid - grid in R

savefilename - save to or restore from this savefile (pickle)

+bovy\_plot.bovy\_plot args and kwargs

OUTPUT:

plot to output device

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## Specific potentials

All of the 3D potentials above can be used as two-dimensional potentials in the mid-plane.

### galpy.potential.RZToplanarPotential

`galpy.potential.RZToplanarPotential(RZPot)`

NAME:

RZToplanarPotential

PURPOSE:

convert an RZPotential to a planarPotential in the mid-plane ( $z=0$ )

INPUT:

RZPot - RZPotential instance or list of such instances (existing planarPotential instances are just copied to the output)

OUTPUT:

planarPotential instance(s)

HISTORY:

2010-07-13 - Written - Bovy (NYU)

In addition, a two-dimensional bar potential and a two spiral potentials are included

### Dehnen bar potential

```
class galpy.potential.DehnenBarPotential(amp=1.0, omegab=None, rb=None, chi=0.8,
                                         rolr=0.9, barphi=0.4363323129985824, tform=-4.0,
                                         tsteady=None, beta=0.0, alpha=0.01, Af=None)
```

Class that implements the Dehnen bar potential (Dehnen 2000)

```
__init__(amp=1.0, omegab=None, rb=None, chi=0.8, rolr=0.9, barphi=0.4363323129985824,
        tform=-4.0, tsteady=None, beta=0.0, alpha=0.01, Af=None)
```

NAME:

`__init__`

PURPOSE:

initialize a Dehnen bar potential

INPUT:

amp - amplitude to be applied to the potential (default: 1., see alpha or Ab below)

barphi - angle between sun-GC line and the bar's major axis (in rad; default=25 degree)

tform - start of bar growth / bar period (default: -4)

tsteady - time at which the bar is fully grown / bar period (default: tform/2)

Either provide:

1.rolr - radius of the Outer Lindblad Resonance for a circular orbit

chi - fraction R\_bar / R\_CR (corotation radius of bar)

alpha - relative bar strength (default: 0.01)

beta - power law index of rotation curve (to calculate OLR, etc.)  
2.omegab - rotation speed of the bar  
rb - bar radius  
Af - bar strength

OUTPUT:

(none)

HISTORY:

2010-11-24 - Started - Bovy (NYU)

### Cos(m phi) disk potential

Generalization of the *lopsided* and *elliptical* disk potentials to any m.

```
class galpy.potential.CosmphiDiskPotential(amp=1.0, phib=0.4363323129985824, p=0.0, phio=0.01, m=1.0, tform=None, tsteady=None, cp=None, sp=None)
```

Class that implements the disk potential  $\phi(R,\phi) = \phi_{\text{io}} (R/R_{\text{o}})^p \cos[m(\phi - \phi_{\text{ib}})]$

```
__init__(amp=1.0, phib=0.4363323129985824, p=0.0, phio=0.01, m=1.0, tform=None, tsteady=None, cp=None, sp=None)
```

NAME:

\_\_init\_\_

PURPOSE:

initialize an cosmphi disk potential

$\phi(R,\phi) = \phi_{\text{io}} (R/R_{\text{o}})^p \cos[m(\phi - \phi_{\text{ib}})]$

INPUT:

amp= amplitude to be applied to the potential (default: 1.), see twophio below

tform= start of growth (to smoothly grow this potential)

tsteady= time delay at which the perturbation is fully grown (default: 2.)

m=  $\cos(m * (\phi - \phi_{\text{ib}}))$

p= power-law index of the  $\phi(R) = (R/R_{\text{o}})^p$  part

Either:

1.phib= angle (in rad; default=25 degree)

phio= potential perturbation (in terms of  $\phi_{\text{io}}/\text{vo}^2$  if  $\text{vo}=1$  at  $R_{\text{o}}=1$ )

2.cp, sp=  $m * \phi_{\text{io}} * \cos(m * \phi_{\text{ib}})$ ,  $m * \phi_{\text{io}} * \sin(m * \phi_{\text{ib}})$

OUTPUT:

(none)

HISTORY:

2011-10-27 - Started - Bovy (IAS)

## Elliptical disk potential

Like in Kuijken & Tremaine

```
class galpy.potential.EllipticalDiskPotential(amp=1.0, phib=0.4363323129985824,
                                              p=0.0, twophio=0.01, tform=None,
                                              tsteady=None, cp=None, sp=None)
    Class that implements the Elliptical disk potential of Kuijken & Tremaine (1994) phi(R,phi) = phio (R/Ro)^p cos[2(phi-phib)]
    __init__(amp=1.0, phib=0.4363323129985824, p=0.0, twophio=0.01, tform=None, tsteady=None,
             cp=None, sp=None)
```

NAME:

`__init__`

PURPOSE:

initialize an Elliptical disk potential

$\phi(R,\phi) = \phi_{\text{io}} (R/R_o)^p \cos[2(\phi-\phi_{\text{ib}})]$

INPUT:

`amp`= amplitude to be applied to the potential (default: 1.), see `twophio` below

`tform`= start of growth (to smoothly grow this potential)

`tsteady`= time delay at which the perturbation is fully grown (default: 2.)

`p`= power-law index of the  $\phi(R) = (R/R_o)^p$  part

Either:

1.`phib`= angle (in rad; default=25 degree)

`twophio`= potential perturbation (in terms of  $2\phi_{\text{io}}/\text{vo}^2$  if `vo`=1 at `Ro`=1)

2.`cp, sp`=  $\text{twophio} * \cos(2\phi_{\text{ib}}), \text{twophio} * \sin(2\phi_{\text{ib}})$

OUTPUT:

(none)

HISTORY:

2011-10-19 - Started - Bovy (IAS)

## Lopsided disk potential

Like in Kuijken & Tremaine, but for  $m=1$

```
class galpy.potential.LopsidedDiskPotential(amp=1.0, phib=0.4363323129985824, p=0.0,
                                              phio=0.01, tform=None, tsteady=None,
                                              cp=None, sp=None)
```

Class that implements the disk potential  $\phi(R,\phi) = \phi_{\text{io}} (R/R_o)^p \cos[\phi-\phi_{\text{ib}}]$  See documentation for `CosmphiDiskPotential`

### Steady-state logarithmic spiral potential

```
class galpy.potential.SteadyLogSpiralPotential(amp=1.0, omegas=0.65, A=-0.035, alpha=-7.0, m=2, gamma=0.7853981633974483, p=None, tform=None, tsteady=None)
```

Class that implements a steady-state spiral potential

$V(r,\phi,t) = A/\alpha \cos(\alpha \ln(r) - m(\phi - \Omega_{\text{gas}} * t - \gamma))$

```
__init__(amp=1.0, omegas=0.65, A=-0.035, alpha=-7.0, m=2, gamma=0.7853981633974483, p=None, tform=None, tsteady=None)
```

NAME:

\_\_init\_\_

PURPOSE:

initialize a logarithmic spiral potential

INPUT:

amp - amplitude to be applied to the potential (default: 1., A below)

gamma - angle between sun-GC line and the line connecting the peak of the spiral pattern at the Solar radius (in rad; default=45 degree)

A - force amplitude ( $\alpha * \text{potential-amplitude}$ ; default=0.035)

omegas= - pattern speed (default=0.65)

m= number of arms

Either provide:

1.alpha=

2.p= pitch angle (rad)

tform - start of spiral growth / spiral period (default: -Infinity)

tsteady - time from tform at which the spiral is fully grown / spiral period (default: tform+2 periods)

OUTPUT:

(none)

HISTORY:

2011-03-27 - Started - Bovy (NYU)

### Transient logarithmic spiral potential

```
class galpy.potential.TransientLogSpiralPotential(amp=1.0, omegas=0.65, A=-0.035, alpha=-7.0, m=2, gamma=0.7853981633974483, p=None, sigma=1.0, to=0.0)
```

Class that implements a steady-state spiral potential

$V(r,\phi,t) = A(t)/\alpha \cos(\alpha \ln(r) - m(\phi - \Omega_{\text{gas}} * t - \gamma))$

where

$A(t) = A_{\text{max}} \exp(-[t - t_0]^2/\sigma^2/2.)$

---

`__init__(amp=1.0, omegas=0.65, A=-0.035, alpha=-7.0, m=2, gamma=0.7853981633974483, p=None, sigma=1.0, to=0.0)`

NAME:

`__init__`

PURPOSE:

initialize a transient logarithmic spiral potential localized around to

INPUT:

amp - amplitude to be applied to the potential (default: 1., A below)

gamma - angle between sun-GC line and the line connecting the peak of the spiral pattern at the Solar radius (in rad; default=45 degree)

A - force amplitude (alpha\*potential-amplitude; default=0.035)

omegas= - pattern speed (default=0.65)

m= number of arms

to= time at which the spiral peaks

sigma= “spiral duration” (sigma in Gaussian amplitude)

Either provide:

1.alpha=

2.p= pitch angle (rad)

OUTPUT:

(none)

HISTORY:

2011-03-27 - Started - Bovy (NYU)

### 2.2.3 1D potentials

#### General instance routines

Use as `Potential-instance.method(...)`

#### `galpy.potential.linearPotential.__call__`

`linearPotential.__call__(x, t=0.0)`

NAME: `__call__`

PURPOSE:

evaluate the potential

INPUT:

x - position

t= time (optional)

OUTPUT:

$\Phi(x,t)$

HISTORY:

2010-07-12 - Written - Bovy (NYU)

**galpy.potential.linearPotential.force**

`linearPotential.force (x, t=0.0)`

NAME:

`force`

PURPOSE:

evaluate the force

INPUT:

`x` - position

`t`= time (optional)

OUTPUT:

$F(x,t)$

HISTORY:

2010-07-12 - Written - Bovy (NYU)

**galpy.potential.linearPotential.plot**

`linearPotential.plot (t=0.0, min=-15.0, max=15, ns=21, savefilename=None)`

NAME:

`plot`

PURPOSE:

plot the potential

INPUT:

`t` - time to evaluate the potential at

`min` - minimum `x`

`max` - maximum `x`

`ns` - grid in `x`

`savefilename` - save to or restore from this savefile (pickle)

OUTPUT:

plot to output device

HISTORY:

2010-07-13 - Written - Bovy (NYU)

## General 1D potential routines

Use as method ( . . . )

### **galpy.potential.evaluateLinearForces**

`galpy.potential.evaluateLinearForces (x, Pot, t=0.0)`

NAME:

evaluateLinearForces

PURPOSE:

evaluate the forces due to a list of potentials

INPUT:

x - evaluate forces at this position

Pot - (list of) linearPotential instance(s)

t - time to evaluate at

OUTPUT:

force(x,t)

HISTORY:

2010-07-13 - Written - Bovy (NYU)

### **galpy.potential.evaluateLinearPotentials**

`galpy.potential.evaluateLinearPotentials (x, Pot, t=0.0)`

NAME:

evaluateLinearPotentials

PURPOSE:

evaluate the sum of a list of potentials

INPUT:

x - evaluate potentials at this position

Pot - (list of) linearPotential instance(s)

t - time to evaluate at

OUTPUT:

pot(x,t)

HISTORY:

2010-07-13 - Written - Bovy (NYU)

## galpy.potential.plotlinearPotentials

```
galpy.potential.plotlinearPotentials(Pot, t=0.0, min=-15.0, max=15, ns=21, savefile-name=None)
```

NAME:

plotlinearPotentials

PURPOSE:

plot a combination of potentials

INPUT:

t - time to evaluate potential at

min - minimum x

max - maximum x

ns - grid in x

savefilename - save to or restore from this savefile (pickle)

OUTPUT:

plot to output device

HISTORY:

2010-07-13 - Written - Bovy (NYU)

## Specific potentials

### Vertical Kuijken & Gilmore potential

```
class galpy.potential.KGPotential(K=1.15, F=0.03, D=1.8, amp=1.0)
```

Class representing the Kuijken & Gilmore (1989) potential

```
__init__(K=1.15, F=0.03, D=1.8, amp=1.0)
```

NAME: \_\_init\_\_

PURPOSE:

Initialize a KGPotential

INPUT:

K= K parameter

F= F parameter

D= D parameter

amp - an overall amplitude

OUTPUT:

instance

HISTORY:

2010-07-12 - Written - Bovy (NYU)

One-dimensional potentials can also be derived from 3D axisymmetric potentials as the vertical potential at a certain Galactocentric radius

### `galpy.potential.RZToverticalPotential`

`galpy.potential.RZToverticalPotential (RZPot, R)`

NAME:

RZToverticalPotential

PURPOSE:

convert a RZPotential to a vertical potential at a given R

INPUT:

RZPot - RZPotential instance or list of such instances

R - Galactocentric radius at which to evaluate the vertical potential

OUTPUT:

(list of) linearPotential instance(s)

HISTORY:

2010-07-21 - Written - Bovy (NYU)

## 2.3 DF

### 2.3.1 Two-dimensional Disk distribution functions

Distribution function for orbits in the plane of a galactic disk.

#### General instance routines

##### `galpy.df.diskdf.__call__`

`diskdf.__call__ (*args, **kwargs)`

NAME:

`__call__`

PURPOSE:

evaluate the distribution function

INPUT:

either an orbit instance, a list of such instances, or E,Lz

1.Orbit instance or list: a) Orbit instance alone: use vxvv member b) Orbit instance + t: call the Orbit instance (for list, each instance is called at t)

2.E - energy (/vo^2) L - angular momentum (/ro/vo)

3.array vxvv [3/4,nt]

KWARGS:

marginalizeVperp - marginalize over perpendicular velocity (only supported with 1a) for single orbits above)

marginalizeVlos - marginalize over line-of-sight velocity (only supported with 1a) for single orbits above)

nsigma= number of sigma to integrate over when marginalizing

+scipy.integrate.quad keywords

OUTPUT:

DF(orbit/E,L)

HISTORY:

2010-07-10 - Written - Bovy (NYU)

## galpy.df.diskdf.asymmetricdrift

diskdf.**asymmetricdrift**(*R*)

NAME:

asymmetricdrift

PURPOSE:

estimate the asymmetric drift ( $v_c$ -mean- $v\phi$ ) from an approximation to the Jeans equation

INPUT:

*R* - radius at which to calculate the asymmetric drift (/ $\rho_0$ )

OUTPUT:

asymmetric drift at *R*

HISTORY:

2011-04-02 - Written - Bovy (NYU)

## galpy.df.diskdf.kurtosisvR

diskdf.**kurtosisvR**(*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

NAME:

kurtosisvR

PURPOSE:

calculate excess kurtosis in  $v_R$  at *R* by marginalizing over velocity

INPUT:

*R* - radius at which to calculate  $\langle v_R \rangle$  (/ $\rho_0$ )

OPTIONAL INPUT:

*nsigma* - number of sigma to integrate the velocities over

KEYWORDS:

*romberg* - if True, use a romberg integrator (default: False)

OUTPUT:

kurtosisvR

HISTORY:

2011-12-07 - Written - Bovy (NYU)

### galpy.df.diskdf.kurtosisvT

diskdf.**kurtosisvT**(*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

NAME:

kurtosisvT

PURPOSE:

calculate excess kurtosis in vT at R by marginalizing over velocity

INPUT:

*R* - radius at which to calculate  $\langle vR \rangle$  (/ro)

OPTIONAL INPUT:

*nsigma* - number of sigma to integrate the velocities over

KEYWORDS:

*romberg* - if True, use a romberg integrator (default: False)

OUTPUT:

kurtosisvT

HISTORY:

2011-12-07 - Written - Bovy (NYU)

### galpy.df.diskdf.meanvR

diskdf.**meanvR**(*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

NAME:

meanvR

PURPOSE:

calculate  $\langle vR \rangle$  at R by marginalizing over velocity

INPUT:

*R* - radius at which to calculate  $\langle vR \rangle$  (/ro)

OPTIONAL INPUT:

*nsigma* - number of sigma to integrate the velocities over

KEYWORDS:

*romberg* - if True, use a romberg integrator (default: False)

OUTPUT:

$\langle vR \rangle$  at R

HISTORY:

2011-03-30 - Written - Bovy (NYU)

### galpy.df.diskdf.meanvT

diskdf.**meanvT** (*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

NAME:

meanvT

PURPOSE:

calculate  $\langle v_T \rangle$  at R by marginalizing over velocity

INPUT:

R - radius at which to calculate  $\langle v_T \rangle$  (/ro)

OPTIONAL INPUT:

nsigma - number of sigma to integrate the velocities over

KEYWORDS:

romberg - if True, use a romberg integrator (default: False)

OUTPUT:

$\langle v_T \rangle$  at R

HISTORY:

2011-03-30 - Written - Bovy (NYU)

### galpy.df.diskdf.oortA

diskdf.**oortA** (*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

NAME:

oortA

PURPOSE:

calculate the Oort function A

INPUT:

R - radius at which to calculate A (/ro)

OPTIONAL INPUT:

nsigma - number of sigma to integrate the velocities over

KEYWORDS:

romberg - if True, use a romberg integrator (default: False)

OUTPUT:

Oort A at R

HISTORY:

2011-04-19 - Written - Bovy (NYU)

BUGS:

could be made more efficient, e.g., surfacemass is calculated multiple times

### galpy.df.diskdf.oortB

diskdf.**oortB** (*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

NAME:

oortB

PURPOSE:

calculate the Oort function B

INPUT:

*R* - radius at which to calculate B (/ro)

OPTIONAL INPUT:

*nsigma* - number of sigma to integrate the velocities over

KEYWORDS:

*romberg* - if True, use a romberg integrator (default: False)

OUTPUT:

Oort B at R

HISTORY:

2011-04-19 - Written - Bovy (NYU)

BUGS:

could be made more efficient, e.g., surfacemass is calculated multiple times

### galpy.df.diskdf.oortC

diskdf.**oortC** (*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

NAME:

oortC

PURPOSE:

calculate the Oort function C

INPUT:

*R* - radius at which to calculate C (/ro)

OPTIONAL INPUT:

*nsigma* - number of sigma to integrate the velocities over

KEYWORDS:

*romberg* - if True, use a romberg integrator (default: False)

OUTPUT:

Oort C at R

HISTORY:

2011-04-19 - Written - Bovy (NYU)

BUGS:

could be made more efficient, e.g., surfacemass is calculated multiple times we know this is zero, but it is calculated anyway (bug or feature?)

## galpy.df.diskdf.oortK

diskdf.**oortK**(*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

NAME:

oortK

PURPOSE:

calculate the Oort function K

INPUT:

*R* - radius at which to calculate K (/ro)

OPTIONAL INPUT:

*nsigma* - number of sigma to integrate the velocities over

KEYWORDS:

*romberg* - if True, use a romberg integrator (default: False)

OUTPUT:

Oort K at R

HISTORY:

2011-04-19 - Written - Bovy (NYU)

BUGS:

could be made more efficient, e.g., surfacemass is calculated multiple times we know this is zero, but it is calculated anyway (bug or feature?)

## galpy.df.diskdf.sigma2surfacemass

diskdf.**sigma2surfacemass**(*R*, *romberg=False*, *nsigma=None*, *relative=False*)

NAME:

sigma2surfacemass

PURPOSE:

calculate the product  $\sigma_R^2 \times$  surface-mass at R by marginalizing over velocity

INPUT:

*R* - radius at which to calculate the  $\sigma_R^2 \times$  surfacemass density (/ro)

OPTIONAL INPUT:

*nsigma* - number of sigma to integrate the velocities over

KEYWORDS:

*romberg* - if True, use a romberg integrator (default: False)

**OUTPUT:**

sigma\_R^2 x surface-mass at R

**HISTORY:**

2010-03-XX - Written - Bovy (NYU)

**galpy.df.diskdf.sigma2**

diskdf.**sigma2** (*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

**NAME:**

sigma2

**PURPOSE:**

calculate sigma\_R^2 at R by marginalizing over velocity

**INPUT:**

*R* - radius at which to calculate sigma\_R^2 density (/ro)

**OPTIONAL INPUT:**

*nsigma* - number of sigma to integrate the velocities over

**KEYWORDS:**

*romberg* - if True, use a romberg integrator (default: False)

**OUTPUT:**

sigma\_R^2 at R

**HISTORY:**

2010-03-XX - Written - Bovy (NYU)

**galpy.df.diskdf.sigmaR2**

diskdf.**sigmaR2** (*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

**NAME:**

sigmaR2 (duplicate of sigma2 for consistency)

**PURPOSE:**

calculate sigma\_R^2 at R by marginalizing over velocity

**INPUT:**

*R* - radius at which to calculate sigma\_R^2 (/ro)

**OPTIONAL INPUT:**

*nsigma* - number of sigma to integrate the velocities over

**KEYWORDS:**

*romberg* - if True, use a romberg integrator (default: False)

**OUTPUT:**

sigma\_R^2 at R

HISTORY:

2011-03-30 - Written - Bovy (NYU)

**galpy.df.diskdf.sigmaT2**

diskdf.**sigmaT2** ( $R$ ,  $romberg=False$ ,  $nsigma=None$ ,  $\phi=0.0$ )

NAME:

sigmaT2

PURPOSE:

calculate  $\sigma_T^2$  at  $R$  by marginalizing over velocity

INPUT:

$R$  - radius at which to calculate  $\sigma_T^2$  (/ $r_0$ )

OPTIONAL INPUT:

$nsigma$  - number of sigma to integrate the velocities over

KEYWORDS:

$romberg$  - if True, use a romberg integrator (default: False)

OUTPUT:

$\sigma_T^2$  at  $R$

HISTORY:

2011-03-30 - Written - Bovy (NYU)

**galpy.df.diskdf.skewvR**

diskdf.**skewvR** ( $R$ ,  $romberg=False$ ,  $nsigma=None$ ,  $\phi=0.0$ )

NAME:

skewvR

PURPOSE:

calculate skew in  $v_R$  at  $R$  by marginalizing over velocity

INPUT:

$R$  - radius at which to calculate  $\langle v_R \rangle$  (/ $r_0$ )

OPTIONAL INPUT:

$nsigma$  - number of sigma to integrate the velocities over

KEYWORDS:

$romberg$  - if True, use a romberg integrator (default: False)

OUTPUT:

skewvR

HISTORY:

2011-12-07 - Written - Bovy (NYU)

**galpy.df.diskdf.skewvT**

diskdf.**skewvT** (*R*, *romberg=False*, *nsigma=None*, *phi=0.0*)

NAME:

skewvT

PURPOSE:

calculate skew in vT at R by marginalizing over velocity

INPUT:

*R* - radius at which to calculate  $\langle vR \rangle$  (/ro)

OPTIONAL INPUT:

*nsigma* - number of sigma to integrate the velocities over

KEYWORDS:

*romberg* - if True, use a romberg integrator (default: False)

OUTPUT:

skewvT

HISTORY:

2011-12-07 - Written - Bovy (NYU)

**galpy.df.diskdf.surfacemass**

diskdf.**surfacemass** (*R*, *romberg=False*, *nsigma=None*, *relative=False*)

NAME:

surfacemass

PURPOSE:

calculate the surface-mass at R by marginalizing over velocity

INPUT:

*R* - radius at which to calculate the surfacemass density (/ro)

OPTIONAL INPUT:

*nsigma* - number of sigma to integrate the velocities over

KEYWORDS:

*romberg* - if True, use a romberg integrator (default: False)

OUTPUT:

surface mass at R

HISTORY:

2010-03-XX - Written - Bovy (NYU)

## galpy.df.diskdf.surfacemassLOS

diskdf.**surfacemassLOS** ( $d$ ,  $l$ ,  $deg=True$ ,  $target=True$ ,  $romberg=False$ ,  $nsigma=None$ ,  $relative=None$ )

NAME:

surfacemassLOS

PURPOSE:

evaluate the surface mass along the LOS given l and d

INPUT:

$d$  - distance along the line of sight

$l$  - Galactic longitude (in deg, unless  $deg=False$ )

OPTIONAL INPUT:

$nsigma$  - number of sigma to integrate the velocities over

KEYWORDS:

$target=True$ , use target surfacemass (default)

$romberg=True$ , use a romberg integrator (default: False)

$deg=False$ ,  $l$  is in radians

OUTPUT:

$\Sigma(d,l)$

HISTORY:

2011-03-24 - Written - Bovy (NYU)

## galpy.df.diskdf.targetSigma2

diskdf.**targetSigma2** ( $R$ ,  $log=False$ )

NAME:

targetSigma2

PURPOSE:

evaluate the target  $\Sigma_R(R)$

INPUT:

$R$  - radius at which to evaluate ( $/r_\odot$ )

OUTPUT:

target  $\Sigma_R(R)$

$log=True$ , return the log (default: False)

HISTORY:

2010-03-28 - Written - Bovy (NYU)

**galpy.df.diskdf.targetSurfacemass**

diskdf.**targetSurfacemass** ( $R$ ,  $\log=False$ )

NAME:

targetSurfacemass

PURPOSE:

evaluate the target surface mass at R

INPUT:

$R$  - radius at which to evaluate

$\log$  - if True, return the log (default: False)

OUTPUT:

$\Sigma(R)$

HISTORY:

2010-03-28 - Written - Bovy (NYU)

**galpy.df.diskdf.targetSurfacemassLOS**

diskdf.**targetSurfacemassLOS** ( $d$ ,  $l$ ,  $\log=False$ ,  $deg=True$ )

NAME:

targetSurfacemassLOS

PURPOSE:

evaluate the target surface mass along the LOS given l and d

INPUT:

$d$  - distance along the line of sight

$l$  - Galactic longitude (in deg, unless deg=False)

$deg$ = if False, l is in radians

$\log$  - if True, return the log (default: False)

OUTPUT:

$\Sigma(d,l)$

HISTORY:

2011-03-23 - Written - Bovy (NYU)

**galpy.df.diskdf.vmomentsurfacemass**

diskdf.**vmomentsurfacemass** ( $R$ ,  $n$ ,  $m$ ,  $romberg=False$ ,  $nsigma=None$ ,  $relative=False$ ,  $phi=0.0$ ,  $de-$   
 $riv=None$ )

NAME:

vmomentsurfacemass

PURPOSE:

calculate the an arbitrary moment of the velocity distribution at R times the surfacemass

INPUT:

R - radius at which to calculate the moment(/ro)  
n -  $vR^n$   
m -  $vT^m$

OPTIONAL INPUT:

nsigma - number of sigma to integrate the velocities over

KEYWORDS:

romberg - if True, use a romberg integrator (default: False)  
deriv= None, ‘R’, or ‘phi’: calculates derivative of the moment wrt R or phi

OUTPUT:

$\langle vR^n vT^m \times \text{surface-mass} \rangle$  at R

HISTORY:

2011-03-30 - Written - Bovy (NYU)

## Sampling routines

### galpy.df.diskdf.sample

```
diskdf.sample(n=1, rrange=None, returnROrbit=True, returnOrbit=False, nphi=1.0, los=None, los-
deg=True, nsigma=None, maxd=None, target=True)
```

NAME:

sample

PURPOSE:

sample  $n * n\phi$  points from this DF

INPUT:

n - number of desired sample (specifying this rather than calling this routine n times is more efficient)  
rrange - if you only want samples in this range, set this keyword (only works when asking for an (RZ)Orbit

**returnROrbit - if True, return a planarROrbit instance:** [R,vR,vT] (default)

returnOrbit - if True, return a planarOrbit instance (including phi)

nphi - number of azimuths to sample for each E,L

los= line of sight sampling along this line of sight

losdeg= los in degrees? (default=True)

target= if True, use target surface mass and sigma2 profiles (default=True)

nsigma= number of sigma to rejection-sample on

maxd= maximum distance to consider (for the rejection sampling)

OUTPUT:

$n * n\phi$  list of [[E,Lz],...] or list of planar(R)Orbits

**CAUTION: lists of EL need to be post-processed to account for the**  $\kappa/\omega_R$  **discrepancy**

**HISTORY:**

2010-07-10 - Started - Bovy (NYU)

**galpy.df.diskdf.sampledSurfacemassLOS**

diskdf . **sampledSurfacemassLOS** (*l*, *n*=1, *maxd*=None, *target*=True)

**NAME:**

sampledSurfacemassLOS

**PURPOSE:**

sample a distance along the line of sight

**INPUT:**

*l* - Galactic longitude (in rad)

*n*= number of distances to sample

*maxd*= maximum distance to consider (for the rejection sampling)

*target*= if True, sample from the ‘target’ surface mass density, rather than the actual surface mass density (default=True)

**OUTPUT:**

list of samples

**HISTORY:**

2011-03-24 - Written - Bovy (NYU)

**hhgalpy.df.diskdf.sampleLOS**

diskdf . **sampleLOS** (*los*, *n*=1, *deg*=True, *maxd*=None, *nsigma*=None, *target*=True)

**NAME:**

sampleLOS

**PURPOSE:**

sample along a given LOS

**INPUT:**

*los* - line of sight (in deg, unless *deg*=False)

*n*= number of desired samples

*deg*= los in degrees? (default=True)

**target=** if True, use target surface mass and sigma2 profiles (default=True)

**OUTPUT:**

returns list of Orbit

**BUGS:** *target=False* uses target distribution for derivatives (this is a detail)

**HISTORY:**

2011-03-24 - Started - Bovy (NYU)

**galpy.df.diskdf.sampleVRVT**

`diskdf.sampleVRVT(R, n=1, nsigma=None, target=True)`

NAME:

sampleVRVT

PURPOSE:

sample a radial and azimuthal velocity at R

INPUT:

R - Galactocentric distance

n= number of distances to sample

nsigma= number of sigma to rejection-sample on

target= if True, sample using the ‘target’ sigma\_R rather than the actual sigma\_R (default=True)

OUTPUT:

list of samples

BUGS:

should use the fact that vR and vT separate

HISTORY:

2011-03-24 - Written - Bovy (NYU)

## Specific distribution functions

### Dehnen DF

```
class galpy.df.dehnendf(surfaceSigma=<class galpy.df_src.surfaceSigmaProfile.expSurfaceSigmaProfile
                           at 0x6970a78>, profileParams=(0.3333333333333333, 1.0, 0.2), correct=False, beta=0.0, **kwargs)
```

Dehnen’s ‘new’ df

```
__init__(surfaceSigma=<class galpy.df_src.surfaceSigmaProfile.expSurfaceSigmaProfile
          at 0x6970a78>, profileParams=(0.3333333333333333, 1.0, 0.2), correct=False, beta=0.0,
          **kwargs)
```

NAME: `__init__`

PURPOSE: Initialize a Dehnen ‘new’ DF

INPUT:

**surfaceSigma - instance or class name of the target** surface density and sigma\_R profile (default: both exponential)

**profileParams - parameters of the surface and sigma\_R profile:** (xD,xS,Sro) where

xD - disk surface mass scalelength / Ro

xS - disk velocity dispersion scalelength / Ro

Sro - disk velocity dispersion at Ro (/vo)

Directly given to the ‘surfaceSigmaProfile class, so could be anything that class takes

beta - power-law index of the rotation curve  
 correct - if True, correct the DF  
 +DFcorrection kwargs (except for those already specified)

**OUTPUT:**

instance

**HISTORY:**

2010-03-10 - Written - Bovy (NYU)

**Shu DF**

```
class galpy.df.shudf(surfaceSigma=<class galpy.df_src.surfaceSigmaProfile.expSurfaceSigmaProfile at
0x6970a78>, profileParams=(0.3333333333333333, 1.0, 0.2), correct=False,
beta=0.0, **kwargs)
```

Shu's df (1969)

```
__init__(surfaceSigma=<class      galpy.df_src.surfaceSigmaProfile.expSurfaceSigmaProfile      at
0x6970a78>, profileParams=(0.3333333333333333, 1.0, 0.2), correct=False, beta=0.0,
**kwargs)
```

**NAME:** \_\_init\_\_

**PURPOSE:** Initialize a Shu DF

**INPUT:**

**surfaceSigma - instance or class name of the target** surface density and sigma\_R profile (default: both exponential)

**profileParams - parameters of the surface and sigma\_R profile:** (xD,xS,Sro) where

xD - disk surface mass scalelength / Ro

xS - disk velocity dispersion scalelength / Ro

Sro - disk velocity dispersion at Ro (/vo)

Directly given to the ‘surfaceSigmaProfile class, so could be anything that class takes

beta - power-law index of the rotation curve

correct - if True, correct the DF

+DFcorrection kwargs (except for those already specified)

**OUTPUT:**

instance

**HISTORY:**

2010-05-09 - Written - Bovy (NYU)

**2.3.2 Three-dimensional Disk distribution functions**

Distribution functions for orbits in galactic disks, including the vertical motion for stars reaching large heights above the plane. Currently only the *quasi-isothermal DF*.

## General instance routines

### galpy.df.quasiisothermaldf.\_\_call\_\_

quasiisothermaldf.\_\_call\_\_(\*args, \*\*kwargs)

**NAME:** \_\_call\_\_

**PURPOSE:** return the DF

**INPUT:**

**Either:**

a)(jr,lz,jz) tuple

where: jr - radial action lz - z-component of angular momentum jz - vertical action

2. R,vR,vT,z,vz

3. Orbit instance: initial condition used if that's it, orbit(t) if there is a time given as well

log= if True, return the natural log

+scipy.integrate.quadrature kwargs

func= function of (jr,lz,jz) to multiply f with (useful for moments)

**OUTPUT:** value of DF

**HISTORY:** 2012-07-25 - Written - Bovy ([IAS@MPIA](#))

**NOTE:** For Miyamoto-Nagai/adiabatic approximation this seems to take about 30 ms / evaluation in the extended Solar neighborhood For a MWPotential/adiabatic approximation this takes about 50 ms / evaluation in the extended Solar neighborhood

For adiabatic-approximation grid this seems to take about 0.67 to 0.75 ms / evaluation in the extended Solar neighborhood (includes some out of the grid)

up to 200x faster when called with vector R,vR,vT,z,vz

### galpy.df.quasiisothermaldf.density

quasiisothermaldf.density(R, z, nsigma=None, mc=False, nmc=10000, gl=True, ngl=10, \*\*kwargs)

**NAME:** density

**PURPOSE:** calculate the density at R,z by marginalizing over velocity

**INPUT:**

R - radius at which to calculate the density

z - height at which to calculate the density

**OPTIONAL INPUT:** nsigma - number of sigma to integrate the velocities over

scipy.integrate.tplquad kwargs epsabs and epsrel

mc= if True, calculate using Monte Carlo integration

nmc= if mc, use nmc samples

gl= if True, calculate using Gauss-Legendre integration  
ngl= if gl, use ngl-th order Gauss-Legendre integration for each dimension

**OUTPUT:** density at (R,z)

**HISTORY:** 2012-07-26 - Written - Bovy ([IAS@MPIA](#))

### galpy.df.quasiisothermaldf.estimate\_hr

quasiisothermaldf.**estimate\_hr**( $R, z=0.0, dR=1e-08, \text{**kwargs}$ )

**NAME:** estimate\_hr

**PURPOSE:** estimate the exponential scale length at R

**INPUT:** R - Galactocentric radius

z= height (default: 0 pc)

dR- range in R to use

density kwargs

**OUTPUT:** estimated hR

**HISTORY:** 2012-09-11 - Written - Bovy (IAS) 2013-01-28 - Re-written - Bovy

### galpy.df.quasiisothermaldf.estimate\_hsr

quasiisothermaldf.**estimate\_hsr**( $R, z=0.0, dR=1e-08, \text{**kwargs}$ )

**NAME:** estimate\_hsr

**PURPOSE:** estimate the exponential scale length of the radial dispersion at R

**INPUT:** R - Galactocentric radius

z= height (default: 0 pc)

dR- range in R to use

density kwargs

**OUTPUT:** estimated hsR

**HISTORY:** 2013-03-08 - Written - Bovy (IAS)

### galpy.df.quasiisothermaldf.estimate\_hsz

quasiisothermaldf.**estimate\_hsz**( $R, z=0.0, dR=1e-08, \text{**kwargs}$ )

**NAME:** estimate\_hsz

**PURPOSE:** estimate the exponential scale length of the vertical dispersion at R

**INPUT:** R - Galactocentric radius

z= height (default: 0 pc)

dR- range in R to use

density kwargs

**OUTPUT:** estimated hsz

**HISTORY:** 2013-03-08 - Written - Bovy (IAS)

### galpy.df.quasiisothermaldf.estimate\_hz

quasiisothermaldf.**estimate\_hz**(*R, z, dz=1e-08, \*\*kwargs*)

**NAME:** estimate\_hz

**PURPOSE:** estimate the exponential scale height at R

**INPUT:** R - Galactocentric radius

dz - z range to use

density kwargs

**OUTPUT:** estimated hz

**HISTORY:** 2012-08-30 - Written - Bovy (IAS)

2013-01-28 - Re-written - Bovy

### galpy.df.quasiisothermaldf.jmomentdensity

quasiisothermaldf.**jmomentdensity**(*R, z, n, m, o, nsigma=None, mc=True, nmc=10000, \_returnmc=False, \_vrs=None, \_vts=None, \_vzs=None, \*\*kwargs*)

**NAME:** jmomentdensity

**PURPOSE:** calculate the an arbitrary moment of an action of the velocity distribution at R times the surfacmass

**INPUT:** R - radius at which to calculate the moment(/ro)

n - jr^n

m - lz^m

o - jz^o

**OPTIONAL INPUT:** nsigma - number of sigma to integrate the velocities over (when doing explicit numerical integral)

mc= if True, calculate using Monte Carlo integration

nmc= if mc, use nmc samples

**OUTPUT:** <jr^n lz^m jz^o x density> at R

**HISTORY:** 2012-08-09 - Written - Bovy ([IAS@MPIA](#))

### galpy.df.quasiisothermaldf.meanjr

quasiisothermaldf.**meanjr**(*R, z, nsigma=None, mc=True, nmc=10000, \*\*kwargs*)

**NAME:** meanjr

**PURPOSE:** calculate the mean radial action by marginalizing over velocity

**INPUT:**

R - radius at which to calculate this

z - height at which to calculate this

**OPTIONAL INPUT:**

nsigma - number of sigma to integrate the velocities over

scipy.integrate.tplquad kwargs epsabs and epsrel

mc= if True, calculate using Monte Carlo integration

nmc= if mc, use nmc samples

**OUTPUT:** meanjr

**HISTORY:** 2012-08-09 - Written - Bovy ([IAS@MPIA](#))

## galpy.df.quasiisothermaldf.meanjz

quasiisothermaldf.**meanjz** ( $R, z, nsigma=None, mc=True, nmc=10000, \text{**kwargs}$ )

**NAME:** meanjz

**PURPOSE:** calculate the mean vertical action by marginalizing over velocity

**INPUT:**

R - radius at which to calculate this

z - height at which to calculate this

**OPTIONAL INPUT:**

nsigma - number of sigma to integrate the velocities over

scipy.integrate.tplquad kwargs epsabs and epsrel

mc= if True, calculate using Monte Carlo integration

nmc= if mc, use nmc samples

**OUTPUT:** meanjz

**HISTORY:** 2012-08-09 - Written - Bovy ([IAS@MPIA](#))

## galpy.df.quasiisothermaldf.meanlz

quasiisothermaldf.**meanlz** ( $R, z, nsigma=None, mc=True, nmc=10000, \text{**kwargs}$ )

**NAME:** meanlz

**PURPOSE:** calculate the mean angular momentum by marginalizing over velocity

**INPUT:**

R - radius at which to calculate this

z - height at which to calculate this

**OPTIONAL INPUT:**

nsigma - number of sigma to integrate the velocities over  
scipy.integrate.tplquad kwargs epsabs and epsrel  
mc= if True, calculate using Monte Carlo integration  
nmc= if mc, use nmc samples

**OUTPUT:** meanlz

**HISTORY:** 2012-08-09 - Written - Bovy ([IAS@MPIA](#))

### **galpy.df.quasiisothermaldf.meanvR**

`quasiisothermaldf.meanvR(R, z, nsigma=None, mc=False, nmc=10000, gl=True, ngl=10, **kwargs)`

**NAME:** meanvR

**PURPOSE:** calculate the mean radial velocity by marginalizing over velocity

**INPUT:**

R - radius at which to calculate this  
z - height at which to calculate this

**OPTIONAL INPUT:**

nsigma - number of sigma to integrate the velocities over  
scipy.integrate.tplquad kwargs epsabs and epsrel  
mc= if True, calculate using Monte Carlo integration  
nmc= if mc, use nmc samples  
gl= if True, calculate using Gauss-Legendre integration  
ngl= if gl, use ngl-th order Gauss-Legendre integration for each dimension

**OUTPUT:** meanvR

**HISTORY:** 2012-12-23 - Written - Bovy (IAS)

### **galpy.df.quasiisothermaldf.meanvT**

`quasiisothermaldf.meanvT(R, z, nsigma=None, mc=False, nmc=10000, gl=True, ngl=10, **kwargs)`  
**NAME:**

meanvT

**PURPOSE:**

calculate the mean rotational velocity by marginalizing over velocity

**INPUT:**

R - radius at which to calculate this  
z - height at which to calculate this

**OPTIONAL INPUT:**

nsigma - number of sigma to integrate the velocities over  
scipy.integrate.tplquad kwargs epsabs and epsrel  
mc= if True, calculate using Monte Carlo integration  
nmc= if mc, use nmc samples  
gl= if True, calculate using Gauss-Legendre integration  
ngl= if gl, use ngl-th order Gauss-Legendre integration for each dimension

**OUTPUT:** meanvT

**HISTORY:** 2012-07-30 - Written - Bovy ([IAS@MPIA](#))

### galpy.df.quasiisothermaldf.meanvz

quasiisothermaldf.**meanvz** ( $R, z, nsigma=None, mc=False, nmc=10000, gl=True, ngl=10, **kwargs$ )

**NAME:** meanvz

**PURPOSE:** calculate the mean vertical velocity by marginalizing over velocity

**INPUT:**

$R$  - radius at which to calculate this

$z$  - height at which to calculate this

**OPTIONAL INPUT:**

nsigma - number of sigma to integrate the velocities over

scipy.integrate.tplquad kwargs epsabs and epsrel

mc= if True, calculate using Monte Carlo integration

nmc= if mc, use nmc samples

gl= if True, calculate using Gauss-Legendre integration

ngl= if gl, use ngl-th order Gauss-Legendre integration for each dimension

**OUTPUT:** meanvz

**HISTORY:** 2012-12-23 - Written - Bovy (IAS)

### galpy.df.quasiisothermaldf.pvR

quasiisothermaldf.**pvR** ( $vR, R, z, gl=True, ngl=20$ )

**NAME:** pvR

**PURPOSE:** calculate the marginalized vR probability at this location (NOT normalized by the density)

**INPUT:**

$vR$  - radial velocity (/ $v_o$ )

$R$  - radius (/ $r_o$ )

$z$  - height (/ $r_o$ )

gl - use Gauss-Legendre integration (True, currently the only option)

ngl - order of Gauss-Legendre integration

**OUTPUT:** p(vR,R,z)

**HISTORY:** 2012-12-22 - Written - Bovy (IAS)

### galpy.df.quasiisothermaldf.pvRvT

quasiisothermaldf.**pvRvT**(vR, vT, R, z, gl=True, ngl=20)

**NAME:** pvRvT

**PURPOSE:** calculate the marginalized (vR,vT) probability at this location (NOT normalized by the density)

**INPUT:**

vR - radial velocity (/vo)

vT - tangential velocity (/vo)

R - radius (/ro)

z - height (/ro)

gl - use Gauss-Legendre integration (True, currently the only option)

ngl - order of Gauss-Legendre integration

**OUTPUT:** p(vR,vT,R,z)

**HISTORY:** 2013-01-02 - Written - Bovy (IAS)

### galpy.df.quasiisothermaldf.pvRvz

quasiisothermaldf.**pvRvz**(vR, vz, R, z, gl=True, ngl=20)

**NAME:** pvR

**PURPOSE:** calculate the marginalized (vR,vz) probability at this location (NOT normalized by the density)

**INPUT:**

vR - radial velocity (/vo)

vz - vertical velocity (/vo)

R - radius (/ro)

z - height (/ro)

gl - use Gauss-Legendre integration (True, currently the only option)

ngl - order of Gauss-Legendre integration

**OUTPUT:** p(vR,vz,R,z)

**HISTORY:** 2013-01-02 - Written - Bovy (IAS)

**galpy.df.quasiisothermaldf.pvT**

`quasiisothermaldf.pvT(vT, R, z, gl=True, ngl=20)`

**NAME:** pvT

**PURPOSE:** calculate the marginalized vT probability at this location (NOT normalized by the density)

**INPUT:**

vT - tangential velocity (/vo)

R - radius (/ro)

z - height (/ro)

gl - use Gauss-Legendre integration (True, currently the only option)

ngl - order of Gauss-Legendre integration

**OUTPUT:** p(vT,R,z)

**HISTORY:** 2012-12-22 - Written - Bovy (IAS)

**galpy.df.quasiisothermaldf.pvTvz**

`quasiisothermaldf.pvTvz(vT, vz, R, z, gl=True, ngl=20)`

**NAME:** pvTvz

**PURPOSE:** calculate the marginalized (vT,vz) probability at this location (NOT normalized by the density)

**INPUT:**

vT - tangential velocity (/vo)

vz - vertical velocity (/vo)

R - radius (/ro)

z - height (/ro)

gl - use Gauss-Legendre integration (True, currently the only option)

ngl - order of Gauss-Legendre integration

**OUTPUT:** p(vT,vz,R,z)

**HISTORY:** 2012-12-22 - Written - Bovy (IAS)

**galpy.df.quasiisothermaldf.pvz**

`quasiisothermaldf.pvz(vz, R, z, gl=True, ngl=20, _return_actions=False, _jr=None, _lz=None, _jz=None, _return_freqs=False, _rg=None, _kappa=None, _nu=None, _Omega=None, _sigmaR1=None)`

**NAME:** pvz

**PURPOSE:** calculate the marginalized vz probability at this location (NOT normalized by the density)

**INPUT:**  $v_z$  - vertical velocity ( $/v_o$ )  
R - radius ( $/r_o$ )  
z - height ( $/r_o$ )  
gl - use Gauss-Legendre integration (True, currently the only option)  
ngl - order of Gauss-Legendre integration  
**OUTPUT:**  $p(v_z, R, z)$   
**HISTORY:** 2012-12-22 - Written - Bovy (IAS)

### `galpy.df.quasiisothermaldf.sampleV`

`quasiisothermaldf.sampleV(R, z, n=1)`

**NAME:** sampleV  
**PURPOSE:** sample a radial, azimuthal, and vertical velocity at R,z  
**INPUT:**  
R - Galactocentric distance  
z - height  
n= number of distances to sample  
**OUTPUT:** list of samples  
**HISTORY:** 2012-12-17 - Written - Bovy (IAS)

### `galpy.df.quasiisothermaldf.sigmaR2`

`quasiisothermaldf.sigmaR2(R, z, nsigma=None, mc=False, nmc=10000, gl=True, ngl=10, **kwargs)`

**NAME:** sigmaR2  
**PURPOSE:** calculate  $\sigma_R^2$  by marginalizing over velocity  
**INPUT:**  
R - radius at which to calculate this  
z - height at which to calculate this  
**OPTIONAL INPUT:**  
nsigma - number of sigma to integrate the velocities over  
scipy.integrate.tplquad kwargs epsabs and epsrel  
mc= if True, calculate using Monte Carlo integration  
nmc= if mc, use nmc samples  
gl= if True, calculate using Gauss-Legendre integration  
ngl= if gl, use ngl-th order Gauss-Legendre integration for each dimension  
**OUTPUT:**  $\sigma_R^2$

**HISTORY:** 2012-07-30 - Written - Bovy ([IAS@MPIA](#))

### **galpy.df.quasiisothermaldf.sigmaRz**

`quasiisothermaldf.sigmaRz(R, z, nsigma=None, mc=False, nmc=10000, gl=True, ngl=10, **kwargs)`

**NAME:** sigmaRz

**PURPOSE:** calculate sigma\_RZ^2 by marginalizing over velocity

**INPUT:**

*R* - radius at which to calculate this

*z* - height at which to calculate this

**OPTIONAL INPUT:**

*nsigma* - number of sigma to integrate the velocities over

`scipy.integrate.tplquad` kwargs *epsabs* and *epsrel*

*mc*= if True, calculate using Monte Carlo integration

*nmc*= if *mc*, use *nmc* samples

*gl*= if True, calculate using Gauss-Legendre integration

*ngl*= if *gl*, use *ngl*-th order Gauss-Legendre integration for each dimension

**OUTPUT:** sigma\_Rz^2

**HISTORY:** 2012-07-30 - Written - Bovy ([IAS@MPIA](#))

### **galpy.df.quasiisothermaldf.sigmaT2**

`quasiisothermaldf.sigmaT2(R, z, nsigma=None, mc=False, nmc=10000, gl=True, ngl=10, **kwargs)`

**NAME:** sigmaT2

**PURPOSE:** calculate sigma\_T^2 by marginalizing over velocity

**INPUT:**

*R* - radius at which to calculate this

*z* - height at which to calculate this

**OPTIONAL INPUT:**

*nsigma* - number of sigma to integrate the velocities over

`scipy.integrate.tplquad` kwargs *epsabs* and *epsrel*

*mc*= if True, calculate using Monte Carlo integration

*nmc*= if *mc*, use *nmc* samples

*gl*= if True, calculate using Gauss-Legendre integration

*ngl*= if *gl*, use *ngl*-th order Gauss-Legendre integration for each dimension

**OUTPUT:** sigma\_T^2

**HISTORY:** 2012-07-30 - Written - Bovy ([IAS@MPIA](#))

### **galpy.df.quasiisothermaldf.sigmaz2**

`quasiisothermaldf.sigmaz2(R, z, nsigma=None, mc=False, nmc=10000, gl=True, ngl=10, **kwargs)`

**NAME:** sigmaz2

**PURPOSE:** calculate sigma\_z^2 by marginalizing over velocity

**INPUT:**

R - radius at which to calculate this

z - height at which to calculate this

**OPTIONAL INPUT:**

nsigma - number of sigma to integrate the velocities over

scipy.integrate.tplquad kwargs epsabs and epsrel

mc= if True, calculate using Monte Carlo integration

nmc= if mc, use nmc samples

gl= if True, calculate using Gauss-Legendre integration

ngl= if gl, use ngl-th order Gauss-Legendre integration for each dimension

**OUTPUT:** sigma\_z^2

**HISTORY:** 2012-07-30 - Written - Bovy ([IAS@MPIA](#))

### **galpy.df.quasiisothermaldf.surfacemass\_z**

`quasiisothermaldf.surfacemass_z(R, nz=7, zmax=1.0, fixed_quad=True, fixed_order=8, **kwargs)`

**NAME:** surfacemass\_z

**PURPOSE:** calculate the vertically-integrated surface density

**INPUT:** R - Galactocentric radius

fixed\_quad= if True (default), use Gauss-Legendre integration

fixed\_order= (20), order of GL integration to use

nz= number of zs to use to estimate

zmax=m minimum z to use

density kwargs

**OUTPUT:** Sigma(R)

**HISTORY:** 2012-08-30 - Written - Bovy (IAS)

**galpy.df.quasiisothermaldf.tilt**

```
quasiisothermaldf.tilt (R, z, nsigma=None, mc=False, nmc=10000, gl=True, ngl=10, **kwargs)
```

**NAME:** tilt

**PURPOSE:** calculate the tilt of the velocity ellipsoid by marginalizing over velocity

**INPUT:**

R - radius at which to calculate this

z - height at which to calculate this

**OPTIONAL INPUT:**

nsigma - number of sigma to integrate the velocities over

scipy.integrate.tplquad kwargs epsabs and epsrel

mc= if True, calculate using Monte Carlo integration

nmc= if mc, use nmc samples

gl= if True, calculate using Gauss-Legendre integration

ngl= if gl, use ngl-th order Gauss-Legendre integration for each dimension

**OUTPUT:** tilt in degree

**HISTORY:** 2012-12-23 - Written - Bovy (IAS)

**galpy.df.quasiisothermaldf.vmomentdensity**

```
quasiisothermaldf.vmomentdensity (R, z, n, m, o, nsigma=None, mc=False, nmc=10000,
                                  _returnnmc=False, _vrs=None, _vts=None, _vzs=None, _raw-
                                  gausssamples=False, gl=False, ngl=10, _returnngl=False,
                                  _glqeval=None, _return_actions=False, _jr=None,
                                  _lz=None, _jz=None, _return_freqs=False, _rg=None,
                                  _kappa=None, _nu=None, _Omega=None, _sigmaRI=None,
                                  _sigmazI=None, **kwargs)
```

**NAME:** vmomentdensity

**PURPOSE:** calculate the an arbitrary moment of the velocity distribution at R times the density

**INPUT:** R - radius at which to calculate the moment( $\rho_0$ )

n -  $v^2 R^n$

m -  $v^T M$

o -  $v^2 O$

**OPTIONAL INPUT:** nsigma - number of sigma to integrate the velocities over (when doing explicit numerical integral)

mc= if True, calculate using Monte Carlo integration

nmc= if mc, use nmc samples

gl= use Gauss-Legendre

\_returnngl= if True, return the evaluated DF

\_return\_actions= if True, return the evaluated actions (does not work with \_returngl currently)  
\_return\_freqs= if True, return the evaluated frequencies and rg (does not work with \_returngl currently)

**OUTPUT:** <vR^n vT^m x density> at R,z

**HISTORY:** 2012-08-06 - Written - Bovy ([IAS@MPIA](#))

## Specific distribution functions

### Quasi-isothermal DF

```
class galpy.df.quasiisothermaldf(hr, sr, sz, hsr, hsz, pot=None, aA=None, cutcounter=False,  
                                 _precomputerg=True, _precomputergrmax=None, _precomput-  
                                 ergnLz=51, ro=1.0, lo=0.0056818181818182)
```

Class that represents a ‘Binney’ quasi-isothermal DF

```
__init__(hr, sr, sz, hsr, hsz, pot=None, aA=None, cutcounter=False, _precomputerg=True, _precom-  
                                 putergrmax=None, _precomputergnLz=51, ro=1.0, lo=0.00568181818182)
```

NAME:

\_\_init\_\_

PURPOSE:

Initialize a quasi-isothermal DF

INPUT:

hr - radial scale length

sr - radial velocity dispersion at the solar radius

sz - vertical velocity dispersion at the solar radius

hsr - radial-velocity-dispersion scale length

hsz - vertical-velocity-dispersion scale length

pot= Potential instance or list thereof

aA= actionAngle instance used to convert (x,v) to actions

cutcounter= if True, set counter-rotating stars’ DF to zero

ro= reference radius for surface mass and sigmas

lo= reference angular momentum below where there are significant numbers of retrograde stars

OTHER INPUTS:

\_precomputerg= if True (default), pre-compute the rL(L)

\_precomputergrmax= if set, this is the maximum R for which to pre-compute rg (default: 5\*hr)

\_precomputergnLz if set, number of Lz to pre-compute rg for (default: 51)

OUTPUT:

object

HISTORY:

2012-07-25 - Started - Bovy ([IAS@MPIA](#))

## 2.4 actionAngle

### 2.4.1 General instance routines

Not necessarily supported for all different types of actionAngle calculations. These have extra arguments for different actionAngle modules, so check the documentation of the module-specific functions for more info (e.g., `?actionAngleIsochrone.__call__`)

#### `galpy.actionAngle.actionAngle.__call__`

`actionAngle.__call__(*args, **kwargs)`

**NAME:** `__call__`

**PURPOSE:** evaluate the actions ( $j_r, l_z, j_z$ )

**INPUT:**

Either:

1.R,vR,vT,z,vz:

(a)floats: phase-space value for single object

(b)numpy.ndarray: [N] phase-space values for N objects

(c)numpy.ndarray: [N,M] phase-space values for N objects at M times

2.Orbit instance or list thereof; can be integrated already

**OUTPUT:** ( $j_r, l_z, j_z$ )

**HISTORY:** 2014-01-03 - Written for top level - Bovy (IAS)

#### `galpy.actionAngle.actionAngle.actionsFreqs`

`actionAngle.actionsFreqs(*args, **kwargs)`

**NAME:** `actionsFreqs`

**PURPOSE:** evaluate the actions and frequencies ( $j_r, l_z, j_z, \Omega_{\text{gar}}, \Omega_{\text{gaphi}}, \Omega_{\text{gaz}}$ )

**INPUT:**

Either:

1.R,vR,vT,z,vz:

(a)floats: phase-space value for single object

(b)numpy.ndarray: [N] phase-space values for N objects

(c)numpy.ndarray: [N,M] phase-space values for N objects at M times

2.Orbit instance or list thereof; can be integrated already

**OUTPUT:** ( $j_r, l_z, j_z, \Omega_{\text{gar}}, \Omega_{\text{gaphi}}, \Omega_{\text{gaz}}$ )

**HISTORY:** 2014-01-03 - Written for top level - Bovy (IAS)

## galpy.actionAngle.actionAngle.actionsFreqsAngles

`actionAngle.actionsFreqsAngles (*args, **kwargs)`

**NAME:** actionsFreqsAngles

**PURPOSE:** evaluate the actions, frequencies, and angles ( $j_r, l_z, j_z, \Omega_{\text{M}}, \Omega_{\text{M}\phi}, \Omega_{\text{M}\alpha}, \text{angler}, \text{anglephi}, \text{anglez}$ )

**INPUT:**

Either:

1.R,vR,vT,z,vz:

(a)floats: phase-space value for single object

(b)numpy.ndarray: [N] phase-space values for N objects

(c)numpy.ndarray: [N,M] phase-space values for N objects at M times

2.Orbit instance or list thereof; can be integrated already

**OUTPUT:** ( $j_r, l_z, j_z, \Omega_{\text{M}}, \Omega_{\text{M}\phi}, \Omega_{\text{M}\alpha}, \text{angler}, \text{anglephi}, \text{anglez}$ )

**HISTORY:** 2014-01-03 - Written for top level - Bovy (IAS)

## 2.4.2 Specific actionAngle modules

### actionAngleIsochrone

`class galpy.actionAngle.actionAngleIsochrone (*args, **kwargs)`

Action-angle formalism for the isochrone potential, on the  $J\phi, J\theta$  system of Binney & Tremaine (2008)

`__init__ (*args, **kwargs)`

**NAME:** \_\_init\_\_

**PURPOSE:** initialize an actionAngleIsochrone object

**INPUT:** Either:

b= scale parameter of the isochrone parameter

ip= instance of a IsochronePotential

**OUTPUT:** HISTORY:

2013-09-08 - Written - Bovy (IAS)

### actionAngleSpherical

`class galpy.actionAngle.actionAngleSpherical (*args, **kwargs)`

Action-angle formalism for spherical potentials

`__init__ (*args, **kwargs)`

**NAME:** \_\_init\_\_

**PURPOSE:** initialize an actionAngleSpherical object

**INPUT:** pot= a Spherical potential

**OUTPUT:** HISTORY:

---

2013-12-28 - Written - Bovy (IAS)

### **actionAngleAdiabatic**

```
class galpy.actionAngle.actionAngleAdiabatic(*args, **kwargs)
    Action-angle formalism for axisymmetric potentials using the adiabatic approximation
```

```
__init__(*args, **kwargs)
```

**NAME:** \_\_init\_\_

**PURPOSE:** initialize an actionAngleAdiabatic object

**INPUT:**

pot= potential or list of potentials (planarPotentials)

gamma= (default=1.) replace Lz by Lz+gamma Jz in effective potential

**OUTPUT: HISTORY:**

2012-07-26 - Written - Bovy (IAS@MPIA)

### **actionAngleAdiabaticGrid**

```
class galpy.actionAngle.actionAngleAdiabaticGrid(pot=None, zmax=1.0, gamma=1.0,
                                             Rmax=5.0, nR=16, nEz=16, nEr=31,
                                             nLz=31, numcores=1, **kwargs)
```

Action-angle formalism for axisymmetric potentials using the adiabatic approximation, grid-based interpolation

```
__init__(pot=None, zmax=1.0, gamma=1.0, Rmax=5.0, nR=16, nEz=16, nEr=31, nLz=31, num-
        cores=1, **kwargs)
```

**NAME:** \_\_init\_\_

**PURPOSE:** initialize an actionAngleAdiabaticGrid object

**INPUT:**

pot= potential or list of potentials

zmax= zmax for building Ez grid

Rmax = Rmax for building grids

gamma= (default=1.) replace Lz by Lz+gamma Jz in effective potential

nEz=, nEr=, nLz, nR= grid size

numcores= number of cpus to use to parallelize

c= if True, use C to calculate actions

+scipy.integrate.quad keywords

**OUTPUT: HISTORY:**

2012-07-27 - Written - Bovy (IAS@MPIA)

## actionAngleStaeckel

```
class galpy.actionAngle.actionAngleStaeckel(*args, **kwargs)
    Action-angle formalism for axisymmetric potentials using Binney (2012)'s Staeckel approximation
```

```
__init__(*args, **kwargs)
```

**NAME:** \_\_init\_\_

**PURPOSE:** initialize an actionAngleStaeckel object

**INPUT:** pot= potential or list of potentials (3D)

delta= focus

useu0 - use u0 to calculate dV (NOT recommended)

c= if True, always use C for calculations

**OUTPUT: HISTORY:**

2012-11-27 - Written - Bovy (IAS)

## actionAngleStaeckelGrid

```
class galpy.actionAngle.actionAngleStaeckelGrid(pot=None, delta=None, Rmax=5.0,
                                                nE=25, npsi=25, nLz=25, numcores=1,
                                                **kwargs)
```

Action-angle formalism for axisymmetric potentials using Binney (2012)'s Staeckel approximation, grid-based interpolation

```
__init__(pot=None, delta=None, Rmax=5.0, nE=25, npsi=25, nLz=25, numcores=1, **kwargs)
```

**NAME:** \_\_init\_\_

**PURPOSE:** initialize an actionAngleStaeckelGrid object

**INPUT:** pot= potential or list of potentials

delta= focus of prolate confocal coordinate system

Rmax = Rmax for building grids

nE=, npsi=, nLz= grid size

numcores= number of cpus to use to parallelize

+scipy.integrate.quad keywords

**OUTPUT: HISTORY:**

2012-11-29 - Written - Bovy (IAS)

## actionAngleIsochroneApprox

```
class galpy.actionAngle.actionAngleIsochroneApprox(*args, **kwargs)
```

Action-angle formalism using an isochrone potential as an approximate potential and using a Fox & Binney (2014?) like algorithm to calculate the actions using orbit integrations and a torus-machinery-like angle-fit to get the angles and frequencies (Bovy 2014)

```
__init__(*args, **kwargs)
```

**NAME:** \_\_init\_\_

**PURPOSE:** initialize an actionAngleIsochroneApprox object

**INPUT:**

Either:

b= scale parameter of the isochrone parameter

ip= instance of a IsochronePotential

aAI= instance of an actionAngleIsochrone

pot= potential to calculate action-angle variables for

tintJ= (default: 100) time to integrate orbits for to estimate actions

ntintJ= (default: 10000) number of time-integration points actions

integrate\_method= (default: ‘dopr54\_c’) integration method to use

**OUTPUT: HISTORY:**

2013-09-10 - Written - Bovy (IAS)

## 2.5 Utilities

### 2.5.1 galpy.util.bovy\_plot

Various plotting routines:

#### galpy.util.bovy\_plot.bovy\_dens2d

galpy.util.bovy\_plot.**bovy\_dens2d**(X, \*\*kwargs)

NAME:

bovy\_dens2d

**PURPOSE:**

plot a 2d density with optional contours

**INPUT:**

first argument is the density

matplotlib.pyplot.imshow keywords (see [http://matplotlib.sourceforge.net/api/axes\\_api.html#matplotlib.axes.Axes.imshow](http://matplotlib.sourceforge.net/api/axes_api.html#matplotlib.axes.Axes.imshow))

xlabel - (raw string!) x-axis label, LaTeX math mode, no \$s needed

ylabel - (raw string!) y-axis label, LaTeX math mode, no \$s needed

xrange

yrange

noaxes - don’t plot any axes

overplot - if True, overplot

colorbar - if True, add colorbar

shrink= colorbar argument: shrink the colorbar by the factor (optional)

Contours:

justcontours - if True, only draw contours  
contours - if True, draw contours (10 by default)  
levels - contour-levels  
cntrmass - if True, the density is a probability and the levels are probability masses contained within the contour  
cntrcolors - colors for contours (single color or array)  
cntrlabel - label the contours  
cntrlw, cntrls - linewidths and linestyles for contour  
cntrlabelsize, cntrlabelcolors,cntrinline - contour arguments  
cntrSmooth - use ndimage.gaussian\_filter to smooth before contouring  
onedhists - if True, make one-d histograms on the sides  
onedhistcolor - histogram color  
retAxes= return all Axes instances  
retCont= return the contour instance

OUTPUT:

plot to output device, Axes instances depending on input

HISTORY:

2010-03-09 - Written - Bovy (NYU)

## galpy.util.bovy\_plot.bovy\_end\_print

galpy.util.bovy\_plot.**bovy\_end\_print** (filename, \*\*kwargs)

NAME:

bovy\_end\_print

PURPOSE:

saves the current figure(s) to filename

INPUT:

filename - filename for plot (with extension)

OPTIONAL INPUTS:

format - file-format

OUTPUT:

(none)

HISTORY:

2009-12-23 - Written - Bovy (NYU)

**galpy.util.bovy\_plot.bovy\_hist**

```
galpy.util.bovy_plot.bovy_hist(x, xlabel=None, ylabel=None, overplot=False, **kwargs)
```

NAME:

bovy\_hist

PURPOSE:

wrapper around matplotlib's hist function

INPUT:

x - array to histogram

xlabel - (raw string!) x-axis label, LaTeX math mode, no \$s needed

ylabel - (raw string!) y-axis label, LaTeX math mode, no \$s needed

yrange - set the y-axis range

+all pyplot.hist keywords

OUTPUT: (from the matplotlib docs: [http://matplotlib.sourceforge.net/api/pyplot\\_api.html#matplotlib.pyplot.hist](http://matplotlib.sourceforge.net/api/pyplot_api.html#matplotlib.pyplot.hist))

The return value is a tuple (n, bins, patches) or ([n0, n1, ...], bins, [patches0, patches1,...]) if the input contains multiple data

HISTORY:

2009-12-23 - Written - Bovy (NYU)

**galpy.util.bovy\_plot.bovy\_plot**

```
galpy.util.bovy_plot.bovy_plot(*args, **kwargs)
```

NAME:

bovy\_plot

PURPOSE:

wrapper around matplotlib's plot function

INPUT:

see [http://matplotlib.sourceforge.net/api/pyplot\\_api.html#matplotlib.pyplot.plot](http://matplotlib.sourceforge.net/api/pyplot_api.html#matplotlib.pyplot.plot)

xlabel - (raw string!) x-axis label, LaTeX math mode, no \$s needed

ylabel - (raw string!) y-axis label, LaTeX math mode, no \$s needed

xrange

yrange

scatter= if True, use pyplot.scatter and its options etc.

colorbar= if True, and scatter==True, add colorbar

crange - range for colorbar of scatter==True

clabel= label for colorbar

overplot=True does not start a new figure

onedhists - if True, make one-d histograms on the sides

onedhistcolor, onedhistfc, onedhistec  
onedhistxnormed, onedhistynormed - normed keyword for one-d histograms  
onedhistxweights, onedhistyweights - weights keyword for one-d histograms  
bins= number of bins for onedhists  
semilogx=, semilogy=, loglog= if True, plot logs

OUTPUT:

plot to output device, returns what pyplot.plot returns, or 3 Axes instances if onedhists=True

HISTORY:

2009-12-28 - Written - Bovy (NYU)

## galpy.util.bovy\_plot.bovy\_print

```
galpy.util.bovy_plot.bovy_print(fig_width=5, fig_height=5, axes_labelsize=16,
                                text_fontsize=11, legend_fontsize=12, xtick_labelsize=10,
                                ytick_labelsize=10, xtick_minor_size=2, ytick_minor_size=2,
                                xtick_major_size=4, ytick_major_size=4)
```

NAME:

bovy\_print

PURPOSE:

setup a figure for plotting

INPUT:

fig\_width - width in inches  
fig\_height - height in inches  
axes\_labelsize - size of the axis-labels  
text\_fontsize - font-size of the text (if any)  
legend\_fontsize - font-size of the legend (if any)  
xtick\_labelsize - size of the x-axis labels  
ytick\_labelsize - size of the y-axis labels  
xtick\_minor\_size - size of the minor x-ticks  
ytick\_minor\_size - size of the minor y-ticks

OUTPUT:

(none)

HISTORY:

2009-12-23 - Written - Bovy (NYU)

## galpy.util.bovy\_plot.bovy\_text

```
galpy.util.bovy_plot.bovy_text(*args, **kwargs)
```

NAME:

bovy\_text

**PURPOSE:**

thin wrapper around matplotlib's text and annotate

use keywords:

‘bottom\_left=True’

‘bottom\_right=True’

‘top\_left=True’

‘top\_right=True’

‘title=True’

to place the text in one of the corners or use it as the title

**INPUT:**

see **matplotlib's text** ([http://matplotlib.sourceforge.net/api/pyplot\\_api.html#matplotlib.pyplot.text](http://matplotlib.sourceforge.net/api/pyplot_api.html#matplotlib.pyplot.text))

**OUTPUT:**

prints text on the current figure

**HISTORY:**

2010-01-26 - Written - Bovy (NYU)

**galpy.util.bovy\_plot.scatterplot**

galpy.util.bovy\_plot.**scatterplot** (*x*, *y*, \**args*, \*\**kwargs*)

**NAME:**

scatterplot

**PURPOSE:**

make a ‘smart’ scatterplot that is a density plot in high-density regions and a regular scatterplot for outliers

**INPUT:**

*x*, *y*

*xlabel* - (raw string!) x-axis label, LaTeX math mode, no \$s needed

*ylabel* - (raw string!) y-axis label, LaTeX math mode, no \$s needed

*xrange*

*yrange*

*bins* - number of bins to use in each dimension

*weights* - data-weights

*aspect* - aspect ratio

*contours* - if False, don't plot contours

*cntrcolors* - color of contours (can be array as for bovy\_dens2d)

*cntrlw*, *cntrls* - linewidths and linestyles for contour

*cntrSmooth* - use ndimage.gaussian\_filter to smooth before contouring

*onedhists* - if True, make one-d histograms on the sides

onedhistx - if True, make one-d histograms on the side of the x distribution  
onedhisty - if True, make one-d histograms on the side of the y distribution  
onedhistcolor, onedhistfc, onedhistec  
onedhistxnormed, onedhistynormed - normed keyword for one-d histograms  
onedhistxweights, onedhistyweights - weights keyword for one-d histograms  
cmap= cmap for density plot  
hist= and edges= - you can supply the histogram of the data yourself, this can be useful if you want to censor the data, both need to be set and calculated using `scipy.histogramdd` with the given range  
retAxes= return all Axes instances

OUTPUT:

plot to output device, Axes instance(s) or not, depending on input

HISTORY:

2010-04-15 - Written - Bovy (NYU)

## 2.5.2 galpy.util.bovy\_conversion

Conversion between galpy's *natural* units and *physical* units

### galpy.util.bovy\_conversion.dens\_in\_msolpc3

`galpy.util.bovy_conversion.dens_in_msolpc3(vo, ro)`

NAME:

`dens_in_msolpc3`

PURPOSE:

convert density to Msolar / pc<sup>3</sup>

INPUT:

vo - velocity unit in km/s

ro - length unit in kpc

OUTPUT:

conversion from units where vo=1. at ro=1. to Msolar/pc<sup>3</sup>

HISTORY:

2013-09-01 - Written - Bovy (IAS)

### galpy.util.bovy\_conversion.force\_in\_2piGmsolpc2

`galpy.util.bovy_conversion.force_in_2piGmsolpc2(vo, ro)`

NAME:

`force_in_2piGmsolpc2`

PURPOSE:

convert a force or acceleration to 2piG x Msolar / pc<sup>2</sup>

**INPUT:**

vo - velocity unit in km/s

ro - length unit in kpc

**OUTPUT:**

conversion from units where vo=1. at ro=1.

**HISTORY:**

2013-09-01 - Written - Bovy (IAS)

**galpy.util.bovy\_conversion.force\_in\_pcMyr2**

galpy.util.bovy\_conversion.**force\_in\_pcMyr2**(*vo, ro*)

**NAME:**

force\_in\_pcMyr2

**PURPOSE:**

convert a force or acceleration to pc/Myr^2

**INPUT:**

vo - velocity unit in km/s

ro - length unit in kpc

**OUTPUT:**

conversion from units where vo=1. at ro=1.

**HISTORY:**

2013-09-01 - Written - Bovy (IAS)

**galpy.util.bovy\_conversion.force\_in\_kmsMyr**

galpy.util.bovy\_conversion.**force\_in\_kmsMyr**(*vo, ro*)

**NAME:**

force\_in\_kmsMyr

**PURPOSE:**

convert a force or acceleration to km/s/Myr

**INPUT:**

vo - velocity unit in km/s

ro - length unit in kpc

**OUTPUT:**

conversion from units where vo=1. at ro=1.

**HISTORY:**

2013-09-01 - Written - Bovy (IAS)

### galpy.util.bovy\_conversion.freq\_in\_Gyr

galpy.util.bovy\_conversion.**freq\_in\_Gyr**(*vo, ro*)

NAME:

freq\_in\_Gyr

PURPOSE:

convert a frequency to 1/Gyr

INPUT:

*vo* - velocity unit in km/s

*ro* - length unit in kpc

OUTPUT:

conversion from units where *vo*=1. at *ro*=1.

HISTORY:

2013-09-01 - Written - Bovy (IAS)

### galpy.util.bovy\_conversion.freq\_in\_kmskpc

galpy.util.bovy\_conversion.**freq\_in\_kmskpc**(*vo, ro*)

NAME:

freq\_in\_kmskpc

PURPOSE:

convert a frequency to km/s/kpc

INPUT:

*vo* - velocity unit in km/s

*ro* - length unit in kpc

OUTPUT:

conversion from units where *vo*=1. at *ro*=1.

HISTORY:

2013-09-01 - Written - Bovy (IAS)

### galpy.util.bovy\_conversion.surfdens\_in\_msolpc2

galpy.util.bovy\_conversion.**surfdens\_in\_msolpc2**(*vo, ro*)

NAME:

surfdens\_in\_msolpc2

PURPOSE:

convert a surface density to Msolar / pc<sup>2</sup>

INPUT:

vo - velocity unit in km/s

ro - length unit in kpc

OUTPUT:

conversion from units where vo=1. at ro=1.

HISTORY:

2013-09-01 - Written - Bovy (IAS)

### **galpy.util.bovy\_conversion.mass\_in\_msol**

galpy.util.bovy\_conversion.**mass\_in\_msol**(*vo, ro*)

NAME:

mass\_in\_msol

PURPOSE:

convert a mass to Msolar

INPUT:

vo - velocity unit in km/s

ro - length unit in kpc

OUTPUT:

conversion from units where vo=1. at ro=1.

HISTORY:

2013-09-01 - Written - Bovy (IAS)

### **galpy.util.bovy\_conversion.mass\_in\_1010msol**

galpy.util.bovy\_conversion.**mass\_in\_1010msol**(*vo, ro*)

NAME:

mass\_in\_1010msol

PURPOSE:

convert a mass to 10^10 x Msolar

INPUT:

vo - velocity unit in km/s

ro - length unit in kpc

OUTPUT:

conversion from units where vo=1. at ro=1.

HISTORY:

2013-09-01 - Written - Bovy (IAS)

### galpy.util.bovy\_conversion.time\_in\_Gyr

galpy.util.bovy\_conversion.**time\_in\_Gyr**(vo, ro)

NAME:

time\_in\_Gyr

PURPOSE:

convert a time to Gyr

INPUT:

vo - velocity unit in km/s

ro - length unit in kpc

OUTPUT:

conversion from units where vo=1. at ro=1.

HISTORY:

2013-09-01 - Written - Bovy (IAS)

### 2.5.3 galpy.util.bovy\_coords

Various coordinate transformation routines with fairly self-explanatory names:

#### galpy.util.bovy\_coords.cov\_dvrpmllbb\_to\_vxyz

galpy.util.bovy\_coords.**cov\_dvrpmllbb\_to\_vxyz**(d, e\_d, e\_vr, pmll, pmbb, cov\_pmllbb, l, b,  
plx=False, degree=False)

NAME:

cov\_dvrpmllbb\_to\_vxyz

PURPOSE:

propagate distance, radial velocity, and proper motion uncertainties to Galactic coordinates

INPUT:

d - distance [kpc, as/mas for plx]

e\_d - distance uncertainty [kpc, [as/mas] for plx]

e\_vr - low velocity uncertainty [km/s]

pmll - proper motion in l ( $*\cos(b)$ ) [ [as/mas]/yr ]

pmbb - proper motion in b [ [as/mas]/yr ]

cov\_pmllbb - uncertainty covariance for proper motion

l - Galactic longitude

b - Galactic latitude

KEYWORDS:

plx - if True, d is a parallax, and e\_d is a parallax uncertainty

degree - if True, l and b are given in degree

**OUTPUT:**

`cov(vx,vy,vz) [3,3] or [:,3,3]`

**HISTORY:**

2010-04-12 - Written - Bovy (NYU)

**`galpy.util.bovy_coords.cov_pmrapmdec_to_pmllpmbb`**

`galpy.util.bovy_coords.cov_pmrapmdec_to_pmllpmbb (cov_pmradec, ra, dec, degree=False, epoch=2000.0)`

**NAME:**

`cov_pmrapmdec_to_pmllpmbb`

**PURPOSE:**

propagate the proper motions errors through the rotation from (ra,dec) to (l,b)

**INPUT:**

`covar_pmradec` - uncertainty covariance matrix of the proper motion in ra (multiplied with cos(dec)) and dec [2,2] or [:,2,2]

`ra` - right ascension

`dec` - declination

`degree` - if True, ra and dec are given in degrees (default=False)

`epoch` - epoch of ra,dec (right now only 2000.0 and 1950.0 are supported)

**OUTPUT:**

`covar_pmllbb [2,2] or [:,2,2]`

**HISTORY:**

2010-04-12 - Written - Bovy (NYU)

**`galpy.util.bovy_coords.cyl_to_rect`**

`galpy.util.bovy_coords.cyl_to_rect (R, phi, Z)`

**NAME:**

`cyl_to_rect`

**PURPOSE:**

convert from cylindrical to rectangular coordinates

**INPUT:**

`R, phi, Z` - cylindrical coordinates

**OUTPUT:**

`[:,3] X,Y,Z`

**HISTORY:**

2011-02-23 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.cyl\_to\_rect\_vec**

galpy.util.bovy\_coords.**cyl\_to\_rect\_vec**(*vr, vt, vz, phi*)

NAME:

cyl\_to\_rect\_vec

PURPOSE:

transform vectors from cylindrical to rectangular coordinate vectors

INPUT:

*vr* - radial velocity

*vt* - tangential velocity

*vz* - vertical velocity

*phi* - azimuth

OUTPUT:

*vx,vy,vz*

HISTORY:

2011-02-24 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.dl\_to\_rphi\_2d**

galpy.util.bovy\_coords.**dl\_to\_rphi\_2d**(*d, l, degree=False, ro=1.0, phio=0.0*)

NAME:

dl\_to\_rphi\_2d

PURPOSE:

convert Galactic longitude and distance to Galactocentric radius and azimuth

INPUT:

*d* - distance

*l* - Galactic longitude [rad/deg if degree]

KEYWORDS:

*degree*= (False): *l* is in degrees rather than rad

*ro*= (1) Galactocentric radius of the observer

*phio*= (0) Galactocentric azimuth of the observer [rad/deg if degree]

OUTPUT:

(*R,phi*); *phi* in degree if degree

HISTORY:

2012-01-04 - Written - Bovy (IAS)

**galpy.util.bovy\_coords.galcencyl\_to\_XYZ**

galpy.util.bovy\_coords.**galcencyl\_to\_XYZ** ( $R, phi, Z, X_{\text{sun}}=1.0, Y_{\text{sun}}=0.0, Z_{\text{sun}}=0.0$ )  
NAME:

galcencyl\_to\_XYZ

PURPOSE:

transform cylindrical Galactocentric coordinates to XYZ coordinates (wrt Sun)

INPUT:

$R, phi, Z$  - Galactocentric cylindrical coordinates

OUTPUT:

[;3]= X,Y,Z

HISTORY:

2011-02-23 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.galcencyl\_to\_vxvyvz**

galpy.util.bovy\_coords.**galcencyl\_to\_vxvyvz** ( $vR, vT, vZ, phi, v_{\text{sun}}=[0.0, 1.0, 0.0]$ )  
NAME:

galcencyl\_to\_vxvyvz

PURPOSE:

transform cylindrical Galactocentric coordinates to XYZ (wrt Sun) coordinates for velocities

INPUT:

$vR$  - Galactocentric radial velocity

$vT$  - Galactocentric tangential velocity

$vZ$  - Galactocentric vertical velocity

$phi$  - Galactocentric azimuth

$v_{\text{sun}}$  - velocity of the sun ndarray[3]

OUTPUT:

$vx, vy, vz$

HISTORY:

2011-02-24 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.galcenrect\_to\_vxvyvz**

galpy.util.bovy\_coords.**galcenrect\_to\_vxvyvz** ( $vXg, vYg, vZg, v_{\text{sun}}=[0.0, 1.0, 0.0]$ )  
NAME:

galcenrect\_to\_vxvyvz

PURPOSE:

transform rectangular Galactocentric coordinates to XYZ coordinates (wrt Sun) for velocities

INPUT:

vXg - Galactocentric x-velocity  
vYg - Galactocentric y-velocity  
vZg - Galactocentric z-velocity  
vsun - velocity of the sun ndarray[3]

OUTPUT:

[:,3]= vx, vy, vz

HISTORY:

2011-02-24 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.lb\_to\_radec**

galpy.util.bovy\_coords.**lb\_to\_radec** (*l, b, degree=False, epoch=2000.0*)

NAME:

lb\_to\_radec

PURPOSE:

transform from Galactic coordinates to equatorial coordinates

INPUT:

*l* - Galactic longitude  
*b* - Galactic latitude  
*degree* - (Bool) if True, *l* and *b* are given in degree and ra and dec will be as well  
*epoch* - epoch of target ra,dec (right now only 2000.0 and 1950.0 are supported)

OUTPUT:

ra,dec

For vector inputs [:,2]

HISTORY:

2010-04-07 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.lb\_to\_radec**

galpy.util.bovy\_coords.**lbd\_to\_XYZ** (*l, b, d, degree=False*)

NAME:

lbd\_to\_XYZ

PURPOSE:

transform from spherical Galactic coordinates to rectangular Galactic coordinates (works with vector inputs)

INPUT:

l - Galactic longitude (rad)  
b - Galactic latitude (rad)  
d - distance (arbitrary units)  
degree - (bool) if True, l and b are in degrees

OUTPUT:

[X,Y,Z] in whatever units d was in  
For vector inputs [:,3]

HISTORY:

2009-10-24- Written - Bovy (NYU)

### **galpy.util.bovy\_coords.pmllpmbb\_to\_pmrapmdec**

```
galpy.util.bovy_coords.pmllpmbb_to_pmrapmdec(pmll, pmbb, l, b, degree=False,  
epoch=2000.0)
```

NAME:

pmllpmbb\_to\_pmrapmdec

PURPOSE:

rotate proper motions in (l,b) into proper motions in (ra,dec)

INPUT:

pmll - proper motion in l (multiplied with cos(b)) [mas/yr]  
pmbb - proper motion in b [mas/yr]  
l - Galactic longitude  
b - Galactic latitude  
degree - if True, l and b are given in degrees (default=False)  
epoch - epoch of ra,dec (right now only 2000.0 and 1950.0 are supported)

OUTPUT:

(pmra,pmdec), for vector inputs [:,2]

HISTORY:

2010-04-07 - Written - Bovy (NYU)

### **galpy.util.bovy\_coords.cov\_pmrapmdec\_to\_pmllpmbb**

```
galpy.util.bovy_coords.cov_pmrapmdec_to_pmllpmbb(cov_pmradec, ra, dec, degree=False,  
epoch=2000.0)
```

NAME:

cov\_pmrapmdec\_to\_pmllpmbb

PURPOSE:

propagate the proper motions errors through the rotation from (ra,dec) to (l,b)

INPUT:

covar\_pmradec - uncertainty covariance matrix of the proper motion in ra (multiplied with cos(dec)) and dec [2,2] or [:,2,2]

ra - right ascension

dec - declination

degree - if True, ra and dec are given in degrees (default=False)

epoch - epoch of ra,dec (right now only 2000.0 and 1950.0 are supported)

OUTPUT:

covar\_pmllbb [2,2] or [:,2,2]

HISTORY:

2010-04-12 - Written - Bovy (NYU)

## galpy.util.bovy\_coords.radec\_to\_lb

galpy.util.bovy\_coords.**radec\_to\_lb** (*ra, dec, degree=False, epoch=2000.0*)

NAME:

radec\_to\_lb

PURPOSE:

transform from equatorial coordinates to Galactic coordinates

INPUT:

ra - right ascension

dec - declination

degree - (Bool) if True, ra and dec are given in degree and l and b will be as well

epoch - epoch of ra,dec (right now only 2000.0 and 1950.0 are supported)

OUTPUT:

l,b

For vector inputs [:,2]

HISTORY:

2009-11-12 - Written - Bovy (NYU)

## galpy.util.bovy\_coords.rectgal\_to\_spherical

galpy.util.bovy\_coords.**rectgal\_to\_spherical** (*X, Y, Z, vx, vy, vz, degree=False*)

NAME:

rectgal\_to\_spherical

PURPOSE:

transform phase-space coordinates in rectangular Galactic coordinates to spherical Galactic coordinates (can take vector inputs)

INPUT:

X - component towards the Galactic Center (kpc)  
Y - component in the direction of Galactic rotation (kpc)  
Z - component towards the North Galactic Pole (kpc)  
vx - velocity towards the Galactic Center (km/s)  
vy - velocity in the direction of Galactic rotation (km/s)  
vz - velocity towards the North Galactic Pole (km/s)  
degree - (Bool) if True, return l and b in degrees

OUTPUT:

(l,b,d,vr,pmll,pmbb) in (rad,rad,kpc,km/s,mas/yr,mas/yr)

HISTORY:

2009-10-25 - Written - Bovy (NYU)

### `galpy.util.bovy_coords.rect_to_cyl`

`galpy.util.bovy_coords.rect_to_cyl(X, Y, Z)`

NAME:

`rect_to_cyl`

PURPOSE:

convert from rectangular to cylindrical coordinates

INPUT:

X, Y, Z - rectangular coordinates

OUTPUT:

[:,3] R,phi,z

HISTORY:

2010-09-24 - Written - Bovy (NYU)

### `galpy.util.bovy_coords.rect_to_cyl_vec`

`galpy.util.bovy_coords.rect_to_cyl_vec(vx, vy, vz, X, Y, Z, cyl=False)`

NAME:

`rect_to_cyl_vec`

PURPOSE:

transform vectors from rectangular to cylindrical coordinates vectors

INPUT:

vx -

vy -

vz -

X - X

Y - Y

Z - Z

cyl - if True, X,Y,Z are already cylindrical

OUTPUT:

vR,vT,vz

HISTORY:

2010-09-24 - Written - Bovy (NYU)

## galpy.util.bovy\_coords.rphi\_to\_dl\_2d

galpy.util.bovy\_coords.**rphi\_to\_dl\_2d**(*R, phi, degree=False, ro=1.0, phio=0.0*)

NAME:

rphi\_to\_dl\_2d

PURPOSE:

convert Galactocentric radius and azimuth to distance and Galactic longitude

INPUT:

*R* - Galactocentric radius

*phi* - Galactocentric azimuth [rad/deg if degree]

KEYWORDS:

*degree*= (False): *phi* is in degrees rather than rad

*ro*= (1) Galactocentric radius of the observer

*phio*= (0) Galactocentric azimuth of the observer [rad/deg if degree]

OUTPUT:

(*d,l*); *phi* in degree if degree

HISTORY:

2012-01-04 - Written - Bovy (IAS)

## galpy.util.bovy\_coords.Rz\_to\_coshucosv

galpy.util.bovy\_coords.**Rz\_to\_coshucosv**(*R, z, delta=1.0*)

NAME:

Rz\_to\_coshucosv

PURPOSE:

calculate prolate confocal cosh(*u*) and cos(*v*) coordinates from *R,z*, and *delta*

INPUT:

*R* - radius

*z* - height

*delta*= focus

**OUTPUT:**

(cosh(u),cos(v))

**HISTORY:**

2012-11-27 - Written - Bovy (IAS)

**galpy.util.bovy\_coords.Rz\_to\_uv**galpy.util.bovy\_coords.**Rz\_to\_uv**(*R, z, delta=1.0*)**NAME:**

Rz\_to\_uv

**PURPOSE:**

calculate prolate confocal u and v coordinates from R,z, and delta

**INPUT:**

R - radius

z - height

delta= focus

**OUTPUT:**

(u,v)

**HISTORY:**

2012-11-27 - Written - Bovy (IAS)

**galpy.util.bovy\_coords.sphergal\_to\_rectgal**galpy.util.bovy\_coords.**sphergal\_to\_rectgal**(*l, b, d, vr, pmll, pmbb, degree=False*)**NAME:**

sphergal\_to\_rectgal

**PURPOSE:**

transform phase-space coordinates in spherical Galactic coordinates to rectangular Galactic coordinates (can take vector inputs)

**INPUT:**

l - Galactic longitude (rad)

b - Galactic latitude (rad)

d - distance (kpc)

vr - line-of-sight velocity (km/s)

pmll - proper motion in the Galactic longitude direction ( $\mu_l \cos(b)$ ) (mas/yr)

pmbb - proper motion in the Galactic latitude (mas/yr)

degree - (bool) if True, l and b are in degrees

**OUTPUT:**

(X,Y,Z,vx,vy,vz) in (kpc,kpc,kpc,km/s,km/s,km/s)

HISTORY:

2009-10-25 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.uv\_to\_Rz**

`galpy.util.bovy_coords.uv_to_Rz(u, v, delta=1.0)`

NAME:

`uv_to_Rz`

PURPOSE:

calculate R and z from prolate confocal u and v coordinates

INPUT:

`u` - confocal u

`v` - confocal v

`delta=` focus

OUTPUT:

`(R,z)`

HISTORY:

2012-11-27 - Written - Bovy (IAS)

**galpy.util.bovy\_coords.vrpmllpmbb\_to\_vxvyvz**

`galpy.util.bovy_coords.vrpmllpmbb_to_vxvyvz(vr, pmll, pmbb, l, b, d, XYZ=False, degree=False)`

NAME:

`vrpmllpmbb_to_vxvyvz`

PURPOSE:

Transform velocities in the spherical Galactic coordinate frame to the rectangular Galactic coordinate frame (can take vector inputs)

INPUT:

`vr` - line-of-sight velocity (km/s)

`pmll` - proper motion in the Galactic longitude ( $\mu_l \cos(b)$ )(mas/yr)

`pmbb` - proper motion in the Galactic latitude (mas/yr)

`l` - Galactic longitude

`b` - Galactic latitude

`d` - distance (kpc)

`XYZ` - (bool) If True, then `l,b,d` is actually X,Y,Z (rectangular Galactic coordinates)

`degree` - (bool) if True, `l` and `b` are in degrees

OUTPUT:

`(vx,vy,vz)` in (km/s,km/s,km/s)

**HISTORY:**

2009-10-24 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.vxvyvz\_to\_galcencyl**

`galpy.util.bovy_coords.vxvyvz_to_galcencyl(vx, vy, vz, X, Y, Z, vsun=[0.0, 1.0, 0.0], galcen=False)`

**NAME:**

`vxvyvz_to_galcencyl`

**PURPOSE:**

transform XYZ coordinates (wrt Sun) to cylindrical Galactocentric coordinates for velocities

**INPUT:**

vx - U

vy - V

vz - W

X - X

Y - Y

Z - Z

vsun - velocity of the sun ndarray[3]

galcen - if True, then X,Y,Z are in cylindrical Galactocentric coordinates

**OUTPUT:**

vRg, vTg, vZg

**HISTORY:**

2010-09-24 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.vxvyvz\_to\_galcenrect**

`galpy.util.bovy_coords.vxvyvz_to_galcenrect(vx, vy, vz, vsun=[0.0, 1.0, 0.0])`

**NAME:**

`vxvyvz_to_galcenrect`

**PURPOSE:**

transform XYZ coordinates (wrt Sun) to rectangular Galactocentric coordinates for velocities

**INPUT:**

vx - U

vy - V

vz - W

vsun - velocity of the sun ndarray[3]

**OUTPUT:**

[:,3]= vXg, vYg, vZg

HISTORY:

2010-09-24 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.vxvyvz\_to\_vrpmllpmbb**

`galpy.util.bovy_coords.vxvyvz_to_vrpmllpmbb` (*vx*, *vy*, *vz*, *l*, *b*, *d*, *XYZ=False*, *degree=False*)  
NAME:

`vxvyvz_to_vrpmllpmbb`

PURPOSE:

Transform velocities in the rectangular Galactic coordinate frame to the spherical Galactic coordinate frame (can take vector inputs)

INPUT:

*vx* - velocity towards the Galactic Center (km/s)  
*vy* - velocity in the direction of Galactic rotation (km/s)  
*vz* - velocity towards the North Galactic Pole (km/s)  
*l* - Galactic longitude  
*b* - Galactic latitude  
*d* - distance (kpc)  
*XYZ* - (bool) If True, then *l,b,d* is actually X,Y,Z (rectangular Galactic coordinates)  
*degree* - (bool) if True, *l* and *b* are in degrees

OUTPUT:

(*vr*,*pmll*,*pmbb*) in (km/s,mas/yr,mas/yr); *pmll* =  $\mu_l \cos(b)$

HISTORY:

2009-10-24 - Written - Bovy (NYU)

**galpy.util.bovy\_coords.XYZ\_to\_galcencyl**

`galpy.util.bovy_coords.XYZ_to_galcencyl` (*X*, *Y*, *Z*, *Xsun=1.0*, *Ysun=0.0*, *Zsun=0.0*)  
NAME:

`XYZ_to_galcencyl`

PURPOSE:

transform XYZ coordinates (wrt Sun) to cylindrical Galactocentric coordinates

INPUT:

*X* - X  
*Y* - Y  
*Z* - Z

OUTPUT:

[*:3*] = R,phi,z

HISTORY:

2010-09-24 - Written - Bovy (NYU)

### **galpy.util.bovy\_coords.XYZ\_to\_galcenrect**

`galpy.util.bovy_coords.XYZ_to_galcenrect(X, Y, Z, Xsun=1.0, Ysun=0.0, Zsun=0.0)`

NAME:

`XYZ_to_galcenrect`

PURPOSE:

transform XYZ coordinates (wrt Sun) to rectangular Galactocentric coordinates

INPUT:

X - X

Y - Y

Z - Z

OUTPUT:

(Xg, Yg, Zg)

HISTORY:

2010-09-24 - Written - Bovy (NYU)

### **galpy.util.bovy\_coords.XYZ\_to\_lbd**

`galpy.util.bovy_coords.XYZ_to_lbd(X, Y, Z, degree=False)`

NAME:

`XYZ_to_lbd`

PURPOSE:

transform from rectangular Galactic coordinates to spherical Galactic coordinates (works with vector inputs)

INPUT:

X - component towards the Galactic Center (in kpc; though this obviously does not matter)

Y - component in the direction of Galactic rotation (in kpc)

Z - component towards the North Galactic Pole (kpc)

degree - (Bool) if True, return l and b in degrees

OUTPUT:

[l,b,d] in (rad,rad,kpc)

For vector inputs [:,3]

HISTORY:

2009-10-24 - Written - Bovy (NYU)

## 2.5.4 galpy.util.bovy\_ars.bovy\_ars

```
galpy.util.bovy_ars.bovy_ars(domain, isDomainFinite, abcissae, hx, hpx, nsamples=1, hx-  
params=(), maxn=100)
```

bovy\_ars: Implementation of the Adaptive-Rejection Sampling algorithm by Gilks & Wild (1992): Adaptive Rejection Sampling for Gibbs Sampling, Applied Statistics, 41, 337 Based on Wild & Gilks (1993), Algorithm AS 287: Adaptive Rejection Sampling from Log-concave Density Functions, Applied Statistics, 42, 701

Input:

- domain - [...] upper and lower limit to the domain
- isDomainFinite - [...] is there a lower/upper limit to the domain?
- abcissae - initial list of abcissae (must lie on either side of the peak in hx if the domain is unbounded)
- hx - function that evaluates  $h(x) = \ln g(x)$
- hpx - function that evaluates  $hp(x) = d h(x) / d x$
- nsamples - (optional) number of desired samples (default=1)
- hxparams - (optional) a tuple of parameters for  $h(x)$  and  $h'(x)$
- maxn - (optional) maximum number of updates to the hull (default=100)

Output:

- list with nsamples of samples from  $\exp(h(x))$

External dependencies:

- math
- scipy
- scipy.stats

**History:** 2009-05-21 - Written - Bovy (NYU)

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**Tutorials**

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## 3.1 Dynamical modeling of tidal streams

galpy contains tools to model the dynamics of tidal streams, making extensive use of action-angle variables. As an example, we can model the dynamics of the following tidal stream (that of Bovy 2014; ). This movie shows the disruption of a cluster on a GD-1-like orbit around the Milky Way:

The blue line is the orbit of the progenitor cluster and the black points are cluster members. The disruption is shown in an approximate orbital plane and the movie is comoving with the progenitor cluster.

Streams can be represented by simple dynamical models in action-angle coordinates. In action-angle coordinates, stream members are stripped from the progenitor cluster onto orbits specified by a set of actions ( $J_R, J_\phi, J_Z$ ), which remain constant after the stars have been stripped. This is shown in the following movie, which shows the generation of the stream in action space

The color-coding gives the angular momentum  $J_\phi$  and the black dot shows the progenitor orbit. These actions were calculated using `galpy.actionAngle.actionAngleIsochroneApprox`. The points move slightly because of small errors in the action calculation (these are correlated, so the cloud of points moves coherently because of calculation errors). The same movie that also shows the actions of stars in the cluster can be found [here](#). This shows that the actions of stars in the cluster are not conserved (because the self-gravity of the cluster is important), but that the actions of stream members freeze once they are stripped. The angle difference between stars in a stream and the progenitor increases linearly with time, which is shown in the following movie:

where the radial and vertical angle difference with respect to the progenitor (co-moving at  $(\theta_R, \theta_\phi, \theta_Z) = (\pi, \pi, \pi)$ ) is shown for each snapshot (the color-coding gives  $\theta_\phi$ ).

One last movie provides further insight in how a stream evolves over time. The following movie shows the evolution of the stream in the two dimensional plane of frequency and angle along the stream (that is, both are projections of the three dimensional frequencies or angles onto the angle direction along the stream). The points are color-coded by the time at which they were removed from the progenitor cluster.

It is clear that disruption happens in bursts (at pericenter passages) and that the initial frequency distribution at the time of removal does not change (much) with time. However, stars removed at larger frequency difference move away from the cluster faster, such that the end of the stream is primarily made up of stars with large frequency differences with respect to the progenitor. This leads to a gradient in the typical orbit in the stream, and the stream is on average *not* on a single orbit.

### 3.1.1 Modeling streams in galpy

In galpy we can model streams using the tools in `galpy.df.streamdf`. We setup a `streamdf` instance by specifying the host gravitational potential `pot=`, an `actionAngle` method (typically `galpy.actionAngle.actionAngleIsochroneApprox`), a `galpy.orbit.Orbit` instance with

the position of the progenitor, a parameter related to the velocity dispersion of the progenitor, and the time since disruption began. We first import all of the necessary modules

```
>>> from galpy.df import streamdf
>>> from galpy.orbit import Orbit
>>> from galpy.potential import LogarithmicHaloPotential
>>> from galpy.actionAngle import actionAngleIsochroneApprox
>>> from galpy.util import bovy_conversion #for unit conversions
```

setup the potential and actionAngle instances

```
>>> lp= LogarithmicHaloPotential(normalize=1.,q=0.9)
>>> aAI= actionAngleIsochroneApprox(pot=lp,b=0.8)
```

define a progenitor Orbit instance

```
>>> obs= Orbit([1.56148083,0.35081535,-1.15481504,0.88719443,-0.47713334,0.12019596])
```

and instantiate the streamdf model

```
>>> sigv= 0.365 #km/s
>>> sdf= streamdf(sigv/220.,progenitor=obs,pot=lp,aA=aAI,leading=True,nTrackChunks=11,tdisrupt=4.5/bc)
```

for a leading stream. This runs in about half a minute on a 2011 Macbook Air.

We can calculate some simple properties of the stream, such as the ratio of the largest and second-to-largest eigenvalue of the Hessian  $\partial\Omega/\partial\mathbf{J}$

```
>>> sdf.freqEigvalRatio(isotropic=True)
34.450028399901434
```

or the model's ratio of the largest and second-to-largest eigenvalue of the model frequency variance matrix

```
>>> sdf.freqEigvalRatio()
29.625538344985291
```

The fact that this ratio is so large means that an approximately one dimensional stream will form.

Similarly, we can calculate the angle between the frequency vector of the progenitor and of the model mean frequency vector

```
>>> sdf.misalignment()
-0.49526013844831596
```

which returns this angle in degrees. We can also calculate the angle between the frequency vector of the progenitor and the principal eigenvector of  $\partial\Omega/\partial\mathbf{J}$

```
>>> sdf.misalignment(isotropic=True)
1.2825116841963993
```

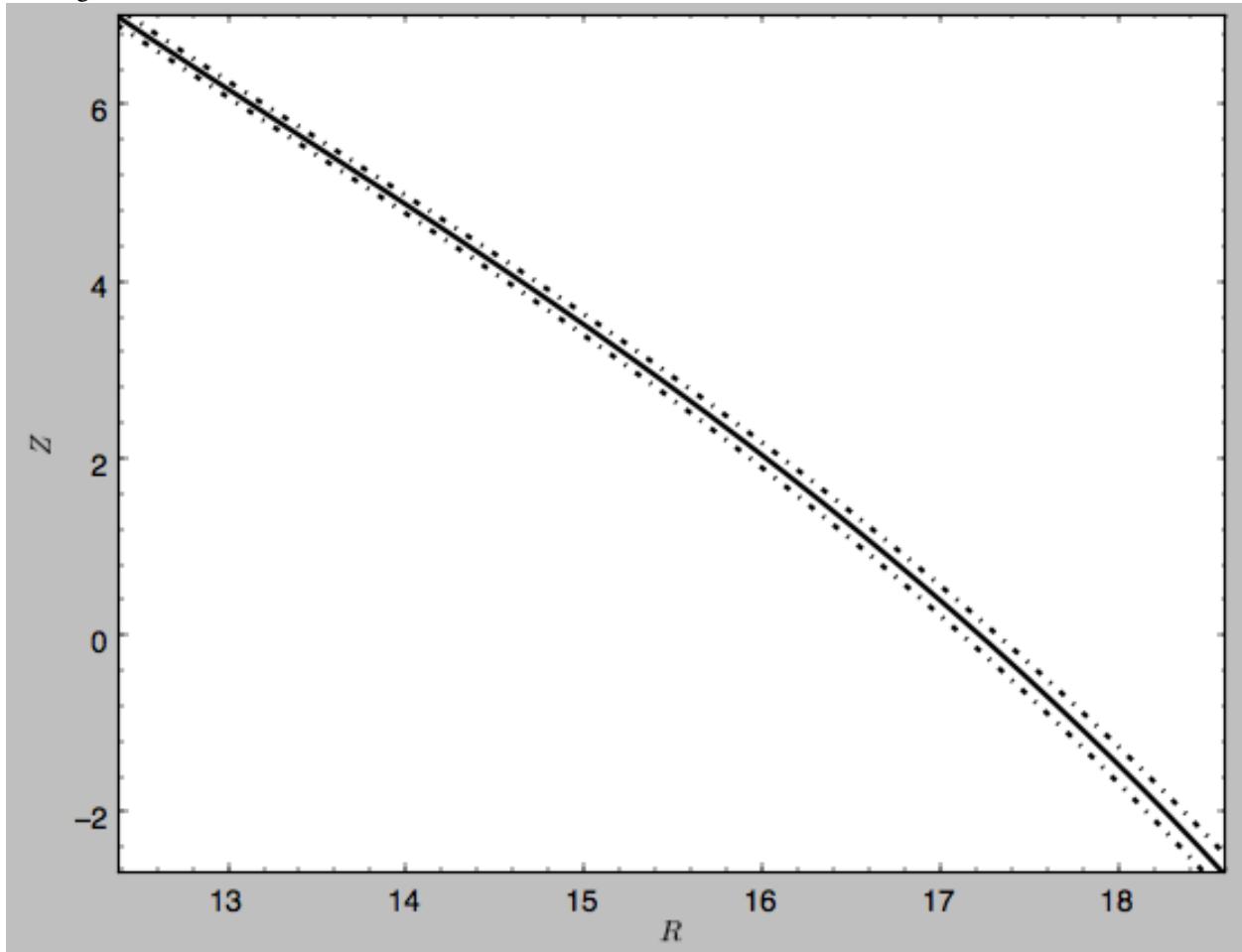
(the reason these are obtained by specifying `isotropic=True` is that these would be the ratio of the eigenvalues or the angle if we assumed that the disrupted materials action distribution were isotropic).

### 3.1.2 Calculating the average stream location (track)

We can display the stream track in various coordinate systems as follows

```
>>> sdf.plotTrack(d1='r',d2='z',interp=True,color='k',spread=2,overplot=False,lw=2.,scaleToPhysical=True)
```

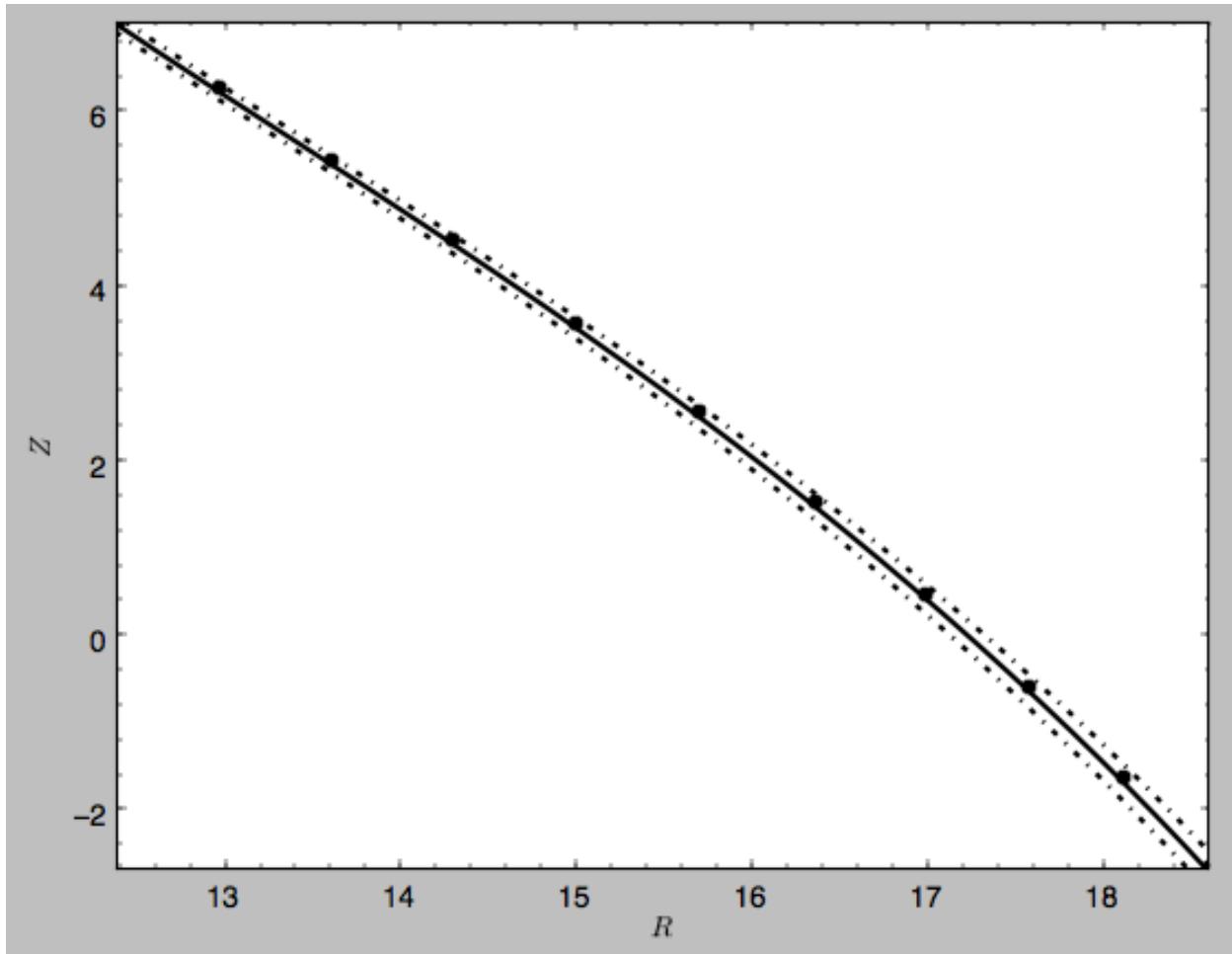
which gives



which shows the track in Galactocentric  $R$  and  $Z$  coordinates as well as an estimate of the spread around the track as the dash-dotted line. We can overplot the points along the track along which the  $(x, v) \rightarrow (\Omega, \theta)$  transformation and the track position is explicitly calculated, by turning off the interpolation

```
>>> sdf.plotTrack(d1='r', d2='z', interp=False, color='k', spread=0, overplot=True, ls='none', marker='o', s=1)
```

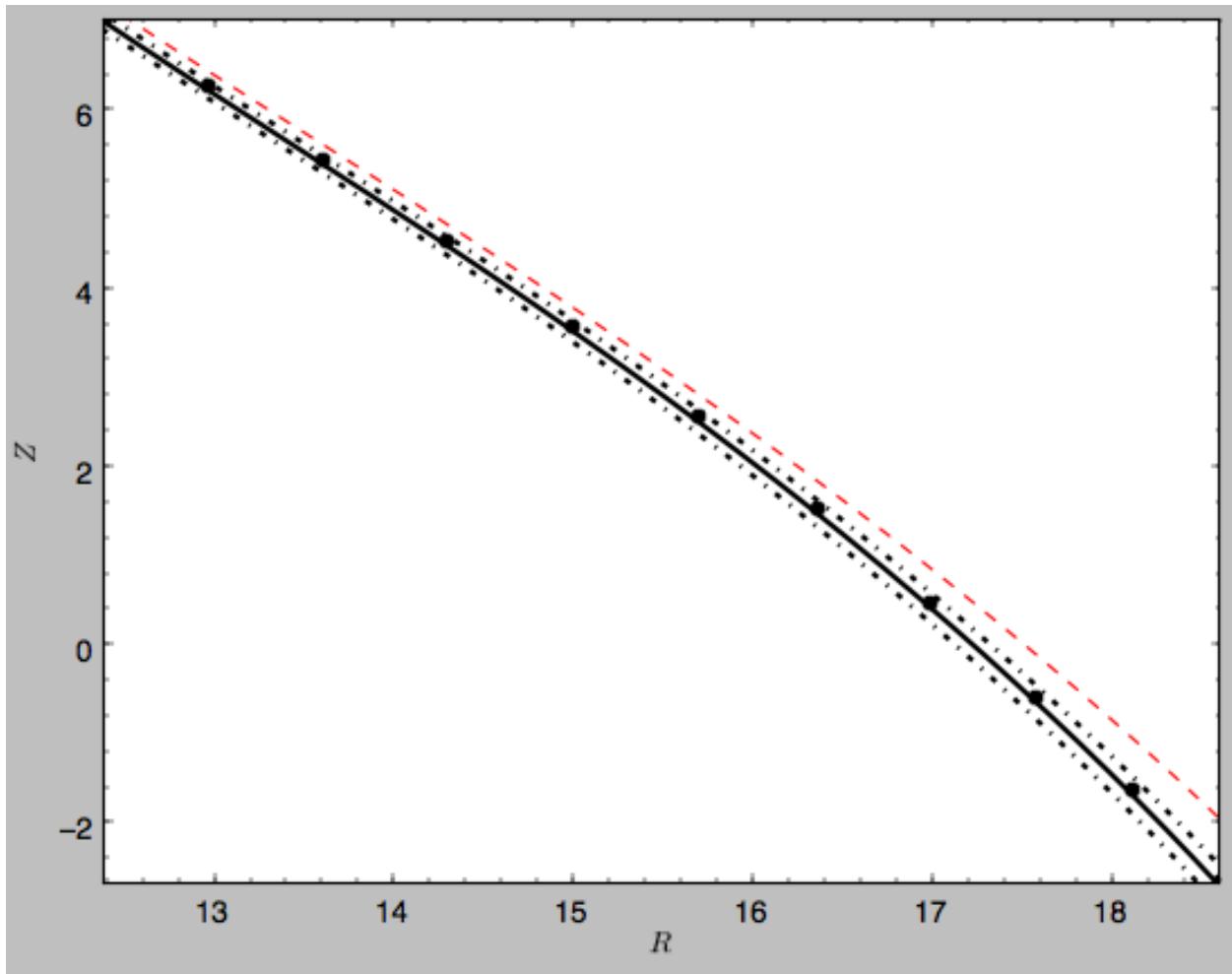
which gives



We can also overplot the orbit of the progenitor

```
>>> sdf.plotProgenitor(d1='r', d2='z', color='r', overplot=True, ls='--', scaleToPhysical=True)
```

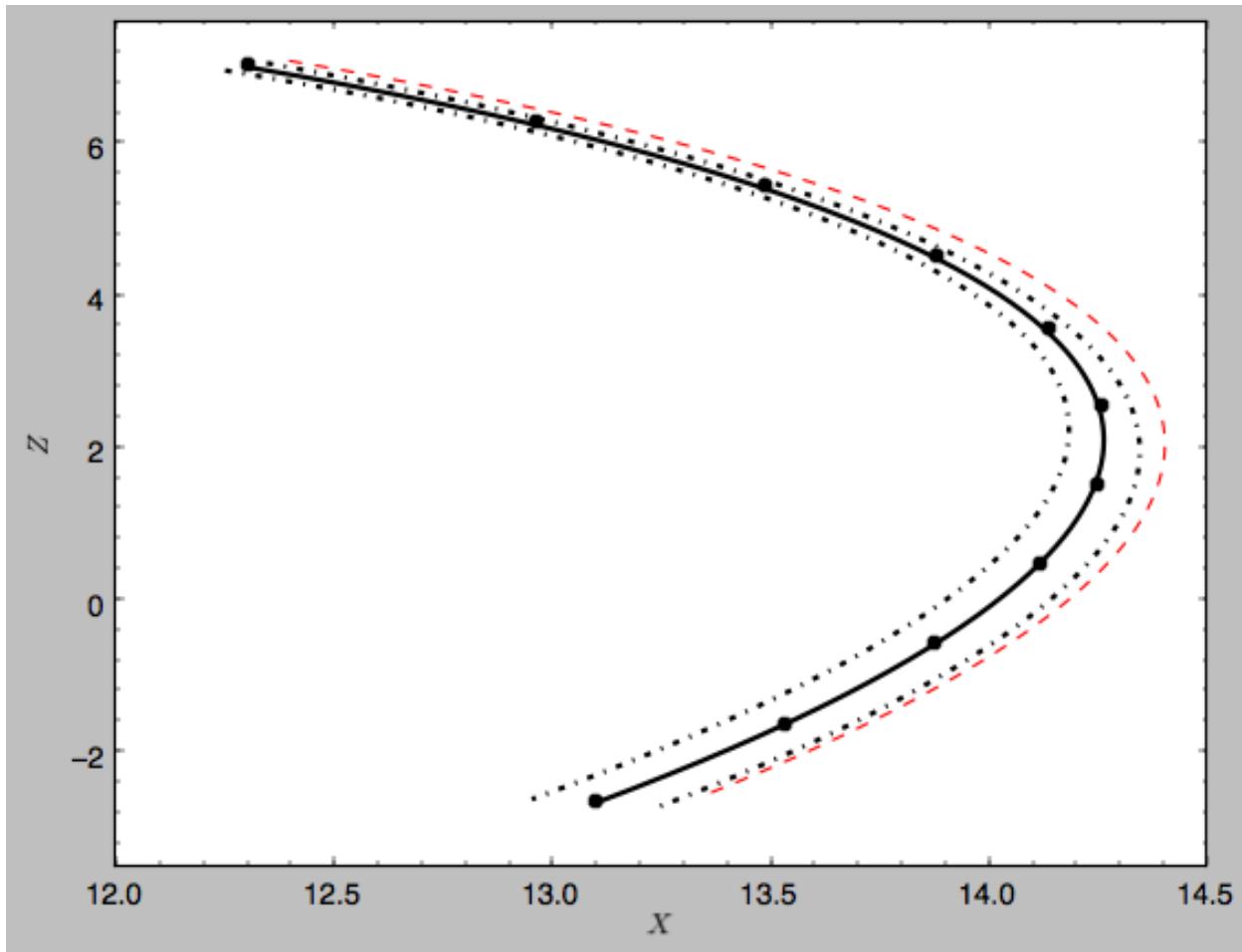
to give



We can do the same in other coordinate systems, for example  $X$  and  $Z$  (as in Figure 1 of Bovy 2014)

```
>>> sdf.plotTrack(d1='x',d2='z',interp=True,color='k',spread=2,overplot=False,lw=2.,scaleToPhysical=False)
>>> sdf.plotTrack(d1='x',d2='z',interp=False,color='k',spread=0,overplot=True,ls='none',marker='o',scaleToPhysical=False)
>>> sdf.plotProgenitor(d1='x',d2='z',color='r',overplot=True,ls='--',scaleToPhysical=True)
>>> xlim(12.,14.5); ylim(-3.5,7.6)
```

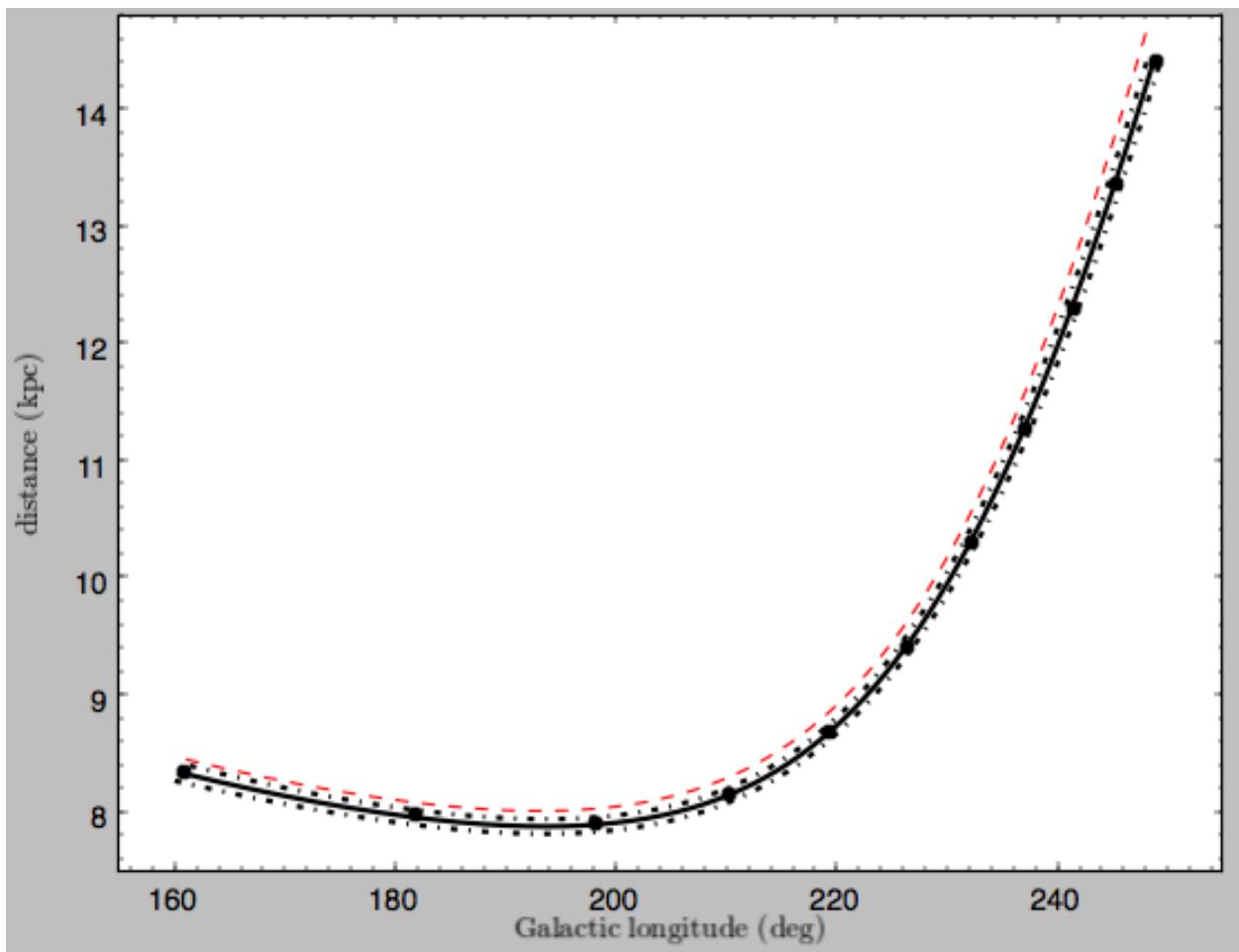
which gives



or we can calculate the track in observable coordinates, e.g.,

```
>>> sdf.plotTrack(d1='ll',d2='dist',interp=True,color='k',spread=2,overplot=False,lw=2.)
>>> sdf.plotTrack(d1='ll',d2='dist',interp=False,color='k',spread=0,overplot=True,ls='none',marker='o')
>>> sdf.plotProgenitor(d1='ll',d2='dist',color='r',overplot=True,ls='--')
>>> xlim(155.,255.); ylim(7.5,14.8)
```

which displays



Coordinate transformations to physical coordinates are done using parameters set when initializing the `sdf` instance. See the help for `?streamdf` for a complete list of initialization parameters.

### 3.1.3 Mock stream data generation

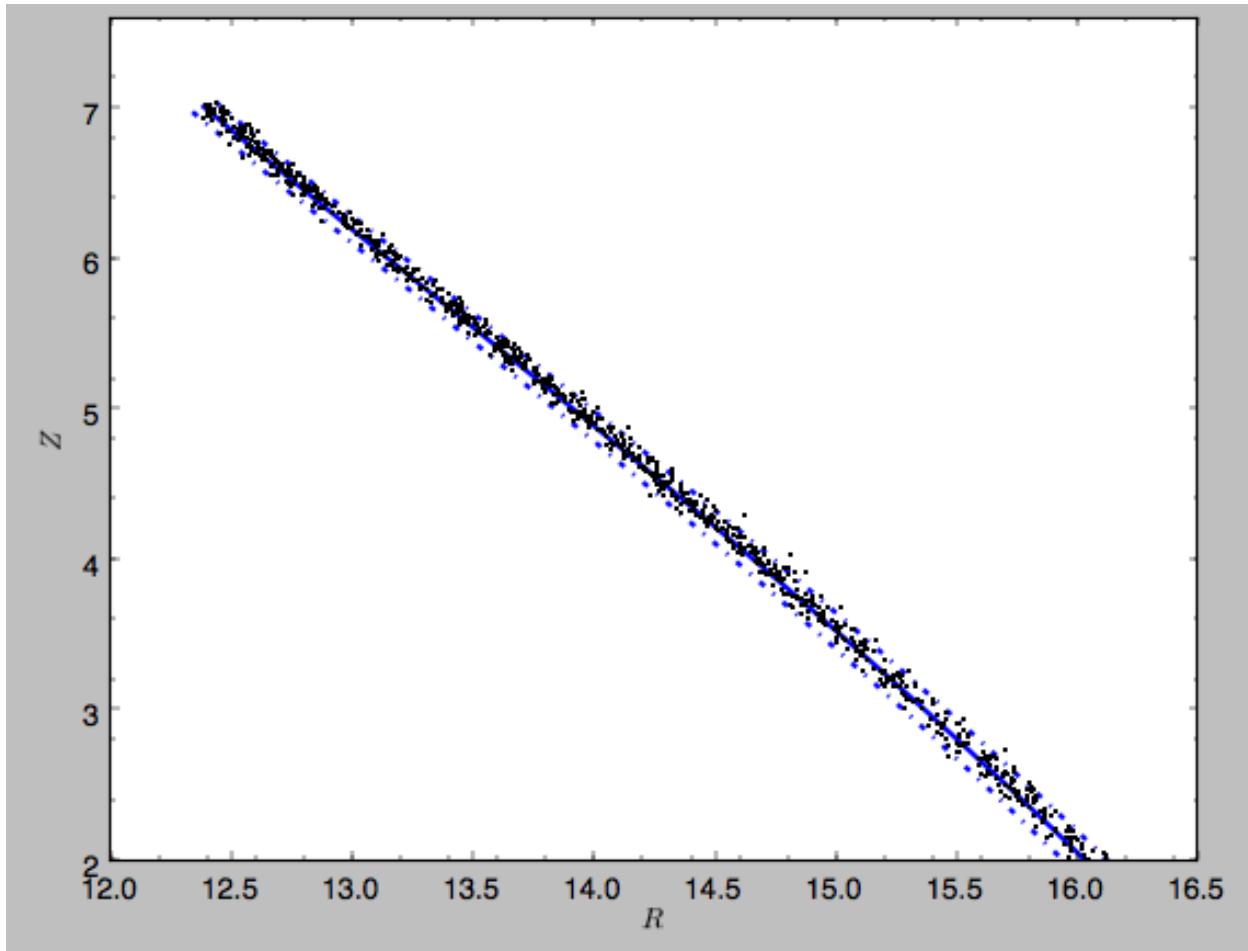
We can also easily generate mock data from the stream model. This uses `streamdf.sample`. For example,

```
>>> RvR= sdf.sample(n=1000)
```

which returns the sampled points as a set  $(R, v_R, v_T, Z, v_Z, \phi)$  in natural galpy coordinates. We can plot these and compare them to the track location

```
>>> sdf.plotTrack(d1='r',d2='z',interp=True,color='b',spread=2,overplot=False,lw=2.,scaleToPhysical=True)
>>> plot(RvR[0]*8.,RvR[3]*8.,'k.',ms=2.) #multiply by the physical distance scale
>>> xlim(12.,16.5); ylim(2.,7.6)
```

which gives



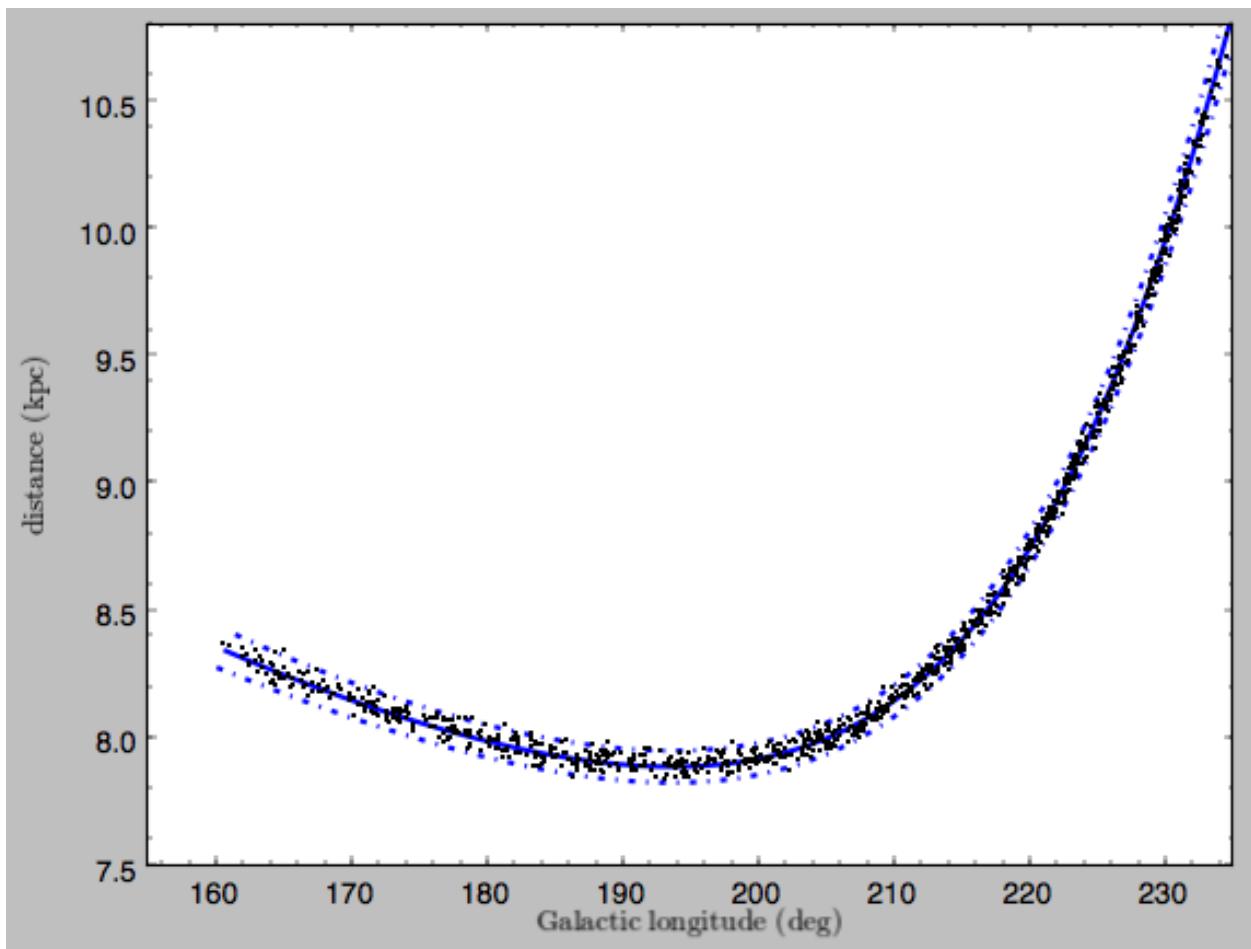
Similarly, we can generate mock data in observable coordinates

```
>>> lb= sdf.sample(n=1000,lb=True)
```

and plot it

```
>>> sdf.plotTrack(d1='ll',d2='dist',interp=True,color='b',spread=2,overplot=False,lw=2.)  
>>> plot(lb[0],lb[2],'k.',ms=2.)  
>>> xlim(155.,235.); ylim(7.5,10.8)
```

which displays

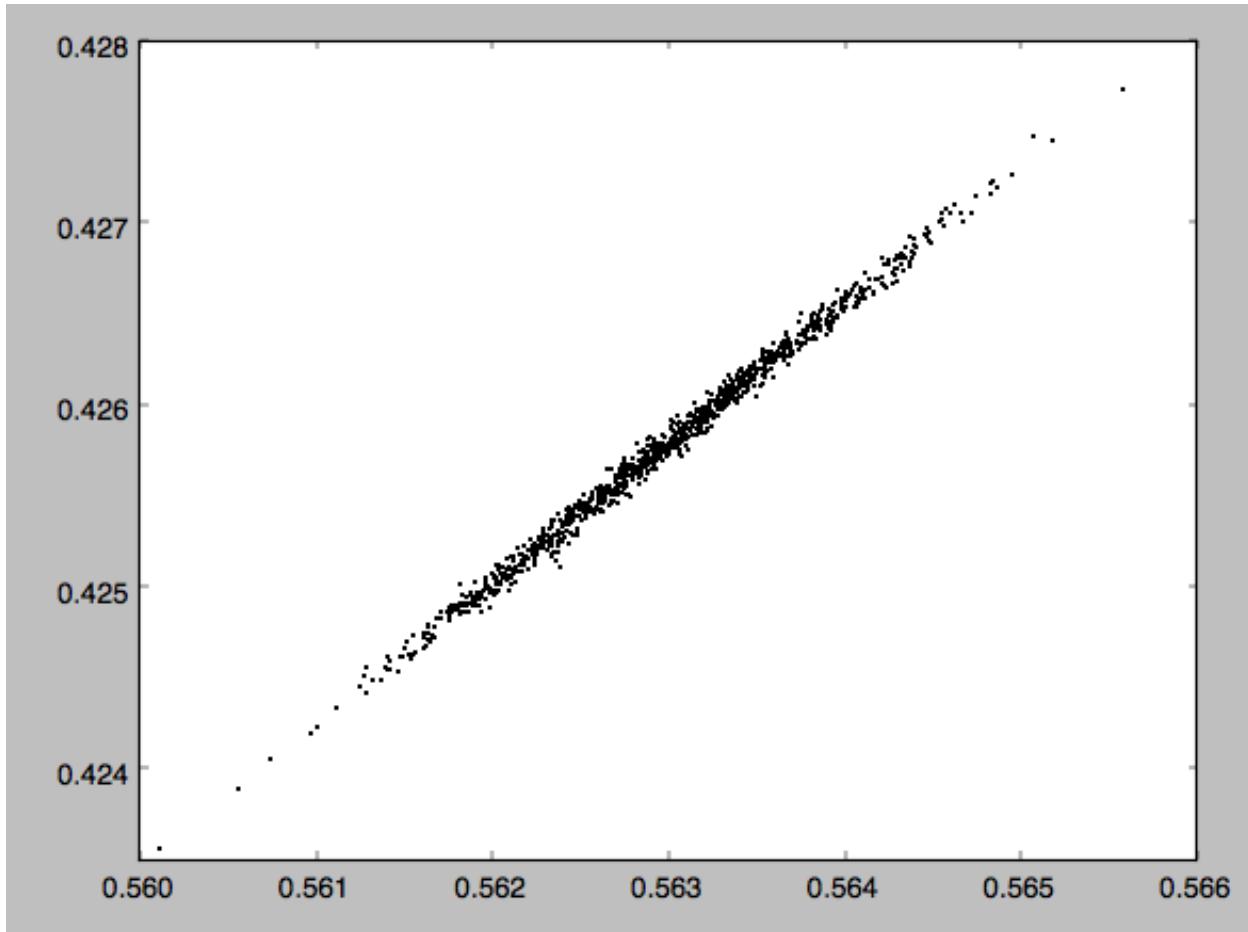


We can also just generate mock stream data in frequency-angle coordinates

```
>>> mockaA= sdf.sample(n=1000,returnaAdt=True)
```

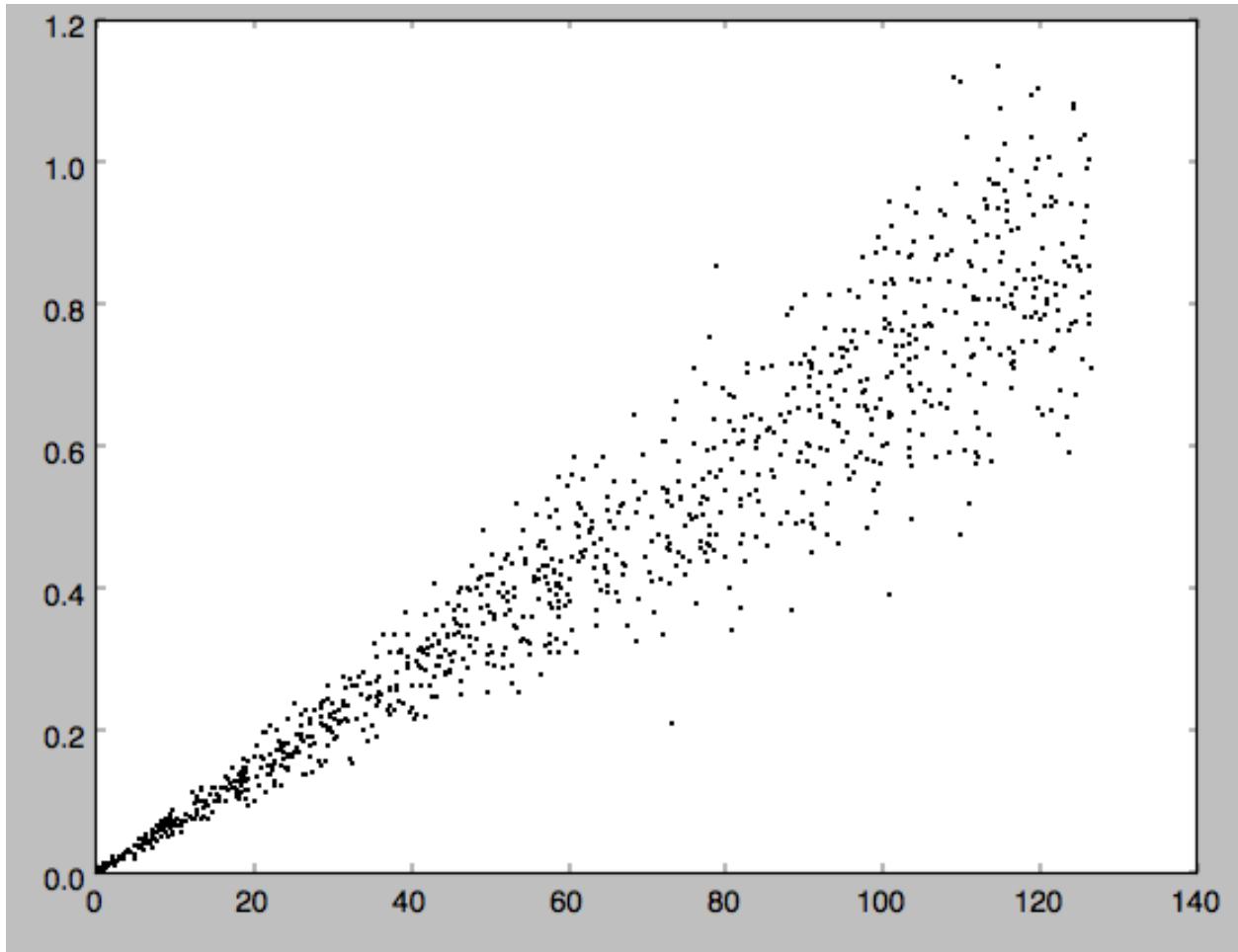
which returns a tuple with three components: an array with shape [3,N] of frequency vectors ( $\Omega_R, \Omega_\phi, \Omega_Z$ ), an array with shape [3,N] of angle vectors ( $\theta_R, \theta_\phi, \theta_Z$ ) and  $t_s$ , the stripping time. We can plot the vertical versus the radial angle

```
>>> plot(mockaA[0][0],mockaA[0][2],'k.',ms=2.)
```



or we can plot the magnitude of the angle offset as a function of stripping time

```
>>> plot(mockaA[2], numpy.sqrt(numpy.sum((mockaA[1]-numpy.tile(sdf._progenitor_angle,(1000,1)).T)**2,
```



### 3.1.4 Evaluating and marginalizing the full PDF

We can also evaluate the stream PDF, the probability of a  $(\mathbf{x}, \mathbf{v})$  phase-space position in the stream. We can evaluate the PDF, for example, at the location of the progenitor

```
>>> sdf(obs.R(), obs.vR(), obs.vT(), obs.z(), obs.vz(), obs.phi())
array([-33.16985861])
```

which returns the natural log of the PDF. If we go to slightly higher in  $Z$  and slightly smaller in  $R$ , the PDF becomes zero

```
>>> sdf(obs.R() - 0.1, obs.vR(), obs.vT(), obs.z() + 0.1, obs.vz(), obs.phi())
array([-inf])
```

because this phase-space position cannot be reached by a leading stream star. We can also marginalize the PDF over unobserved directions. For example, similar to Figure 10 in Bovy (2014), we can evaluate the PDF  $p(X|Z)$  near a point on the track, say near  $Z = 2$  kpc ( $\approx 0.25$  in natural units). We first find the approximate Gaussian PDF near this point, calculated from the stream track and dispersion (see above)

```
>>> meanp, varp = meanp, varp = sdf.gaussApprox([None, None, 2./8., None, None, None])
```

where the input is a array with entries  $[X, Y, Z, vX, vY, vZ]$  and we substitute `None` for directions that we want to establish the approximate PDF for. So the above expression returns an approximation to  $p(X, Y, vX, vY, vZ|Z)$ . This approximation allows us to get a sense of where the PDF peaks and what its width is

```
>>> meanp[0]*8.
14.267559400127833
>>> numpy.sqrt(varp[0,0])*8.
0.04152968631186698
```

We can now evaluate the PDF  $p(X|Z)$  as a function of  $X$  near the peak

```
>>> xs= numpy.linspace(-3.*numpy.sqrt(varp[0,0]),3.*numpy.sqrt(varp[0,0]),21)+meanp[0]
>>> logps= numpy.array([sdf.callMarg([x,None,2./8.,None,None,None]) for x in xs])
>>> ps= numpy.exp(logps)
```

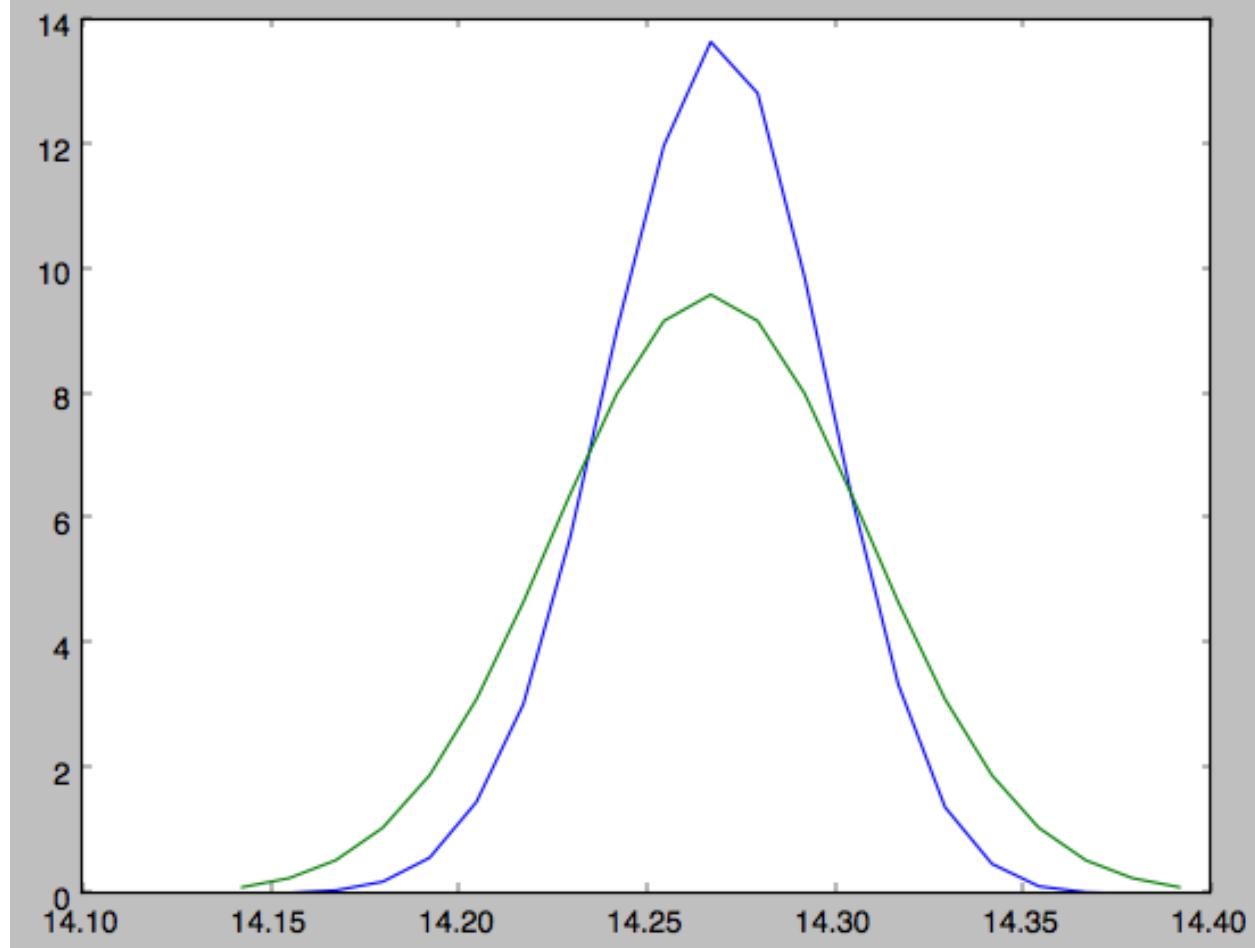
and we normalize the PDF

```
>>> ps/= numpy.sum(ps)*(xs[1]-xs[0])*8.
```

and plot it together with the Gaussian approximation

```
>>> plot(xs*8.,ps)
>>> plot(xs*8.,1./numpy.sqrt(2.*numpy.pi)/numpy.sqrt(varp[0,0])/8.*numpy.exp(-0.5*(xs-meanp[0])**2./varp[0,0]))
```

which gives



Sometimes it is hard to automatically determine the closest point on the calculated track if only one phase-space coordinate is given. For example, this happens when evaluating  $p(Z|X)$  for  $X > 13$  kpc here, where there are two branches of the track in  $Z$  (see the figure of the track above). In that case, we can determine the closest track point on one of the branches by hand and then provide this closest point as the basis of PDF calculations. The following

example shows how this is done for the upper  $Z$  branch at  $X = 13.5$  kpc, which is near  $Z = 5$  kpc (Figure 10 in Bovy 2014).

```
>>> cindx= sdf.find_closest_trackpoint(13.5/8.,None,5.32/8.,None,None,None,xy=True)
```

gives the index of the closest point on the calculated track. This index can then be given as an argument for the PDF functions:

```
>>> meanp, varp= meanp, varp= sdf.gaussApprox([13.5/8.,None,None,None,None],cindx=cindx)
```

computes the approximate  $p(Y, Z, v_X, v_Y, v_Z | X)$  near the upper  $Z$  branch. In  $Z$ , this PDF has mean and dispersion

```
>>> meanp[1]*8.  
5.4005530328542077  
>>> numpy.sqrt(varp[1,1])*8.  
0.05796023309510244
```

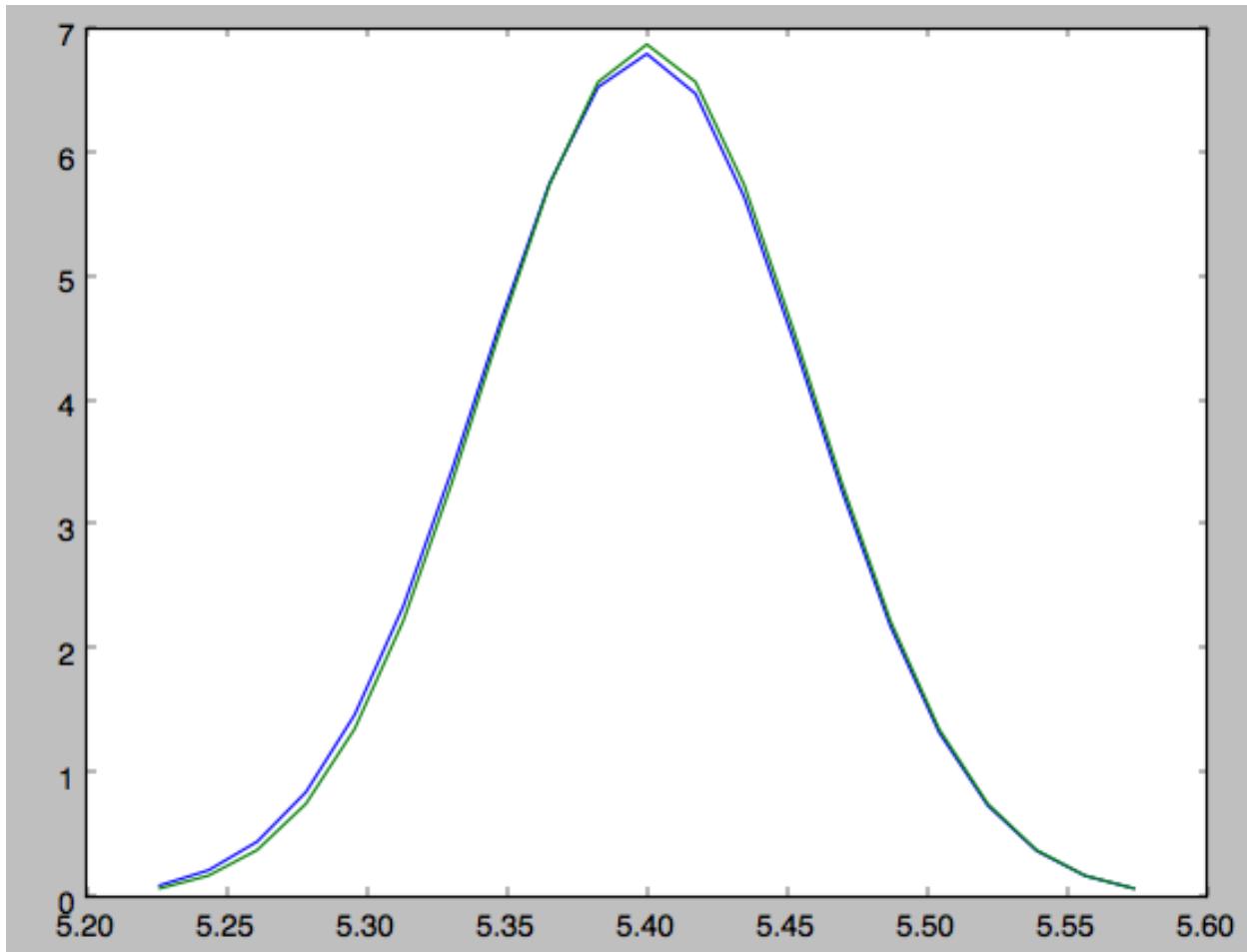
We can then evaluate  $p(Z|X)$  for the upper branch as

```
>>> zs= numpy.linspace(-3.*numpy.sqrt(varp[1,1]),3.*numpy.sqrt(varp[1,1]),21)+meanp[1]  
>>> logps= numpy.array([sdf.callMarg([13.5/8.,None,z,None,None],cindx=cindx) for z in zs])  
>>> ps= numpy.exp(logps)  
>>> ps/= numpy.sum(ps)*(zs[1]-zs[0])*8.
```

and we can again plot this and the approximation

```
>>> plot(zs*8.,ps)  
>>> plot(zs*8.,1./numpy.sqrt(2.*numpy.pi)/numpy.sqrt(varp[1,1])/8.*numpy.exp(-0.5*(zs-meanp[1])**2./v
```

which gives



The approximate PDF in this case is very close to the correct PDF. When supplying the closest track point, care needs to be taken that this really is the closest track point. Otherwise the approximate PDF will not be quite correct.

### Papers using galpy

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Please let me (bovy -at- ias.edu) know if you make use of galpy in a publication.

- ***Tracing the Hercules stream around the Galaxy, Jo Bovy (2010), *Astrophys. J.* 725, 1676 (2010ApJ...725.1676B)***:  
Uses what later became the orbit integration routines and Dehnen and Shu disk distribution functions.
- ***The spatial structure of mono-abundance sub-populations of the Milky Way disk, Jo Bovy, Hans-Walter Rix, Chao Liu, et al. (2011ApJ...732.117)***:  
Employs galpy orbit integration in galpy.potential.MWPotential to characterize the orbits in the SEGUE G dwarf sample.
- ***On the local dark matter density, Jo Bovy & Scott Tremaine (2012), *Astrophys. J.* 756, 89 (2012ApJ...756..89B)***:  
Uses galpy.potential force and density routines to characterize the difference between the vertical force and the surface density at large heights above the MW midplane.
- ***The Milky Way's circular velocity curve between 4 and 14 kpc from APOGEE data, Jo Bovy, Carlos Allende Prieto, Timothy C. Beers, et al. (2012ApJ...756..89B)***:  
Utilizes the Dehnen distribution function to inform a simple model of the velocity distribution of APOGEE stars in the Milky Way disk and to create mock data.
- ***A direct dynamical measurement of the Milky Way's disk surface density profile, disk scale length, and dark matter profile at 4–14 kpc, Jo Bovy, Carlos Allende Prieto, Timothy C. Beers, et al. (2013ApJ...773.113)***:  
Makes use of potential models, the adiabatic and Staeckel actionAngle modules, and the quasiisothermal DF to model the dynamics of the SEGUE G dwarf sample in mono-abundance bins.
- ***Chemodynamics of the Milky Way. I. The first year of APOGEE data, Friedrich Anders, Christina Chiappini, Basilio X. Sanchez, et al. (2013ApJ...773.113)***:  
Employs galpy to perform orbit integrations in galpy.potential.MWPotential to characterize the orbits of stars in the APOGEE sample.



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## Acknowledging galpy

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Please link back to <http://github.com/jobovy/galpy>. When using the `galpy.actionAngle` modules, please cite [2013ApJ...779..115B](#) in addition to the papers describing the algorithm used. When orbit integrations are used, you could cite [2010ApJ...725.1676B](#) (first galpy paper).



## Indices and tables

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- *modindex*
- *search*